NANOWIRE AND FIBER COMPOSITE ELECTROMECHANICAL SENSOR

by

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Fiber or nanowire composites offer many benefits for piezoelectric sensor and actuator applications. Piezoelectric composite is comprised of piezoelectric ceramics lain in polymer matrix. The composite with the piezoelectric ceramics connected in one direction and the polymer in three directions is named as 1-3 composite. 1-3 composites are most ordinary used and the anisotropic alignment of PZT in the composite may substantially lower lateral piezoelectric coupling and increases the sensitivity of the transducer mechanically. Piezoelectric fiber composites are suitable for sensor applications, medical diagnostics and nondestructive testing.

Single crystal zinc-oxide nanowires were synthesized through a simple hydrothermal route and subsequently mixed with polyimide matrix to form ZnO nanocomposites. Superimposed a.c. and d.c. electric fields were applied to microscopically tailor the alignment of ZnO nanowires in polyimide matrix to form anisotropic nanocomposites. Piezoresistive property of ZnO nanocomposite was investigated for strain sensor application. A large gauge factor was obtained from the monotonic uniaxial stress-strain experiment for this nanocomposite and it is much higher than that of ordinary metal strain sensor. A low frequency fiber composite vibration sensor was fabricated and experimentally studied. The global parameters of the composite were substituted into lumped and distributed element constituent equations for piezoelectric unimorph to theoretically predict the sensitivity and effective frequency response range of the vibration
An experiment was carried out to validate the result from the theoretical model. The output voltage per unit input displacement keeps stable in a wide frequency range with a suitable damping ratio. This PZT fiber composite sensor was also applied for soft material strain measurement and soft biomaterial surface morphology and elastic modulus characterization. From the theoretical evaluation and experiment result, this strain sensor is suitable for strain measurement with high sensitivity and high softness. A rectangular breathing sensor and an annular breathing sensor were fabricated for breathing rate and depth monitoring. Both sensors were tested under different physiological conditions and measurement results could be utilized for precaution and monitoring of breathing diseases. Both of them are excellent for monitoring breathing rate and depth and be nice choices for daily use and diagnose purpose.
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1.0 INTRODUCTION

In this chapter, some basic concepts including piezoelectricity, electrostriction, piezoelectric constitutive equations, piezoelectric configurations, piezoelectric materials, and piezoelectric fiber composite will be introduced. Fabrication, electromechanical and dielectric properties, and application of fiber composite will be focused and detailed. Piezoresistive materials and their sensor applications will also be introduced.

1.1 PIEZOELECTRICITY, ELECTROSTRICITION AND THEIR DIFFERENCES

First, the distinction between electrostriction and piezoelectricity will be clarified and it will be helpful to understand piezoelectricity. “It is this reversal of sign of strain with sign of field that distinguishes piezoelectricity from electrostriction” is the difference stated by Cady [1]. Piezoelectricity reveals a linear relationship between mechanical strain and electric field while electrostriction reveals a nonlinear relationship between them (Fig. 1.1). Natural piezoelectric materials which have a linear response to small electric fields will also reveal nonlinearity under high electric fields. Such nonlinearity is caused by weak electrostriction which becomes more important relative to piezoelectricity under higher electric fields.
Curie brothers observed piezoelectric effect first. Mechanical stress caused generation of electric charge is called the direct piezoelectric effect and the length change of materials in an electric field is called the inverse piezoelectric effect. Piezoelectricity occurs in crystal structures which don’t have central symmetry [2]. If an electric field is applied parallel to the length of a bar of piezoelectric crystal, the bar will get longer with the electric field applied in one direction and become shorter with the electric field applied in the opposite direction. A polycrystalline piezoelectric material reveals no macroscopic piezoelectric effect because the piezoelectric effects in randomly-oriented piezoelectric crystallites cancel. For piezoelectric single crystal, it does have piezoelectric effect. Quartz was the first discovered piezoelectric material, followed by others such as Rochelle salt, lithium sulfate and so on.

Electrostriction occurs in all dielectric materials. But only in ferroelectric materials which contain domains, the electrostriction effect is big enough for practical use [3]. The electric field can align the domains in these materials and will cause significant dimensional changes. If an electric field is applied parallel to the length of a bar of electrostrictive material, it will get longer regardless of the direction of the field. Thus the mechanical response is not proportional to the electric field but relies on the square and higher even powers of the field. And if a mechanical stress is applied to the bar, there will be no generation of electric charge. When a much larger bias field is applied to the electrostrictive material, a linear response can be received under the
applied alternating drive field. The bias field creates a polar axis of symmetry and causes a stable displacement along that axis. Then a superimposed alternating drive field causes an alternating displacement around the stable displacement. The approximately linear, reciprocal mechanical response generated from the alternating drive field can be seen in Fig. 1.2. The isotropic polycrystalline electrostrictive material is converted to isotropic material in planes vertical to the polar axis by the bias voltage. This biased electrostrictive material can be seen as a piezoelectric material.

![Figure 1.2](image)

**Figure 1.2.** Electrostrictive material with maintained static bias field $E_0$ and static strain $S_0$ and the alternating field $E_1$ follows a minor hysteresis loop and causes an alternating strain $S_1$ [3]

### 1.2 PIEZOELECTRIC CONSTITUTIVE EQUATIONS, MATERIALS AND CONFIGURATIONS

Familiar piezoelectric materials include piezoelectric single crystals and piezoelectric textures. Piezoelectric single crystals include quartz, tourmaline, gallium orthophosphate, crystals of the Ca$_3$Ga$_2$Ge$_4$O$_{14}$ (CGG) group, Rochelle salt, lithium sulfate and several other piezoelectric single crystals. Piezoelectric textures include piezoelectric ceramics and piezoelectric polymers, such as PVDF and related copolymers. Piezoelectric ceramics include PZT family, lead metaniobate, KNN family, bismuth titanate family, perovskite layer structure, AlN, ZnO piezoelectric thin
film and so on. Lead zirconate titanate (PZT) exhibits outstanding piezoelectric properties, and has been widely used in industry, science, medicine and communications fields.

The electrostrictive materials include high coercive force kind and low coercive force one. After the bias is removed, those with high coercive force will retain large amount of remnant polarization. But those with low coercive force need the bias to maintain the polarization. Barium titanate and PZT are ferroelectric materials with a high coercive force. After a high polarizing field applied to them and removed, the domains still keep partially aligned in one direction. This remnant polarization of them nearly has a linear relation with the alternating electric field which can be seen from Fig. 1.3. BaTiO$_3$ and PZT have excellent piezoelectric effect due to the stable and large remnant polarization. But high temperature, high static pressure cycling in deep water applications, high alternating electric fields will lead to depolarization of them [4]. The internal crystal structure determines the properties of true piezoelectrics which will not be affected by outer conditions. But the level of remnant achieved in the polarization process decides the piezoelectric properties of polarized electrostrictive materials which will be influenced by outer environment. Permanently polarized BaTiO$_3$ and PZT can be thought as piezoelectric and they can be made in the form of ceramics conveniently.

![Figure 1.3](image)

**Figure 1.3.** Polarization and strain vs. electric field showing remnant polarization, $P_0$ (a), and remnant strain, $S_0$ (b), when the field is removed. Application of the alternating field $E_1$ then causes alternating strain $S_1$ about the remnant strain $S_0$. [3]
Lead magnesium niobate (PMN), lead zirconium niobate (PZN) and mixtures with lead titanate (PMN-PT) or (PZN-PT) are ferroelectric materials with strong electrostrictive properties but low coercive force. The remnant polarization in them can be utilized for low field applications. If a steady electric bias applied to them, they are suitable for high field applications with a linear response.

The piezoelectric constitutive equations in this discussion are restricted to linear effect. So a set of linear equations which relate stress tensor $T$, strain tensor $S$, electric field intensity tensor $E$, and electric displacement tensor $D$ can be utilized to describe the piezoelectric effect. Adiabatic conditions are assumed in most of the situations and temperature and entropy variables will be neglected in these equations. But the coefficients in these equations are temperature dependent. Only six independent components in symmetric second rank tensors $T$ and $S$ will be considered. The phenomenological equations will be written as two matrix equations:

\begin{align}
S &= s^e T + d^t E \\
D &= d T + e^T E \\
T &= c^e S - e^t E \\
D &= e S + e^s E \\
S &= s^D T + g^t D \\
E &= -g T + \beta^T D \\
T &= c^D S - h^t D \\
E &= -h S + \beta^S D
\end{align}

where the matrixes with superscript “t” are transpose of these matrixes. $s^D$ and $s^e$ are elastic compliance coefficient tensors under constant electrical displacement and constant electric-field intensity conditions respectively; $d$ is the piezoelectric strain coefficient tensor; $e^T$ and $e^s$ are permittivity tensors under constant stress and constant strain conditions respectively; $c^D$ and $c^e$
are the stiffness coefficient tensors under constant electric displacement and constant electric-field intensity conditions respectively; \( e \) is the piezoelectric stress coefficient tensor; \( g \) is the piezoelectric voltage coefficient tensor; \( h \) is the piezoelectric charge coefficient tensor; and \( \beta^T \) and \( \beta^S \) are permittivity tensors under constant stress and constant strain conditions respectively. Each of them is proportional to a partial derivative when the superscript variable keeps being constant. For example, the permittivity tensor under constant stress can be measured from the slope of the curve of electrical displacement versus electric-field intensity while the stress is held to be constant. Because \( d = (\partial D/\partial T)_E = (\partial S/\partial E)_T \) which can be derived from thermodynamic potentials, the superscript for parameter \( d \) is omitted. This is the reason for the electromechanical reciprocity. These coefficients have some general relationships which can convert results obtained from one pair of equations to the notations in another pair. There are totally 40 different coefficients, but they are not independent.

Familiar piezoelectric configurations include 33-mode longitudinal plate, 31-mode longitudinal plate, 31-mode ring, 33-mode ring, spherical, piston, tonpilz, hybrid, transmission line, composite, flextensional, flexural, bender bar, bender disk, slotted cylinder, bender mode X-spring and so on. And a brief discussion will be given on 33-mode and 31-mode longitudinal plate, which are the most ordinary structures.

A one-dimensional longitudinal vibration piezoelectric ceramic plate will be analyzed in the following part. It has a length \( L \) which is assumed to be less than a quarter wave length of longitudinal waves in the ceramic. A stress \( T \) acts on the surface of the plate along the 3 direction (Fig. 1.4). Two electrodes are attached to the ends of the plate to polarize it and establish the polar axis along the length direction. An alternating electric field \( E_3 \) is created parallel to the polarization direction by applying an alternating voltage \( V \) to the plate. Electric fields \( E_1, E_2 \) can
be assumed to be zero across the plate and the longitudinal electric field does not generate shear stresses. So equation 1.1 will be

\[ S_1 = s_{11}^E T_1 + s_{12}^E T_2 + s_{13}^E T_3 + d_{31} E_3 \]  

(1.5)

\[ S_2 = s_{12}^E T_1 + s_{11}^E T_2 + s_{13}^E T_3 + d_{31} E_3 \]  

(1.6)

\[ S_3 = s_{13}^E T_1 + s_{13}^E T_2 + s_{33}^E T_3 + d_{33} E_3 \]  

(1.7)

\[ D_3 = d_{31} T_1 + d_{33} T_2 + d_{33} T_3 + \varepsilon_{33}^T E_3 \]  

(1.8)

![Figure 1.4. The 33 mode piezoelectric longitudinal vibrator with working strain parallel to poling direction and electrodes on the ends of the plate](image)

The stresses \( T_1 \) and \( T_2 \) are zero on the surfaces of the sides and throughout the plate. Because the sides of the plate are not restricted by anything and the lateral dimensions are small compared to the length. So these equations can be changed to:

\[ S_1 = s_{33}^E T_3 + d_{31} E_3 \]  

(1.9)

\[ S_2 = s_{33}^E T_3 + d_{31} E_3 \]  

(1.10)

\[ S_3 = s_{33}^E T_3 + d_{33} E_3 \]  

(1.11)

\[ D_3 = d_{33} T_3 + \varepsilon_{33}^T E_3 \]  

(1.12)

These lateral strains are caused by the main strain modified by the Poisson ratio effect. But they have no real effect to the actual application.
Another longitudinal vibration piezoelectric ceramic plate is the same with the above one, but excited in 31-mode. It has lower coupling coefficient but also with lower possibility to be depolarized by static pressure cycling because the polarization direction is vertical to the static stress direction [4, 5]. A plate with lateral dimensions h and w which has been polarized along length direction is shown in Fig. 1.5. Now the polar axis is parallel to the length direction and vertical to side direction. A stress $T$ acts on the surface of the plate along the 1 direction. $T_1$ is the only stress component that is not zero and $E_3$ is the only electric field component that has value. In this situation, equation (1.1) can be expanded to

$$S_1 = s_{11}E_1 + d_{31}E_3$$  \hspace{1cm} (1.13)

$$S_2 = s_{12}E_1 + d_{31}E_3$$  \hspace{1cm} (1.14)

$$S_3 = s_{13}E_1 + d_{33}E_3$$  \hspace{1cm} (1.15)

$$D_3 = d_{31}T_1 + e_{33}^T E_3$$  \hspace{1cm} (1.16)

**Figure 1.5.** The 31 mode piezoelectric longitudinal vibrator with working strain perpendicular to poling direction and electrodes on the sides of the plate
1.3 PIEZOELECTRIC FIBER COMPOSITE

1.3.1 Modeling

Piezoelectric composite is comprised of piezoelectric ceramics components lain in polymer matrix, such as epoxy, silicone rubber, polyurethane, polyethylene and so on. Newnham [6] named the composite which describes the connectivity of the piezoelectric material and polymer matrix. Several different piezocomposite configurations in current use are illustrated in Fig. 1.6. The composite with the piezoelectric ceramic connected in one direction and the polymer in three directions is named as 1-3 connectivity. The composite with piezoelectric ceramic particles dispersed in polymer matrix with no connection to each other and the polymer connected in three directions is named as 0-3 connectivity. The composite with both the piezoelectric ceramic and polymer connected in two directions is named 2-2 connectivity. The 2-2 composites can be manufactured by dice-and-fill technique and now have been used in medical field. 0-3 composites with low volume percentages of piezoelectric materials are more suitable as sensors than as actuators. They have very high flexibility but are difficult to be polarized. 1-3 composites are most ordinary used and will be discussed in detail in the following part.

![Composite Configurations](image)

*Figure 1.6. Three piezocomposite configurations in current use for transducers [3]*
In the 1-3 composites as illustrated in Fig. 1.7, the piezoelectric materials are in the shape of rods and not connected in x and y directions while the polymer is connected in all three directions. Because the 1-3 composites can be manufactured with high volume fraction of the piezoelectric materials, they can be tailored with high coupling coefficient and broad-band properties. They can be operated under high pressure without noticeable changes in performance and function as sensors or actuators. The performance of the composite depends on several factors, such as the specific material, the volume fraction, and aspect ratio of the piezoelectric rods, the composition of the polymer, the electrode or packaging material stiffness, the spatial array period compared to the wavelength in the composite, and the overall size compared to the wavelength in the surrounding medium.

1-3 composites can be manufactured in high volume at a low cost by injection molding technology [7] compared to manufacture solid sheet of piezoelectric material. Regular arrays of round and square piezoelectric rods are most ordinary configurations for 1-3 composites. The
width of the rod ranges from 20μm to 5 mm. 1-3 composite with 15% PZT-5H and 85% polymer matrix is compared with solid piezoelectric ceramic PZT-5H in Table 1.1 [8].

Table 1.1. Comparison of 1-3 Composite and PZT-5H

<table>
<thead>
<tr>
<th>Property</th>
<th>Units</th>
<th>1-3 Composite</th>
<th>PZT-5H</th>
</tr>
</thead>
<tbody>
<tr>
<td>Relative Dielectric Constant</td>
<td></td>
<td>460</td>
<td>3200</td>
</tr>
<tr>
<td>Dissipation Factor</td>
<td></td>
<td>0.02</td>
<td>0.02</td>
</tr>
<tr>
<td>Coupling Coefficient $k_t$</td>
<td></td>
<td>0.63</td>
<td>0.51</td>
</tr>
<tr>
<td>Mechanical Q</td>
<td></td>
<td>20</td>
<td>65</td>
</tr>
<tr>
<td>$d_{33}$</td>
<td>(pC/N)</td>
<td>550</td>
<td>650</td>
</tr>
<tr>
<td>Impedance</td>
<td>(Mrayls)</td>
<td>6</td>
<td>30</td>
</tr>
<tr>
<td>Density</td>
<td>(kg/m$^3$)</td>
<td>1800</td>
<td>7500</td>
</tr>
</tbody>
</table>

Smith and Auld [9] developed a thickness mode model to calculate the essential parameters of the 1-3 piezoelectric fiber polymers composite. These parameters can be expressed as a function of the volume fraction $\nu$ of the piezoelectric ceramics. Avellaneda and Swart [10] also developed a tensor model which is more complicated and will not be detailed here. In the Smith-Auld model, piezoelectric constitutive equations in the 3 direction are utilized as origin and strain and electric field components are selected to express the stress and electric displacement components:

$$T_3 = e_{33}^E S_3 - e_{33}^t E_3$$  \hspace{1cm} (1.17)

$$D_3 = e_{33} S_3 + e_{33}^s E_3$$  \hspace{1cm} (1.18)

Some assumptions and approximations are proposed here to simplify the derivation of the expressions for all the coefficients. The ceramic and polymer are assumed to move together in a uniform thickness oscillation and the strains in the 3 direction are the same in both phases,

$$S_3^p = S_3^t = \overline{S}_3$$  \hspace{1cm} (1.19)
The composite plates are electroded and equipotential, so the electric fields are the same in both phases,

\[ E_3^p = E_3^c = \overline{E_3} \]  

(1.20)

Electric field intensity component \( E_3 \) and strain component \( S_3 \) are assumed to be the same in the piezoelectric material and polymer. Piezoelectric ceramic element and its adjacent polymer in the composite look like a cell in the composite. The stresses in the polymer are the same to those in the piezoelectric ceramic in lateral directions. The lateral components of strain and electric field intensity are thought to be zero throughout the composite. The effective strains \( S_1 \) and \( S_2 \) at the cell surfaces and throughout the cell are equal to zero, so clamped boundary conditions are assumed along the lateral directions in thickness mode operation of the composite.

\[ T_1^p = T_1^c = \overline{T_1} \]  

(1.21)

\[ S_1 = \nu S_1^c + (1-\nu)S_1^p = 0 \]  

(1.22)

\[ S_1^p = -S_1^c \nu/(1-\nu) \]  

(1.23)

where the superscripts \( c \) refer to piezoelectric ceramic and \( p \) refer to polymer respectively. \( \nu \) is the volume fraction of the piezoelectric ceramics. The same relation can be derived for strain \( S_2 \) and the effective density is expressed as

\[ \rho = \nu \rho^c + (1-\nu)\rho^p \]  

(1.24)

Since the lateral periodicity is sufficiently fine, the effective total stress and electric displacement can be expressed by averaging the contributions of the constituent phases,

\[ \overline{T_3} = \nu T_3^c + (1-\nu)T_3^p \]  

(1.25)

\[ \overline{D_3} = \nu D_3^c + (1-\nu)D_3^p \]  

(1.26)
After substituting all these conditions into the model, it will give the effective values for the stiffness coefficient under constant electric-field intensity condition $c^E$, permittivity under constant strain condition $e^S$ and the piezoelectric stress coefficient $e$. Several effective values for the composite can be expressed as

$$
e_{33}^E = \nu [e_{33}^{Ec} - 2(e_{13}^{Ec} - c_{12}^{Ep})^2 / c] + (1 - \nu) c_{11}^{Ep} \quad (1.27)$$

$$e_{33} = \nu [e_{33}^c - 2e_{31}^c (c_{13}^{Ec} - c_{12}^{Ep}) / c] \quad (1.28)$$

$$\varepsilon_{33}^S = \nu [\varepsilon_{33}^{Sc} + 2(e_{31}^c)^2 / c] + (1 - \nu) e_{11}^{Ep} \quad (1.29)$$

$$c = c_{11}^{Ep} + c_{12}^{Ep} + \nu (c_{11}^{Ep} + c_{12}^{Ep})/(1 - \nu) \quad (1.30)$$

If $D$ and $S$ are chosen as the independent variables in the piezoelectric constitutive equations, the 33-mode equations of this model may be expressed as

$$T_3 = c_{33}^D S_3 - h_{33} D_3 \quad (1.31)$$

$$E_3 = -h_{33} S_3 + (1 / \varepsilon_{33}^S) D_3 \quad (1.32)$$

$$h_{33} = e_{33}^c / \varepsilon_{33}^S \quad (1.33)$$

$$c_{33}^{Ep} = c_{33}^E + (e_{33}^c)^2 / \varepsilon_{33}^S \quad (1.34)$$

This model with several different compositions as a function of the volume fraction has been evaluated numerically by Smith and Auld [9]. The effective density $\rho$ and the effective relative dielectric constant $\varepsilon_{33}^S$ increase linearly with the increase of volume fraction of piezoelectric material. But the effective elastic constant $c_{33}^D$ and the effective piezoelectric constant $e_{33}$ don’t increase linearly with the increase of volume fraction when it is larger than three quarters. As the volume fraction increases, the PZT rods will be affected laterally by adjacent PZT rods.
This model may be used to describe the composite piezoelectric sensor (Fig. 1.8) if the sensor only operates in 33-mode. If any lateral effect applies on the sensor synchronously, the sensitivity will be lowered. If a piezoelectric sensor made of block material is immersed in an acoustic pressure field and small compared to the wavelength, the pressure on every surface is nearly the same and the sensor output will be nearly zero. The output signal includes all the three modes- 31, 32, and 33 modes and the 31 and 32 modes have the same g constants which is nearly minus half times of the g constant of 33 mode. If a 1-3 composite sensor is exposed to the same environment, the influences of 31 and 32 modes will be very low and a much larger sensitivity can be obtained from the sensor. From the hydrostatic model by Smith [11], the effective \( d_{33} \) value and \( d_{31} \) value will decrease 20\% and 40\% which will lead to an improvement for \( d_h \).

![Figure 1.8. 1-3 composite model for sensor [3]](image)

The sensitivity for the composite sensor below resonance can be written as

\[
M = \frac{V}{p} = (g_{33} + 2g_{31})t = g_h t
\]  \hspace{1cm} (1.35)

where \( V \) is the open circuit output voltage, \( p \) is the acoustic pressure and \( t \) is the thickness along the polarization direction. The effective piezoelectric voltage constant \( g \) is

\[
g_h = g_{33} + 2g_{31} = \frac{d_h}{\varepsilon_{33}^T}
\]  \hspace{1cm} (1.36)

\[
d_h = d_{33} + 2d_{31}
\]  \hspace{1cm} (1.37)
This hydrostatic model is derived from the piezoelectric constitutive equations 1.1, with the same definitions for $s^E$, $\varepsilon^T$ and $d$ and nearly similar assumptions as that for actuator thickness model. The lateral spatial scale of the composite is so fine that the vertical strains are the same in both phases,

$$S_3^p = S_3^c = \overline{S_3}$$  \hspace{1cm} (1.38)

The composite plate is electroded and equipotential, so the electric plates are the same in both phases,

$$E_3^p = E_3^c = \overline{E_3}$$  \hspace{1cm} (1.39)

The stresses in the polymer are the same to those in the piezoelectric ceramic in lateral directions. The lateral stresses are equal in both phases,

$$T_1^p = T_1^c = \overline{T_1}$$  \hspace{1cm} (1.40)

One difference between these two models is that the effective lateral strain $S_1$ is not zero in the hydrostatic model. It is the sum of the strain in the ceramic $S_1^c$ and the strain in the polymer $S_1^p$ proportioned to the volume fraction,

$$S_1 = \nu S_1^c + (1-\nu)S_1^p$$  \hspace{1cm} (1.41)

The effective stress and electric displacement of the composite can be expressed by averaging the contributions of the constituent phases,

$$\overline{T_3} = \nu T_3^c + (1-\nu)T_3^p$$  \hspace{1cm} (1.42)

$$\overline{D_3} = \nu D_3^c + (1-\nu)D_3^p$$  \hspace{1cm} (1.43)

After substituting all these conditions into the model, several effective values for the composite can be derived from these assumptions and they can be expressed as

$$d_{33} = \nu s_{11}^E d_{33}^c / s$$  \hspace{1cm} (1.44)
\[ d_{31} = \nu d_{31}^{E} + \nu(1-\nu)(s_{12}^{E} - s_{11}^{E})d_{31}^{E}/s \]  

(1.45)

\[ \varepsilon_{33}^{T} = \nu \varepsilon_{33}^{E} + (1-\nu)\varepsilon_{11}^{E} - \nu(1-\nu)d_{33}^{2}/s \]  

(1.46)

\[ s_{33}^{E} = s_{33}^{E} - s_{11}^{E}/s \]  

(1.47)

\[ s_{13}^{E} = [\nu s_{13}^{E} + s_{11}^{E}] / s \]  

(1.48)

\[ s_{11}^{E} + s_{12}^{E} = \nu s_{11}^{E} + s_{12}^{E} - 2(s_{13}^{E})^{2}/s_{33}^{E} + (1-\nu)[s_{11}^{E} + s_{12}^{E} - 2(s_{12}^{E})^{2}/s_{11}^{E}] + \]  

(1.49)

\[ 2(\nu s_{13}^{E})^{2}/s_{33}^{E} + (1-\nu)s_{12}^{E}/s_{11}^{E})s_{13}^{E} \]

\[ s_{h}^{E} = s_{33}^{E} + 2(s_{11}^{E} + s_{12}^{E}) + 4s_{13}^{E} \]  

(1.50)

\[ s = (1-\nu)s_{33}^{E} + \nu s_{11}^{E} \]  

(1.51)

This hydrostatic model has also been compared with finite element analysis calculation results by Hayward, Bennett, and Hamilton [12]. And the model is in agreement with the calculation on the volume fraction for maximum performance. Another tensor mode for the composite hydrostatic model has also been developed by Avellaneda and Swart [10]. And they get the conclusions that a polymer with embedded air-filled voids will lower the lateral mode effectively. If the Poisson’s ratio of the polymer is smaller than \( -d_{31}/d_{33} \), the sensitivity of the lateral modes will decrease obviously and the effective \( g_{h} \) will increase and have the largest value.

The equivalent circuit for the composite is shown in Fig. 1.9. Here the sensor is assumed to be operated well below the first resonance frequency of the piezoelectric composite sample. The output voltage equals the product of effective piezoelectric voltage constant, the thickness along the polarization direction and the acoustic pressure. If square root of the front surface area of the composite sensor is larger than the sound wavelength in the medium, the pressure is twice as the original value at the surface. The electrical impedance is composed of the free capacity \( C_{f} \).
parallel together with the shunt dissipation resistor $R_0$. And the resistor equals the inverse of the product of the free capacity, the dissipation factor $\tan \delta$ and the angular frequency $\omega$. A matching layer can be added in front of the 1-3 composite and a tail mass can be added to the back [13].

![Equivalent Circuit Diagram]

**Figure 1.9.** Simplified low frequency piezoelectric sensor equivalent circuit [3]

### 1.3.2 Fabrication

Piezoelectric fiber composite has many benefits compared to bulk piezoelectric ceramics for ultrasonic transducer applications [14]. It has lower acoustic impedance than bulk material and much better impedance match to the media. It has higher coupling coefficient than bulk material and can convert more electrical energy into mechanical energy. It lowers lateral piezoelectric coupling and increases the sensitivity of the transducer. It has much higher flexibility than bulk material and is much easier to be attached to any curved structure. So fiber composite is suitable for sensor applications, medical diagnostics and nondestructive testing. Dice-and-fill technique [15] is usually used to fabricate 1-3 fiber composite. Several cuts are made to the polarized piezoceramics block parallel in one direction and the other several cuts are made parallel and vertical to this direction. The void spaces between the fibers are then filled with polymer and
baked at a suitable temperature. The composite block is cut into required shapes finally. This technique usually cost a long time and the generated element is limited to regular and cube-shaped composite structure. Several new technologies, such as injection molding [16], the lost mold method [17, 18], the soft-mold method [19] and fiber insertion methods [20] were developed to overcome these disadvantages.

Smart materials with embedded fibers to reinforce the structure and sense and actuate the acoustics media inspirit the development of piezoelectric fiber composite [21]. The sol-gel process is a promising way to fabricate thin and separated fibers at low temperature [22]. The PZT fibers produced by several different groups with this method have diameters ranging from 10 to 50 µm [23-27]. Because the fibers can be sintered at low temperature (<1,000°C), the fabricated fibers can be handled in the sintered state as single filaments [28]. The achieved fiber performance can be improved by tailoring the microstructure and the chemical composition of the solution. If lead magnesium niobate (PZT-PMN) is added into PZT to format the solid solution, the dielectric constant and the piezoelectric charge constant can be increased considerably.

The fibers are picked and placed to obtain aligned fiber bundles for the piezoelectric fiber/polymer composite fabrication (Fig. 1.10). Epoxy is infiltrated into the bundles and they are cured under degassing conditions to extract the air bubbles in the polymer matrix. Then the composite block is incised into slices with a specified thickness in the direction vertical to the fiber direction. Finally the sliced composite sample is grounded, metalized, and polarized for transducer application.
Because the PZT fibers from sol-gel-process have bended, twisted shape and random diameters, the spacing between the fibers will be random in the composite. A static pressure can be applied vertical to the fiber direction to adjust the fiber volume fraction in the composite. Higher volume fraction and order can be obtained with larger force accompanying with higher risk of fiber cracking.

Soft-mold process was invented by the Fraunhofer IKTS, Germany [19] and is helpful for people to investigate the static and dynamic properties of 1-3 composites. This process uses a soft plastic template to fabricate 1-3 composites with a high variety of structures, rod size, shape, spacing, and arrangement. The plastic template is generated from a master mold fabricated by chemical or plasma etching, micromachining and several other methods. A positive form of the final structure is used to generate a soft mode. Later calcined piezoceramics powder is filled into the mode and fired at a suitable temperature in PbO-controlled atmosphere. After the piezoelectric structures formed, polymer matrix material is infiltrated into the void spaces and they are cured under degassing conditions to extract the air bubbles in the polymer matrix. Then

**Figure 1.10.** Process chart of 1-3 fiber composite fabrication using sol-gel-derived PZT fibers [28]
the composite block is incised into slices with a specified thickness in the direction vertical to the fiber direction. Finally the sliced composite sample is grounded, metalized, and polarized for transducer application. The process chart is shown in Fig. 1.11. Fibers as fine as 35 µm can be fabricated in this process and the composite can be used at high frequency ranging from 4 to 8 MHz.

Compared to conventional techniques, such as die-and-fill and injection molding, the soft-mold process has many advantages. The mold can be used several times to generate a lot of copies of the fiber arrays. Fibers with various shapes and sizes can be manufactured by soft-mold process. This process doesn’t need an expensive saw to cut the piezoceramics block and has no cost to maintain the saw. This process can maintain superior quality at a reasonable price per unit and has the capacity to manufacture high volumes. By changing the symmetry from square to other arrangement in the mold, the periodicity and regularity of the fibers can be removed and lateral stop band resonance modes can be suppressed or shifted to higher frequencies.

![Process Chart](image)

**Figure 1.11.** Slip casting process using reusable soft plastic molds to manufacture 1-3 composites [28]
Fibers with diameters ranging from 100 to 800µm can be manufactured by powder suspension extrusion [29] and suspension spinning [30, 31] technique. The suspension spinning technique is suitable for mass production. The fibers fabricated by this method can be arranged with regular space or not. Epoxy is infiltrated into the bundles and they are cured under degassing conditions to extract the air bubbles in the polymer matrix. Then the composite block is incised into slices with a specified thickness in the direction vertical to the fiber direction (Fig. 1.12). The composite can also be cut into any other shape or size. Finally the sliced composite sample is grounded, metalized, and polarized for transducer application. The piezoceramics fiber fabrication and arrangement, epoxy selection and the curing step are key points to acquire fiber composite with high quality and this process has been commercialized by Smart Material Corp.

**Figure 1.12.** Process chart of 1-3 fiber composite fabrication using powder-derived PZT fibers [28]

Straight fiber with homogeneous consistency is an important factor for the high quality of the fiber composite. Powder suspension extrusion and spinning process assure the high quality of PZT fibers and this process is suitable for industrial batch manufacturing. Fibers with different components, shapes and even hollow fibers have been successfully fabricated. Sintered PZT
fibers with 250µm diameter and 150mm length are shown in Figure 1.13. Technical data of typical fibers are shown in Table 1.2.

![Image](image.png)

**Figure 1.13.** Sintered PZT fibers ready for composite fabrication [28]

**Table 1.2.** Properties of piezoceramics fibers [28]

<table>
<thead>
<tr>
<th>Piezoceramics</th>
<th>Diameter (µm)</th>
<th>ε_{33}/ε₀</th>
<th>ε value (%)</th>
<th>d_{33} (pC/N)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Navy Type IV</td>
<td>300</td>
<td>2525</td>
<td>66</td>
<td>690</td>
</tr>
<tr>
<td>Navy Type II</td>
<td>250</td>
<td>1300</td>
<td>62</td>
<td>470</td>
</tr>
<tr>
<td>Navy Type II</td>
<td>140</td>
<td>1063</td>
<td>63</td>
<td>374</td>
</tr>
</tbody>
</table>

Compared to piezoceramics block, the fiber composite has decreased total performance which is caused by high surface to volume ratio of single fibers. The performance can be improved by modifying the piezoelectric material composition. The volume fraction of PZT fibers in the composite usually varies from 25% to 65%. Fiber composite with a wide frequency range from 40 kHz to 8MHz is commercially available and can be further manufactured for custom use. For example, concave surfaces can be produced by using custom molds and precision machining to fabricate a broadband sensor. The polymer can protect the fibers from being broken during the machining process.
1.3.3 Electromechanical and dielectric properties

Several technique methods have been developed to characterize the dielectric and electromechanical properties of 1-3 fiber composite. Smith and Auld [11] developed a model which can predict the dielectric and electromechanical properties with high accuracy and work as an effective design tool to direct the development of custom composite. This Smith model can also be utilized to extract unknown fiber data from measured composite data. Dynamic properties, such as vibration modes, the impedance spectrum and the electroacoustic coupling factors can be predicted by finite element analysis. All excited vibration modes, the generated sound field and the correlation to the composite structure can also be predicted by measuring surface velocity and sound fields [32]. Volume fraction of PZT fibers and their arrangement in the composite will determine the electromechanical properties of it. So the composite structure and property relation is very important for parameters prediction.

Technical parameters of the PZT fibers fabricated by sol-gel process are listed in Table 1.3. The electrical properties and the elastic coefficients of them can be calculated from the composite parameters which can be measured by electromechanical resonance experiments. Composite with thickness resonance frequency ranging from 50 kHz to 20MHz can be fabricated and used in many applications. The impedance spectroscopy together with the surface velocity of fiber composites were measured by impedance analyzer and scanning vibrometer and compared with finite element analysis modeling results [32] for directing composite design.

<table>
<thead>
<tr>
<th>Fiber composition</th>
<th>$\varepsilon_{33}/\varepsilon_0$</th>
<th>Tan $\delta$</th>
<th>$d_{33}$ (pC/N)</th>
<th>$-d_{31}$ (pC/N)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Pb $(Zr_{0.53}Ti_{0.47})O_3$</td>
<td>1170</td>
<td>0.014</td>
<td>150</td>
<td>44</td>
</tr>
<tr>
<td>PZT-PMN</td>
<td>2100</td>
<td>0.035</td>
<td>350</td>
<td>80</td>
</tr>
</tbody>
</table>

Table 1.3. Properties of PZT fibers deduced by extrapolation of measured data [28]
1.3.4 Application

Piezoelectric fiber composite is a unique and cost-efficient transducer fabrication technology. They combine the sensing and actuating properties of piezoelectric fibers and the softness properties of polymer to improve the performance of the ultrasonic transducer. These devices can have the benefits, such as high coupling coefficient, low acoustic impedance, broader bandwidth, greater sensitivity, minimized lateral mode coupling and an intermediate dielectric constant.

The fiber composite transducer can work in the frequency range from 40 kHz to 6MHz with spurious modes suppressed. The acoustic impedance can be adjusted to satisfy the needs for several applications, including nondestructive testing, biomedical diagnosis, sonar application and so on. Matching or backing layers are not needed because of their excellent impedance match with the acoustics media. This can help to save space, cost and decrease the total weight of the overall transducer. The fiber composite transducer can also be designed in special shapes to match non planar surfaces which will increase its application field. For example, a broadband transducer is required in guided wave inspections, where curved surfaces are required to be inspected without extensive scanning. The fiber composite piezoelectric transducer can satisfy the requirements and has an excellent impedance match to the test sample.

Both of the piezoelectric fiber composite and piezoelectric bulk materials have applications under certain circumstances. Both of them are needed in the ultrasound transducer industry and the fiber composite will not entirely replace the bulk materials. The fiber composite transducers are suitable to be used in the frequency domain with a resonant frequency from 4 MHz to 6 MHz. Bulk materials are suitable for the applications out of this range. Usually piezoelectric composites cost more than bulk materials but they don’t need matching and backing layers and have better performances in special applications.
1.4 PIEZORESISTIVE MATERIALS AND SENSORS

1.4.1 Piezoresistive materials

Piezoresistivity is a common electromechanical sensing method for micromachined sensors. Doped silicon has excellent piezoresistive characteristics among all piezoresistive materials [33, 34]. A number of representative piezoresistive materials will be introduced here.

Metal strain gauges are often in the form of metal-clad plastic patches which can be glued to surfaces of mechanical structures. Resistors are etched with a zigzagged path to increase the resistor length and the resistance amount in a given area. Metal strain gauges are often not made of pure metal thin films but of metal alloys for actual commercial applications. Metal strain gauges usually have the gauge factors ranging from 0.8 to 3.0. Monolithic integration processes are used to fabricate the micromachined strain gauges on mechanical beams and membranes to acquire small size. Metal strain gauges do not have large piezoresistive gauge factors but can still be applied in many situations. They don’t need doping and lengthy process steps and they can be deposited and processed under much lower temperature than that for doping semiconductors. They also can sustain a much larger elongation before fracture.

Selectively doped silicon can be used to make semiconductor strain gauges [33-35]. The relative orientation of a doped single-crystal silicon piezoresistor to crystallographic directions will influence the piezoresistive coefficients of it. Its piezoresistive coefficients will also be influenced by the doping concentration, type of dopant, and temperature of the substrate [36, 37]. Different elements of the piezoresistive coefficients matrix are affected by temperature and doping concentrations differently. The piezoresistive coefficients decrease with increasing temperature and doping concentrations for both p- and n-type silicon. For single-crystalline
silicon under certain doping concentration and dopant types, the piezoresistive coefficients have been characterized experimentally [38]. If the x-, y-, and z-axes of the crystal are not aligned to the axial directions of the coordinate, the piezoresistive coefficients matrix will change. Young’s modulus of silicon is also a function of the crystal directions. By multiplying the piezoresistive coefficient with Young’s modulus in the applied strain direction, the piezoresistive gauge factors can be acquired. The piezoresistive sensitivity is not exactly a constant.

A successful silicon piezoresistors design will have an appreciable resistance value, a maximum gauge factor, and minimum temperature effects. The doping concentration will affect all of these three performance parameters. For piezoresistors made of doped silicon, the gauge factor and the temperature coefficient of resistance are both functions of the doping concentration. Appropriate doping concentrations must be carefully selected for silicon piezoresistors designs.

Polysilicon which can be deposited on a wide range of substrates offers a number of advantages over single-crystalline silicon for MEMS piezoresistors [39]. The gauge factor of polycrystalline silicon is much smaller than that of single crystalline. But it does not depend on the orientation of the resistor in the substrate plane. The gauge factors for n- and p-type polycrystalline silicon substrates are strongly influenced by the doping concentration and will reach peak magnitude at particular concentrations.

1.4.2 Piezoresistive sensors

Piezoresistive materials have been used for many kinds of sensor applications in these years. A few examples will be discussed here. These examples illustrate the unique device designs, fabrication processes, and achievable specific performances. A proof mass will experience an
inertial force under an applied acceleration, which introduces stress and strain to the mechanical support elements connected to the proof mass. The acceleration value can be acquired by measuring the magnitude of the stress. This is the basic principle of piezoresistive accelerometers. Tactile sensors are used to characterize surface profiles and morphology and to measure contact forces. High integrated tactile sensors can be manufactured by micromachined fabrication process. Micro piezoresistors can also be used for flow sensing applications. Their small physical sizes can minimize the impact on the flow field under test. Fluid flow around a microstructure can generate a lifting force [40, 41], a drag force [42], or momentum transfer on a floating element [43, 44]. These forces will deform the microstructure; change the stress in the floating element or the structures supporting it. By measuring the resistance of the piezoresistors located on these structures, the bending of the structures and the fluid parameters can be predicted.

The pressure sensor was the earliest demonstration fabricated by micromachining technology. The fabrication technology for pressure sensors advances quickly. Both bulk and surface micromachining can be used in the fabrication process. Bulk microfabricated pressure sensors are still the dominated products today. They incorporate thin deformable diaphragms which are made of single crystal silicon. Bulk silicon micromachining steps are used to make the diaphragm with embedded piezoresistors. Selectively doping the silicon diaphragm is used to make the piezoresistors. Piezoresistors are located in the center of four edges where the maximum tensile stress occurs during the bending of the diaphragm. A uniformly applied pressure difference across the diaphragm was utilized to bend the diaphragm.
2.0 RESEARCH OBJECTIVE

As discussed in chapter 1, piezoelectric fiber composite has been proven to be a powerful tool for transducer applications in wide areas with excellent characters, such as high coupling coefficient, low acoustic impedance, broader bandwidth, greater sensitivity, minimized lateral mode coupling and an intermediate dielectric constant. Hence, my PhD research work will focus on this topic and will include two parts, one objective is to fabricate and characterize ZnO nanowires-polymer nanocomposite and experimentally investigate the piezoelectric and piezoresistive properties of this novel nanocomposite; the other objective is to use theoretical modeling and experiment validation to investigate PZT fiber composite and develop their physical and medical applications.

Therefore, the overall objective of this dissertation is on the modeling and experimental study of fiber composite sensor, which has three specific aims:

- ZnO nanowires-polymer nanocomposite piezoelectric and piezoresistive properties investigation
- PZT fiber composite sensor for vibration and strain sensing
- PZT fiber composite sensor for medical applications
3.0 MULTIFUNCTIONAL ZNO NANOWIRES-POLYMER NANOCOMPOSITE AND ITS APPLICATION

3.1 INTRODUCTION

Nanowires and nanotubes may become the basic building blocks for nanoscale electronic, optical and biological systems, since they can function as miniaturized devices as well as electrical interconnects [45]. With some unique optoelectronic, electrical, piezoelectric and photochemical properties, ZnO nanowires have been extensively investigated in the past few years for use in UV lighting-emitting devices [46, 47], gas sensor [48], solar cells [49], and field emitter [50]. Meanwhile, polymer nanocomposites with nanomaterials dispersed in polymer matrix have been studied to develop materials with improved electrical and mechanical properties [51, 52].

It is expected that nanocomposites that make use of the intrinsic properties of the ZnO crystal, the scaling properties of ZnO nanowires, and the induced electric polarization of the dielectric polymeric phase will open a novel route to design and fabricate multifunctional electroactive polymer composite with micro-tailorable properties that single component material cannot achieve. So far, polymer-based dielectrics with a high dielectric constant (high K) have been studied for capacitor and charge-storage device applications [53-56]. Many high-K ceramic fillers are used as additives to improve the K of polymers. Percolative composite capacitors are fabricated by using conductive fillers as another strategy to improve the K [56, 57]. Core/shell
hybrid particles with metal Ag cores coated by organic dielectric shells are also used as additives [58], which can keep a stable high-K, but rather low dielectric loss (\(\tan \delta\)) of the polymer dielectrics. Polymer-based nanocomposites are becoming an attractive set of organic-inorganic materials due to their multifunctionality and many potential applications.

In this work, ZnO nanowires are added into polyimide matrix to form polymer matrix composites, in which the ZnO nanowires are tailored by electric field assisted alignment by using in-plane interdigital transducer (IDT) electrodes to achieve anisotropic properties. The degree of nanowires’ distribution in a dielectric polymer matrix, the orientation of nanowires and the binding between nanowires and polymer matrix, will determine the properties of the composite materials. ZnO single crystal nanowires are usually with hexagonal cross-section and the crystalline c-axis (polarization axis) is along the length direction of the nanowires. Strong piezoelectric and pyroelectric properties are observed along the c-axis of the ZnO with wurtzite structure. Thus alignment of nanowires along the length direction in the nanocomposites is of importance to explore the materials multi-functionality. Electric and material properties of this novel nanocomposite have been characterized with related instruments. High dielectric constant is acquired by experiment and the percolation threshold of the nanocomposite is about 15% ZnO nanowire weight ratio in the nanocomposite. The nanocomposites, with tailorable microscale morphology and high dielectric constant, will be found use in smart materials and structures as electromechanical sensors and actuators, as well as for charge-storage devices and other electronic applications. The piezoresistive property of this nanocomposite without electric field alignment was also investigated for strain sensor application. Large gauge factor caused by semiconductor property of ZnO nanowires was obtained and high flexibility of the nanocomposite sensor made it easy to be attached to any curved structures for strain
measurement. This novel nanocomposite piezoresistive strain sensor with high gauge factor is expected to be widely applied to various occasions, including industrial, civil, medical, and aerospace domains.

3.2 FABRICATION AND ELECTRIC PROPERTIES OF ANISOTROPIC ZNO NANOWIRES-POLYIMIDE NANOCOMPOSITE

3.2.1 Fabrication and characterization

ZnO nanowires were synthesized according to a two-step hydrothermal method [59]. The substrate with ZnO nanowires was characterized under a scanning electron microscope (SEM) to image the surface topography, composition of it, diameter and length of nanowires. The top SEM image of the substrate is shown in Fig. 3.1. To complete this procedure, the substrate with ZnO nanowires array was sonicated in ethanol for 4 hours to break down the ZnO nanowires from the substrate. The ZnO nanowires-ethanol solution was heated to 120°C and held at this temperature for one hour to evaporate the ethanol. SEM image of broken ZnO nanowires is shown in Fig. 3.2. The average length of the ZnO nanowires is nearly 10 μm.

Figure 3.1. Top SEM images of ZnO nanowires on the substrate grown by hydrothermal method
The ZnO nanowires were collected and then dispersed into thinner T9039 for the non-photosensitive pyralin polyimide PI2611 (HD MicroSystems, Parlin, New Jersey). The ZnO nanowires-thinner mixture were sonicated for one hour and whisked for four hours. Then pure polyimide was added into the mixture with weight ratio 1:4 to the thinner. The ZnO nanowires-polyimide mixture was then whisked for another four hours. The liquid nanocomposite was spin-coated onto a glass substrate with IDT electrodes. Gold was deposited onto the substrate to fabricate the IDT electrodes. The IDT has sixty pairs of fingers with 6 mm length, 100 nm thickness, 25 μm width and 50 μm distance between adjacent fingers.

Electric field is employed to tailor the structure of ZnO nanowires-polymer nanocomposites. The direction of the externally applied electric field defines the anisotropy of the resulting composites. Superimposed alternating current (a.c.) and direct current (d.c.) electric field can be used to assemble, re-arrange, and orient the inclusions (ZnO nanowires) whose electric properties differ from those of the polymer matrix. The alignment degree of ZnO nanowires in polymer matrix depends on the controlling parameters such as the amplitude of d.c., the amplitude and frequency of a.c., and duration of the electric field applied to the sample. It also depends on the weight ratio of ZnO nanowires to polyimide, the size of ZnO nanowires, the thickness of the nanocomposite and the configuration parameters of the IDT electrodes.
Superimposed a.c. and d.c. electric field is generated by a function generator (Stanford Research, model DS345) and augmented by a power amplifier (PCB Piezotronics Inc., 790 series). The alignment of the ZnO nanowires in the polymer matrix is caused by the force induced by electric field. An inclusion (nanowire) whose dielectric constant $\varepsilon_n$ exceeds the dielectric constant of the polymer matrix $\varepsilon_p$ (i.e., $\varepsilon_n > \varepsilon_p$) moves towards the stronger electric field region. This phenomena will happen with ZnO nanowires dispersed in a liquid polymer since the dielectric constant of ZnO is (about 8.5) larger than the polymeric matrix. Different a.c. voltage/frequency and d.c. voltage have been applied to examine the alignment and distribution of ZnO nanowires in the polymer matrix. The application of an a.c. electric field will cause local oscillation of the ZnO nanowires in the dielectric liquid. As the amplitude of a.c. voltage increases, ZnO nanowires will oscillate stronger. The superimposed d.c. electric field will align ZnO nanowires parallel to the electric field direction. In the experimental study, it was found that a 30V (pp) a.c. voltage with frequency of 1000Hz superimposed with 1V d.c. voltage resulted in a well aligned ZnO nanowires in the polymer matrix without segregation on the electrode surfaces.

After the electric field was applied for ten minutes, the sample was heated to 120°C on a hot plate and held for ten minutes at that temperature for soft-baking and afterwards heated to 350°C in a furnace (Barnstead 47900) and held for 30 minutes at that temperature for curing. The annealing and polymerization will then take place leading to solid nanocomposites; and the rise in viscosity works to stabilize the dispersion and alignment of the ZnO nanowires. If the spin speed was set to 2000 rpm, a 2.2 μm thick nanocomposite thin film was formed after curing which was measured by a profilometer. The polyimide polymers thus formed will be amorphous, and have dipolar functionality. Fig. 3.3 is a schematic of ZnO nanowires aligned by the
superimposed a.c. and d.c. fields. Typical images taken by a microscope of the ZnO nanowires-polyimide nanocomposite before and after alignment are shown in Fig. 3.4. The nanowires are dispersed in the polyimide matrix homogeneously before electric field alignment. Clearly, the dispersed ZnO nanowires can be micro-tailored by electrical fields for desirable distribution and alignment in the polymer matrix for the fabrication of anisotropic nanocomposites.

Figure 3.3. Schematic of ZnO nanowires alignment by superimposed a.c. and d.c. fields

Figure 3.4. Optical images of ZnO nanowires before (isotropic) and after (anisotropic) alignment

The surface morphology of the ZnO nanowires-polyimide nanocomposite was characterized by a scanning probe microscope (SPM) (Veeco, Dimension V). Fig. 3.5a shows the
surface morphology of pure polyimide. Fig. 3.5b and Fig. 3.5c show the surface morphology of the nanocomposite with 10% and 20% weight ratios of ZnO nanowires. As nanowires are added into the liquid polyimide, the surface of the nanocomposite sample will become coarse. But if more and more nanowires are added, the surface of the sample will change back to be flat with a larger sample thickness compared to pure polyimide sample.

**Figure 3.5.** SPM images of (a) pure polyimide and ZnO nanowires-polyimide nanocomposite with (b) 10% (c) 20% weight ratios of ZnO nanowires
3.2.2 Hysteresis phenomena

The electric field assisted alignment of ZnO nanowires in the polymer matrix should lead to net polarization for the nanocomposites. The polarization-electric field (P-E) hysteresis of the nanocomposite sample is recorded using a ferroelectric test system (Radiant Technologies, Albuquerque, NM) to understand the alignment process. Different weight ratios of ZnO nanowires to polyimide are used in the experimental studies. In order to describe the hysteresis phenomenon, a half period of the P-E loop was recorded while an a.c. voltage with 10V, 0.1Hz was applied to the sample. A P-E loop for pure polyimide was also recorded for comparison purpose. A small net polarization was observed when the voltage changed back to 0 after a half period cycle due to the dipolar functionality of the polyimide. As more ZnO nanowires were added into polyimide, the net polarization clearly increased. The net polarization changes from 0.0008uC/cm$^2$ to 0.0058uC/cm$^2$ when the weight ratio of ZnO nanowires increases from 5% to 15% as shown in Fig. 3.6. With weight ratio of ZnO nanowires further increasing to 30%, the net polarization decreases. All the samples were tested after curing. With too many ZnO nanowires added into the polymer matrix, the nanowires intend to segregate and cross-contact each other, the alignment under electric field will be less effective. If voltage sweeps for a full period, it is found that the resulting full P-E loop is not closed, which can be attributed to the remnant charge trapped at electrode interface [60]. The P-E loops observed are not symmetric about y-axis, which can be attributed to the inability of the nanowires rotating freely in viscous polymer fluid when the polarity of electric field changes.

The samples after curing were also tested under different electric field amplitudes and frequencies. The voltage amplitude was changed from 5V to 25V with 5V intervals using six sweep frequencies, 0.1Hz, 1Hz, 10Hz, 100Hz, 1kHz, and 10kHz. The net polarization increases
nonlinearly with a.c. voltage at low frequency (<10Hz). The P-E loop of ZnO nanocomposite is similar to ferroelectric P-E loop at 1Hz and 0.1 Hz. In addition, the superimposed d.c. voltage doesn’t affect the polarization much. Further studies are needed to understand better the interaction of ZnO nanowires with polyimide matrix under electric field and the alignment dynamics.

![Figure 3.6](image)

Figure 3.6. P-E loops for pure polyimide and nanocomposite with different weight ratios of ZnO nanowires

### 3.2.3 Electric properties

The room temperature I-V characteristic curve of the nanocomposite was measured by a high current source measure unit (Keithley Instrument Inc.) to scale the resistance. The I-V curves for pure polyimide and nanocomposite with low weight ratios (≤10%) of ZnO nanowires were plotted in Fig. 3.7a and those with high weight ratios (≥15%) of ZnO nanowires were plotted in Fig. 3.7b. The horizontal line in Fig. 3.7a is the I-V curve for polyimide which shows that pure polyimide thin film is insulator. When inclusions of ZnO nanowires were added into the polyimide, the current would appear at a specific voltage. The ZnO nanowires are dispersed in the polyimide matrix and the nanocomposite overall shows semiconductor property with low
weight ratios of ZnO nanowires (Fig. 3.7a). The current changes from 16.5 μA to 860 μA with 6 V applied to the sample when the ZnO nanowires weight ratio changes from 10% to 20% in the nanocomposite (Fig. 3.7b). As more ZnO nanowires were added into the polyimide matrix, the conductivity of the nanocomposite sample was significantly increased compared to the nanocomposite with low weight ratios of ZnO nanowires. The nanocomposite changes from semiconductor to conductor.

**Figure 3.7.** I-V curves for the nanocomposite with (a) low (b) high weight ratios of ZnO nanowires

Electrical impedance spectroscopy (EIS) is often used to characterize the dielectric and electrical properties of a material or a device [61]. EIS is a measurement of equivalent electrical impedance of a device under test (DUT) by applying a small AC current excitation signal to the device and measuring the voltage drop across the DUT over a range of frequencies, which will produce the frequency spectra of the resistive and reactive components of the equivalent electrical impedance of the DUT. The impedance spectra provide some important structure-property relationships of the device or material for guiding the materials design and processing.
for device applications. EIS can also be used to establish common equivalent circuit models of the sample. The model parameters can be extracted from the complex impedance values. The equivalent circuit models and model parameters together are useful in the sample analysis and modification.

Data obtained from EIS are usually expressed graphically in a complex impedance plot or Cole-Cole plot [62]. In a complex impedance plot, the impedance is plotted as a function of the log frequency on the X-axis, showing the absolute values of both the resistance and the reactance on the Y-axis. If the resistance value is plotted on the X-axis and the negative reactance value is plotted on the Y-axis of a chart, a Cole-Cole plot is generated. Low frequency data are on the right side and high frequency data are on the left side of the chart for an ordinary Cole-Cole plot. EIS measurement for the ZnO nanocomposites was performed by using an impedance analyzer (Agilent 4294A). The Cole-Cole plot for the nanocomposites with 15%, 20% and 30% weight ratios of ZnO nanowires was shown in Fig. 3.8.

![Cole-Cole plot for the nanocomposites with different weight ratios of ZnO nanowires](image)

**Figure 3.8.** Cole-Cole plot for the nanocomposites with different weight ratios of ZnO nanowires

From the Cole-Cole plot of EIS, many useful data can be obtained. The maximum $ReZ$ value ($ReZ$ at the lowest frequency, or dc resistance) represents the summation of the series
resistance and the parallel resistance to the capacitance, which changes with the content of ZnO nanowires in the nanocomposites. Clearly, the series resistance, which is the minimum ReZ values of the semicircles, is negligible for the nanocomposites, indicating the electrodes and the nanocomposites have a negligible contact resistance. At the maximum ImZ point of the semicircle, $\omega \tau = \omega RC = 1$, C is the equivalent capacitance and $\tau$ is the time constant of the material.

The nanocomposite with low weight ratio of ZnO nanowires has a much larger d.c. resistance (100 times higher) than that with high weight ratio of ZnO nanowires. So the magnitude of the impedance and the dependence of impedance on frequency are both functions of sample composition.

An equivalent circuit model can be established from the dependence of impedance on frequency in EIS [63]. The types of electrical components in the model and their interconnections control the shape of the impedance spectrum of the model. The equivalent circuit parameters which control the size of each feature in the spectrum can be extracted from the EIS data. Both these factors affect the degree to which the impedance spectrum of the model matches a measured EIS. EIS data are generally analyzed in terms of an equivalent circuit model. The equivalent circuit model for the nanocomposite sample is shown in Fig. 3.9. The effective d.c. resistance and capacitance at 1000 Hz for the nanocomposite with 10% weight ratio of ZnO nanowires are 3 MΩ and 145 pF. And these electrical parameters for the nanocomposite with 20% weight ratio of ZnO nanowires are 25 kΩ and 1.21 μF.

![Figure 3.9. The equivalent circuit for the ZnO nanowires-polyimide nanocomposite](image)
With the dimensional parameters of the sample and the resistance and reactance values from EIS, the conductivity and dielectric constant of the nanocomposite can be calculated. These parameters change with weight ratios of ZnO nanowires are plotted in Fig. 3.10. In case the ZnO nanowires weight ratio exceeds 10%, the conductivity and dielectric constant of the nanocomposite sample increase quickly. A significant enhancement of conductivity has been found in nanocomposite with high ZnO nanowires concentration (15%). The percolation limit of the nanocomposite is about 15% ZnO nanowire weight ratio in the nanocomposite. Large piezoresistive effect is expected for the nanocomposite with this concentration. Piezoresistive properties of ZnO nanocomposite with other concentrations will also be investigated for comparison with the result from the composite with concentration near percolation.

Figure 3.10. The nanocomposite conductivity and dielectric constant versus ZnO nanowires weight ratios
3.3 ZNO NANOWIRES-POLYIMIDE NANOCOMPOSITE PIEZORESISTIVE STRAIN SENSOR

3.3.1 Strain measurement methods

Polymer-based nanocomposites are becoming an attractive set of organic-inorganic materials. Due to their structural flexibility, easiness in processing, and possibility of combining multifunctionality, polymer matrix nanocomposites with improved sensing and actuation capability are highly desirable for many smart materials and structure applications [51, 52]. Such examples include piezoresistive sensors and piezoelectric transducers used for structural health monitoring and vibration control in numerous industrial, civil, medical and aerospace fields. Real time monitoring of mechanical strain/stress variation is needed to ensure the reliability of the structures in these applications. The incorporation of functional nanocomposite and devices into the mechanical structures becomes a natural approach, in which the electrical property of the nanocomposite device changes with the stress/strain condition, providing the transduction mechanism to characterize the structural response to the loading situation. Conventionally, strain (or displacement) response in a mechanical structure can be characterized by various techniques, which can be grouped into two categories: the noncontact methods and contact methods [64].

In the case that noncontact methods such as the laser strain micrometry are used, two laser beams are needed to focus on the opposite faces of the sample for the out-of-plane strain measurement. Furthermore, the laser beam should be reflected at the ends of the structure or sample in characterizing the transverse strain response of them. The major benefit for this method is its non-contact nature. The measurement results of the laser are very accurate based on the requirements that the laser beam is aligned properly and the measured surface of the sample
can reflect enough light. However, a laser instrument is usually too bulky to be easily carried on and the technique is so delicate that laboratory conditions are required for its use. Furthermore, flexural vibration mode in the structure may be excited in the strain measurement for thin and soft sample, which will cause errors to the final result [65]. An optical microscope is another noncontact instrument which can only characterize the strain response at low strain response region for its limited resolution [66].

The contact methods such as a differential capacitive sensor or a linear variable differential transformer (LVDT) have been developed for strain/displacement measurement. These two techniques measure either the output voltage of two differential parallel plate capacitors or that of two differential transformers to reflect the structure displacement change. But complex circuit requirements and sensitivity to vibration keep these two methods from being very practical for strain measurement. In the situation that a strain gauge is used and it will not affect the original structure, the strain of the structure can be acquired by measuring the electric voltage change in the strain gauge with external stress exerted on the structure. Piezoresistive and piezoelectric materials are commonly used for strain sensors and vibration sensors. Several piezoresistive materials, such as metal film, single-crystal silicon and polycrystalline silicon, have been widely used to characterize static or dynamic strain variations in mechanical or civil structures [67]. A piezoresistive material is usually sandwiched between two insulation layers to fabricate a strain sensor. Adhesives are used to attach the strain sensor to the host structure prior to measurement. This method is very simple for large structures but may not be suitable for small ones. The size of the strain sensor and even the thickness of the adhesives can influence the behavior of small structures under test. So small strain sensors are expected to minimize their effects to the structure, yet still provide high sensing resolution.
Microelectromechanical systems (MEMS) fabrication techniques can be used to build small sensors with high accuracy. The piezoresistive property of silicon and other semiconductor thin films has been employed for the design and fabrication of microsensors to measure strain induced by vibration in small structures, with applications as accelerometers and resonators [68]. Recent great progress in nanomaterials and nanotechnologies has indicated that nanowires and nanotubes may become the basic building blocks for nanoscale electronic, optical and biological systems, since they can function as miniaturized devices as well as electrical interconnects [45]. A giant piezoresistive effect has been observed in silicon nanowires [69]. Piezoresistive properties of both crystalline and polycrystalline silicon nanowires which are developed using a top-down approach have been investigated [70]. The superior electrical properties of carbon nanowires and carbon nanotube composite have also been utilized for novel strain sensors development [71-73]. The piezoresistive property of ZnO nanowires-polyimide nanocomposite without electric field alignment was investigated for strain sensor application.

3.3.2 The gauge factor of the strain sensor

The material electrical resistance changes with the external mechanical stress or strain is the piezoresistive effect. The sensitivity of a piezoresistive strain sensor or strain gauge is referred as the gauge factor $G$, which is defined as the resistance change percentage per unit strain [74],

$$ G = \frac{\Delta R}{R} \frac{1}{\varepsilon} \quad (3.1) $$

The resistance change percentage can be derived by taking the derivative of the resistance expression $R = \rho l / A$, 

44
\[
\frac{\Delta R}{R} = \frac{\Delta \rho}{\rho} + \left( \frac{\Delta l}{l} - \frac{\Delta A}{A} \right)
\]  
(3.2)

where \(l\), \(A\), and \(\rho\) are the strain gauge length, cross-section area and resistivity, respectively.

The cross-section area change percentage can be written as

\[
\frac{\Delta A}{A} = (1 - \nu)^2 - 1
\]

(3.3)

where \(\nu\) is the Poisson’s ratio of the substrate material. Because the strain varies in a small range, a linear approximation can be applied to this equation,

\[
\frac{\Delta A}{A} = -2\nu
\]

(3.4)

and the resistance change percentage can be expressed as

\[
\frac{\Delta R}{R} = (1 + 2\nu) \frac{\Delta l}{l} + \frac{\Delta \rho}{\rho}
\]

(3.5)

So the gauge factor from the definition can be acquired

\[G = (1 + 2\nu) + \gamma_i\]

(3.6)

where \(\gamma_i\) is the longitude piezoresistive coefficient.

Wheatstone bridge circuits are usually utilized for the resistance change measurement and several variations of Wheatstone bridge circuits have been developed for applications under different circumstances. Four resistors connected in a loop form a basic bridge configuration. An input voltage is applied across two junctions with two resistors connecting them. The output is the voltage difference across the other two junctions. One or more resistors in the bridge loop may work as the strain sensing resistors, whose resistances will change with the external variables [67]. If only one resistor is used as variable, the other resistors can be located in special regions without any strain. One of the configurations with only one piezoresistor implemented into the Wheatstone bridge circuit was shown in Fig. 3.11. When the sensor resistance changes
with external force due to piezoresistive effect, the voltage between the voltage divider will also change with it. If this voltage change is compared with the original value, the resistance change and the amount of strain can be calculated [64].

![Wheatstone Bridge Circuit](image)

**Figure 3.11.** One type of Wheatstone bridge circuit for resistance measurement

The output voltage can be related to the input voltage by the following equation [67],

\[
V_{\text{out}} = \left( \frac{R_2}{R_1 + R_2} - \frac{R_3}{R_3 + R_4} \right) V_{\text{in}}
\] (3.7)

All four resistors have the same resistance value \( R \) in many practical applications and the resistance of the variable resistor (strain sensor) can be represented as

\[
R' = R + \Delta R
\] (3.8)

So the output voltage and the input voltage have the following linear relation,

\[
V_{\text{out}} = \left( -\frac{\Delta R}{2R + \Delta R} \right) V_{\text{in}}
\] (3.9)

Most piezoresistors are sensitive to temperature variations and the Wheatstone bridge circuit is an effective way to eliminate the temperature related resistance change. For all resistors in the bridge will change resistance at the same ratio with the environmental temperature, the temperature effects from every part will cancel each other.

If the strain sensor is used for the cantilever beam strain measurement, the strain sensor will be bonded onto the clamped end of the cantilever beam. A static force can be applied at the
free end of the cantilever beam for strain generation. The dynamic strain in the cantilever beam can also be inspected by applying an impulse or a sinusoidal force to the free end of the cantilever beam to generate an excited vibration of it. Both of these two methods are based on cantilever beam theory. When a force is applied to the free end of a cantilever beam, the tip vertical deflection $z$ can be calculated from [64],

$$ z = \frac{L_2^3}{3EI} F $$  \hspace{1cm} (3.10)

where $F$, $E$, $I$ and $L_2$ are the applied force, Young’s modulus of the beam, second moment of area for beam cross-section, effective beam length, respectively. The strain $\varepsilon$ in the beam is calculated by the following equation,

$$ \varepsilon = \frac{FL_1t}{2EI} $$  \hspace{1cm} (3.11)

where $t$ and $L_1$ are the beam thickness and the distance from the tip to the strain gauge location, respectively. So the strain-tip vertical deflection relation can be acquired,

$$ \varepsilon = \frac{3L_1tz}{2L_2} $$  \hspace{1cm} (3.12)

The strain $\varepsilon$ keeps a linear relation with the tip vertical deflection $z$.

3.3.3 Experimental study

The strain for the piezoresistive property measurement was generated by monotonic uniaxial stress-strain tests. The experiment setup for measuring the gauge factor G of the nanocomposite piezoresistive strain sensor was shown in Fig. 3.12. The polyimide substrates for spin coating the nanocomposites were cut to long strips to obtain samples with high aspect ratio for minimizing
Poisson’s effect during testing. The strips were also cut with smooth edges to prevent pre-mature failure caused by stress concentrations or crack initiation and propagation [75]. A stress/strain apparatus (PASCO AP-8214) was used to stretch the nanocomposite sample together with the resistance change of the sample being measured by the Wheatstone bridge circuits. After calibrating the force sensor with a calibration bar, the nanocomposite sample was mounted on the sample clamps by a tee handle with socket and the lever arm was placed in the starting position. The data from the force sensor was transferred by a ScienceWorkshop 750 USB data acquisition interface (CI-7599) to a computer and recorded by DataStudio software. The crank was turned clockwise very slowly and the software was started to record the data just before the lever arm came into contact with the force sensor. The software was stopped after finishing collecting data. The input voltage to the Wheatstone bridge circuits was generated by a current/voltage source measure unit (Keithley 238). The output voltage from the bridge was transferred to the computer by a GPIB controller (National Instrument) and recorded by a short LabVIEW program simultaneously.

![Image](image_url)

**Figure 3.12.** The stress/strain apparatus with the nanocomposite sample mounted on it

If the strain sensor is used for the cantilever beam strain measurement, it will be bonded onto the clamped end of the cantilever beam as shown in Fig. 3.13. The experimental setup for
the strain measurement was shown in Fig. 3.14. For static strain measurement, an aluminum cantilever beam with a 25.4 cm effective length, a 0.49 cm thickness was used in the experiment and the distance from the tip to the strain sensor location was 24.1 cm. A manual micro-positioning meter mounted near the cantilever tip was used in the test setup as shown in Fig. 3.15. The micro-positioning meter was adjusted to induce the deflection which can be read out directly. The strain sensor was then wired accordingly to a proper bridge configuration and balanced when no load was applied to it. The micro-positioning meter was then turned until it just touched the cantilever surface. This point was used as the zero point of the deflection. The micro-positioning meter was then turned again and the output voltage in the circuit for calculating the resistance change was recorded.

![Figure 3.13. Schematic of the strain sensor bonded on the cantilever beam](image)

![Figure 3.14. The block diagram for using the nanocomposite strain sensor for cantilever beam strain measurement](image)
For dynamic strain measurement, the strain was measured by this sensor and compared with the result calculated from the cantilever tip deflection, which was measured by using a Fotonic sensor system (MTI-2000) as shown in Fig. 3.16. An aluminum cantilever beam with a 55 mm effective length, a 0.5 mm thickness was mounted on a LDS shaker (model V203). The distance from the cantilever tip to the strain sensor was 48 mm. A 2.3 g steel mass was glued at the free end of the beam to increase the vibration amplitude and strain. A sinusoidal signal was generated by a lock-in amplifier (model SR850) and amplified by a LDS power amplifier (PA25E) to drive the shaker in the vertical (z-axis) direction. The input voltage to the Wheatstone bridge circuits was generated by a current/voltage source measure unit (Keithley 238). The peak to peak output voltage from the bridge was measured by the lock-in amplifier. The peak to peak vertical displacement of the cantilever tip was measured by the Fotonic sensor system.
3.3.4 Results and discussion

In the monotonic uniaxial piezoresistive property measurement experiment, the resistance change versus strain curves for the nanocomposites with different weight ratios of ZnO nanowires were shown in Fig. 3.17. As all the other semiconductor strain gauges, this nanocomposite strain sensor has nonlinear resistance change versus strain relation. That is to say, its gauge factor is not a constant as the strain changes. For example, the gauge factor is 11.2 under 4‰ strain and it is 102 under 4% strain for the nanocomposite sample with 15% weight ratio of ZnO nanowires. A curve or a table of values of gauge factor versus resistance should be presented with this nanocomposite strain sensor in application. The force versus strain curve for the nanocomposite with 15% weight ratio of ZnO nanowires was shown in Fig. 3.18. The gauge factors for the samples with different weight ratios of ZnO nanowires under 4‰ strain (usual strain range) were compared and shown in Fig. 3.19. The gauge factors for the samples with different weight ratios of ZnO nanowires with 4% strain were compared and shown in Fig. 3.20. The resistance had no obvious change for the pure polyimide sample and the gauge factor of it was thought as zero. The nanocomposites with 15% and 20% weight ratios of ZnO nanowires have much larger gauge factors than other compositions which prove that strong piezoresistive effect exists in the nanocomposite with the concentration near percolation.
Figure 3.17. The resistance change versus strain curves for the nanocomposites with different weight ratios of ZnO nanowires.

Figure 3.18. The force versus strain curve for the nanocomposite with 15% weight ratio of ZnO nanowires.

Figure 3.19. The gauge factors for the nanocomposites with different compositions under 4‰ strain.
In the cantilever beam static strain measurement application, a 3.95% resistance change was generated accompanying with a 20mm vertical deflection and the gauge factor is about 10.96 with this resistance change. The strain was 0.36% from the experiment and had 5% errors compared to the 0.342% strain from calculation. In the cantilever beam dynamic strain measurement application, a 6μ strain was acquired by calculation with the resistance change from experiment and the gauge factor from chart. The strain was 5.2u by calculation with the peak to peak cantilever tip vertical displacement measured by the Fotonic sensor. The strain measured from the two ways has 13.4% difference which proves that the nanocomposite strain sensor is a suitable instrument for the dynamic strain measurement.

### 3.4 CONCLUSION

Single crystal ZnO nanowires were synthesized through a simple hydrothermal route and subsequently mixed with polyimide matrix to form ZnO nanowires-polyimide nanocomposite which was then spin coated on glass substrate to form nanocomposite thin film. Anisotropic ZnO nanowires-polymer nanocomposite is fabricated by a field assisted alignment technique to
achieve nanocomposites with tailorable microstructure, net polarization, and improved dielectric constant. The enhancement of the dielectric constant can be attributed to the interface polarization formed by nanowires and the dielectric polymer layer. The conductivity, dielectric constant and electrical I-V curve of the nanocomposite change with weight ratios of ZnO nanowires were characterized, plotted and analyzed. The percolation limit of the nanocomposite is nearly 15% ZnO nanowire weight ratio in the nanocomposite. This novel nanocomposite will be found use in smart materials and structures as electromechanical sensors and actuators. A novel ZnO nanowires-polyimide nanocomposite piezoresistive strain sensor was fabricated and characterized based on the piezoresistive property of ZnO nanowires. Static piezoresistive effect of the nanocomposites with different weight ratios of ZnO nanowires was investigated by using a stress/strain apparatus for strain generation and Wheatstone bridge circuits for resistance change measurement. Large gauge factor was acquired for the nanocomposite with concentration near percolation. Static strain measurement was carried out with this strain sensor on a cantilever beam and the calculation and experiment were compatible within the error range. Dynamic strain measurement in a cantilever beam was also carried out with this strain sensor and the data was verified with the result from laser measurement. This novel nanocomposite piezoresistive strain sensor with high gauge factor and flexibility is expected to be widely applied to various occasions, including industrial, civil, medical and aerospace domains.
4.0 PZT FIBER COMPOSITE SENSOR FOR VIBRATION AND STRAIN SENSING

4.1 LOW FREQUENCY VIBRATION SENSOR

4.1.1 Introduction

Microsensors, microactuators, as well as microsystems integrating both micromechanical and microelectronic devices have great development and various applications [76-78]. Micro-electromechanical-systems (MEMS) have been put a great deal of emphasis in recent years on detecting mechanical vibration [79-81]. Electrostatic, electromagnetic, and piezoelectric are commonly used methods in MEMS to sense vibration and convert mechanical vibration into electric energy [82]. Piezoelectric system has a simple structure and high energy conversion efficiency in all of these ways [82-84]. Piezoelectric sensors and actuators have been widely applied to structural health monitoring and vibration control applications [85]. They usually have a bimorph or unimorph cantilever structure with a bulk mass attached to the end of the cantilever beam [86]. The vibration generated from the shaker inspires the cantilever beam which stretches and compresses the piezoelectric materials and generates charge by piezoelectric effect. The strain-dependent charge generated from mechanical excitation has been utilized for sensing vibration [87-90]. The voltage and power output, accompanying with the fluctuation amplitude of the
cantilever beam, arrive at a maximum at resonant frequency. The sensitivity of the vibration sensor has direct relation with the configuration of the cantilever beam [91].

Bulk PZT ceramic is commonly used for sensors due to its high piezoelectric coefficient and wide bandwidth. But many disadvantages are also accompanied with it, such as high dielectric constant, low elastic compliance and so on. The high dielectric constant of bulk PZT reduces the electromechanical coupling coefficient of it and converts less electric energy from mechanical vibration compared to piezoelectric materials with low dielectric constant. The low elastic compliance of bulk PZT makes it too hard to be easily attached to any curved surfaces and make the system have much higher resonance frequency compared to ordinary environmental vibration frequency which is not suitable for low frequency vibration detection. And the bulk PZT is very brittle and unable to withstand large vibration amplitude or shock to the cantilever beam.

Two alternative methods have been developed to overcome these disadvantages [92]. One uses thin film deposition of PZT on the substrate [93] and the other uses packaged PZT composites. PZT thin film needs complex technical processes to be integrated on the substrate and has low charge output. A piezoelectric composite sensor or actuator comprises of one piezoelectric material layer sandwiched between two soft thin encapsulating layers. 1-3 piezoelectric composites which are most commonly used are composed of piezoelectric ceramic rods embedded in a non-piezoelectric matrix. PZT fiber composites can decouple the lateral effect applied to the sensor synchronously and a large sensitivity can be obtained from the sensor [11]. They also have the benefits such as lower dielectric constant, improved elastic compliance and improved electromechanical coupling coefficient and are suitable for vibration detection and
sensor application. Both $d_{31}$ and $d_{33}$ MFCs transducers have been developed and are currently produced by Smart Material (Dresden, Germany).

In this study, a fiber composite unimorph was fabricated and experimentally studied for low frequency vibration signal detection. Firstly, the constitutive relation for the 1-3 PZT fiber composite on interdigitated transducer (IDT) electrodes was derived under several mechanical and electric assumptions. And a new physical model was proposed to calculate the material parameters of the fiber composite and validated with mixing rule. Then, the properties of single PZT fiber and epoxy were substituted into this model to acquire the fiber composites' global properties. And the global parameters of the fiber composites were substituted into lumped and distributed parameters’ constituent equations for piezoelectric unimorph to acquire the input-output transfer function of the vibration sensor. Finally, one MFCs sample M8507-P1 as shown in Fig. 4.1 was glued on a sheet metal substrate with epoxy to fabricate the unimorph vibration sensor and an experiment was carried out to validate the frequency response function of output voltage predicted by the theoretical model.

![Figure 4.1. The schematic and photo of the MFCs sample](image)

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4.1.2 Constitutive relations of in-plane PZT-fiber composite

A physical model will be briefly presented here for the material parameters of the 1-3 PZT fiber composite on interdigitated transducer (IDT) electrodes. To describe the in-plane longitudinal vibration of the fiber composite, the effective constitutive relations for this homogeneous medium will be derived. The strain and electric field are chosen as the independent coordinates and the composite plate is laid in the y-z plane with the fibers lying along the z axes. The constitutive relations for the composite will give the stress and electric displacement for every point in the plate. Several approximations will be utilized to simplify the analysis and extract the essential physics. During ordinary excitation of the fiber composite, the shear mode vibration is thought to be suppressed and will not be coupled with the normal mode vibration. In an average sense, the electric field is independent of x and y coordinates throughout the individual phases. And the x and y components of the electric fields are thought to be zero for the longitudinal vibration modeling. The piezoelectric ceramic is poled along the fiber direction, and the constitutive relations in the ceramic phase are [9],

\[
T_1 = c_{11}E_1 + c_{12}E_2 + c_{13}E_3 - e_{31}E_3 \quad (4.1a)
\]

\[
T_2 = c_{12}E_1 + c_{11}E_2 + c_{13}E_3 - e_{31}E_3 \quad (4.1b)
\]

\[
T_3 = c_{13}E_1 + c_{13}E_2 + e_{33}E_3 - e_{33}E_3 \quad (4.1c)
\]

\[
D_3 = e_{31}E_1 + e_{31}E_2 + e_{33}E_3 + e_{33}E_3 \quad (4.1d)
\]

The elastic and dielectric constants of the ceramic phase will be distinguished from those of the polymer phase by the superscripts E and S, respectively. The stress, strain, field, and displacement in the different phases will be distinguished by a superscript p for the polymer phase and a superscript c for the ceramic phase in the following expressions. In the y direction,
the two different phases have the same stress value but opposite signs and strain will be replaced by stress as the independent coordinate for expressing essential physics meaning reasonably. The constitutive relations within the ceramic phase will be changed to [94],

\[
T_1^c = \frac{c_{11}^E c_{11}^E - c_{12}^E c_{12}^E}{c_{11}^E} S_1^c + \frac{c_{12}^E}{c_{11}^E} T_2^c + \frac{c_{13}^E c_{11}^E - c_{13}^E c_{12}^E}{c_{11}^E} S_3^c + \frac{c_{12}^E e_{31}^E - c_{11}^E e_{31}^E}{c_{11}^E} E_3^c \tag{4.2a}
\]

\[
S_2^c = -\frac{c_{12}^E}{c_{11}^E} S_1^c + \frac{1}{c_{11}^E} T_2^c - \frac{c_{13}^E}{c_{11}^E} S_3^c + \frac{e_{31}^E}{c_{11}^E} E_3^c \tag{4.2b}
\]

\[
T_3^c = \frac{c_{13}^E c_{11}^E - c_{13}^E c_{12}^E}{c_{11}^E} S_1^c + \frac{c_{12}^E}{c_{11}^E} T_2^c + \frac{c_{33}^E c_{11}^E - c_{13}^E c_{13}^E}{c_{11}^E} S_3^c + \frac{c_{12}^E e_{31}^E - c_{11}^E e_{33}^E}{c_{11}^E} E_3^c \tag{4.2c}
\]

\[
D_3^c = \frac{c_{11}^E e_{31}^E - c_{12}^E e_{31}^E}{c_{11}^E} S_1^c + \frac{e_{31}^E}{c_{11}^E} T_2^c + \frac{c_{11}^E e_{33}^E - c_{11}^E e_{31}^E}{c_{11}^E} S_3^c + \frac{e_{31}^E e_{31}^E + c_{11}^E e_{33}^S}{c_{11}^E} E_3^c \tag{4.2d}
\]

The strains are the same in ceramic and polymer during longitudinal vibration along the z direction when the composite has such fine spatial scale that stop-band resonances are at much higher frequencies than the longitudinal resonance.

\[
S_3^p = S_3^c = \bar{S}_3 \tag{4.3}
\]

The electric fields are also the same in both phases for the composite are applied voltage by IDT and equipotential.

\[
E_3^p = E_3^c = \bar{E}_3 \tag{4.4}
\]

Along x direction, the composite as a whole moves together and the strains are the same in both phases. The lateral stresses are equal in both phases along y direction. These are the lateral interaction conditions between the phases.

\[
S_1^p = S_1^c = \bar{S}_1 \tag{4.5}
\]

\[
T_2^p = T_2^c = \bar{T}_2 \tag{4.6}
\]

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Since the lateral periodicity is sufficiently fine, the effective total stress along x or z direction, total strain along y direction and total electric displacement along z direction can be acquired by averaging the contributions of the constituent phases. The average value is the sum of values in the two phases, where the contribution for each phase is in proportion to the volume fraction of each phase.

\[
\bar{T}_1 = \nu T_1^c + (1-\nu)T_1^p \tag{4.7a}
\]

\[
\bar{\varepsilon}_2 = \nu S_2^c + (1-\nu)S_2^p \tag{4.7b}
\]

\[
\bar{T}_3 = \nu T_3^c + (1-\nu)T_3^p \tag{4.7c}
\]

\[
\bar{D}_3 = \nu D_3^c + (1-\nu)D_3^p \tag{4.7d}
\]

where \(\nu\) and \((1-\nu)\) are the volume fractions of ceramic and polymer in the composite.

Equation (4.7) can be written in a matrix format when the combinations for all variables are simultaneously carried out,

\[
\begin{bmatrix}
\bar{T}_1 \\
\bar{S}_2 \\
\bar{T}_3 \\
\bar{D}_3
\end{bmatrix}
= (\nu A_c + (1-\nu)A_p)
\begin{bmatrix}
\bar{S}_1 \\
\bar{S}_2 \\
\bar{S}_3 \\
\bar{E}_3
\end{bmatrix}
= A \begin{bmatrix}
\bar{T}_1 \\
\bar{S}_2 \\
\bar{T}_3 \\
\bar{D}_3
\end{bmatrix}
\tag{4.8}
\]

where \(A_c\) is the coefficient matrix for the ceramic phase and \(A_p\) is the coefficient matrix for the polymer phase from equation (4.2). \(A\) is the combined coefficient matrix of the two phases.

Equation (4.8) can be rewritten in the original form,

\[
\begin{bmatrix}
\bar{T}_1 \\
\bar{T}_2 \\
\bar{T}_3 \\
\bar{D}_3
\end{bmatrix}
= \begin{bmatrix}
-c_{11} & c_{12} & c_{13} & -c_{31} \\
-c_{12} & c_{22} & c_{23} & -c_{32} \\
c_{13} & c_{23} & c_{33} & -c_{33} \\
-c_{31} & c_{32} & c_{33} & -c_{33}
\end{bmatrix}_A
\begin{bmatrix}
\bar{S}_1 \\
\bar{S}_2 \\
\bar{S}_3 \\
\bar{E}_3
\end{bmatrix}
\tag{4.9}
\]
The material parameters of the composite are given in expressions (4.10) in terms of the material parameters of the constituent phases and their proportions. The ratios of the equivalent elastic stiffness coefficient in 1 and 3 directions over the original elastic stiffness coefficient in 1 and 3 directions change with fibers’ volume fraction were shown in Fig. 4.2. The ratios of the
equivalent piezoelectric coefficient in 1 and 3 directions over the original piezoelectric coefficient in 1 and 3 directions change with fibers’ volume fraction were shown in Fig. 4.3. From these figures, the piezoelectric coefficient in the longitudinal direction increases much quicker than the elastic stiffness coefficient in the longitudinal direction for the composite with low proportion of piezoelectric material. The material properties of the composite could be adjusted by changing the volume fraction of the piezoelectric fibers. The device property such as the sensitivity of the vibration sensor could be optimized by choosing suitable proportion of piezoelectric material.

![Figure 4.2](image)

**Figure 4.2.** The ratios of the effective elastic stiffness coefficient in different directions over the original elastic stiffness coefficient change with fibers’ volume fraction

![Figure 4.3](image)

**Figure 4.3.** The ratios of the effective piezoelectric coefficient in different directions over the original piezoelectric coefficient change with fibers’ volume fraction

The PZT fiber composite sample includes 17 PZT fibers and the fiber's volume fraction \( \nu \) is nearly 0.51 by calculation. Unlike the piezo-fibers in Active-Fiber Composites (AFCs), the
piezo-fibers in MFCs have rectangular cross section, which increases the electrode contact and capacitance of the MFCs compared to AFCs. Elastic stiffness, piezoelectric coefficient and dielectric constants of single PZT fiber and epoxy (the polymer phase) were cited from the data in references [92, 94] and listed in Table 4.1. The geometry parameters of single PZT fiber and the PZT fiber composite were acquired from the website of Smart Material and listed in Table 4.2. The distance between IDT electrodes is 0.4mm, which is twice the thickness of the fibers. So the x and y components of the electric fields can nearly be thought to be zero for the longitudinal vibration modeling. With these coefficients and geometry parameters, the global properties of the PZT fiber composite can be calculated from expressions (4.10) and were listed in Table 4.1. These property parameters of the fiber composite were changed to piezoelectric strain coefficient $d_{33}$, tensile modulus $E$ and listed in Table 4.3. If they are compared with the standard data from the technical brochure of Smart Material, the piezoelectric strain coefficient matches the official data very well and the Young’s modulus and Poisson’s ratio have a little difference with them. The difference may be caused by different material properties between the reference and the fiber composite sample.

<table>
<thead>
<tr>
<th>Table 4.1. Composite component and global material properties</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>PZT 5H fiber</strong></td>
</tr>
<tr>
<td>$c_{12}^E (10^{10} \text{N/m}^2)$</td>
</tr>
<tr>
<td>$c_{13}^E (10^{10} \text{N/m}^2)$</td>
</tr>
<tr>
<td>$c_{33}^E (10^{10} \text{N/m}^2)$</td>
</tr>
<tr>
<td>$e_{31} (\text{C/m}^2)$</td>
</tr>
<tr>
<td>$e_{33} (\text{C/m}^2)$</td>
</tr>
<tr>
<td>$e_{33}/\varepsilon_0$</td>
</tr>
<tr>
<td><strong>Epoxy</strong></td>
</tr>
<tr>
<td>$c_{12} (10^{10} \text{N/m}^2)$</td>
</tr>
<tr>
<td>$\varepsilon_{11}/\varepsilon_0$</td>
</tr>
</tbody>
</table>
Table 4.2. Geometric properties of PZT fiber, MFCs and sheet metal substrates

<table>
<thead>
<tr>
<th>Materials</th>
<th>Length (mm)</th>
<th>Width (mm)</th>
<th>Thickness (mm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>PZT fiber</td>
<td>70</td>
<td>0.35</td>
<td>0.18</td>
</tr>
<tr>
<td>MFCs</td>
<td>70</td>
<td>7</td>
<td>0.30</td>
</tr>
<tr>
<td>Steel</td>
<td>70</td>
<td>7</td>
<td>0.127</td>
</tr>
</tbody>
</table>

Table 4.3. MFCs and sheet metal substrates material properties

<table>
<thead>
<tr>
<th>Materials</th>
<th>E ($10^{10}$N/m$^2$)</th>
<th>$\rho$ (kg/m$^3$)</th>
<th>$\bar{d}_{33}$ (10$^{-12}$m/V)</th>
<th>$\varepsilon_{33}/\varepsilon_o$</th>
</tr>
</thead>
<tbody>
<tr>
<td>MFCs (calculation)</td>
<td>3.47</td>
<td>4250</td>
<td>399</td>
<td>717</td>
</tr>
<tr>
<td>MFCs (standard)</td>
<td>3.03</td>
<td>(Not provided)</td>
<td>400</td>
<td>(Not provided)</td>
</tr>
<tr>
<td>Steel</td>
<td>20</td>
<td>7800</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Brass</td>
<td>11</td>
<td>8500</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Aluminum</td>
<td>7</td>
<td>2700</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Polyimide</td>
<td>0.32</td>
<td>1430</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

4.1.3 Lumped parameter electromechanical model for piezoelectric unimorph

The PZT fiber composite sample which was poled on dual sides along length (or 3-) directions with IDT was glued on a sheet metal substrate with epoxy to fabricate a piezoelectric unimorph and this device could be stimulated to work as a vibration sensor. The schematic of the unimorph was shown in Fig. 4.4. A simple mass-spring-damper structure can be used to model the dynamic behavior of the vibration sensor, in which the mass $M$ of the device is restrained by a damper $D$ and spring $K$ as shown in Fig. 4.5. It is assumed the device is attached to a vibration machine with vibration amplitude $x(t) = X \sin \omega t$. The equivalent circuit of the PZT fiber composite was shown in Fig. 4.6. If a sinusoidal force $F(t) = -M \omega^2 \sin \omega t$ acts on the vibration sensor, which consists of a leakage resistance $R_p$, a dielectric capacitance $C_p$ of the piezoelectric material and has a natural frequency $\omega_n = \sqrt{K/M}$, a vibration frequency $s = j\omega$, a damping
ratio $\zeta = D/2\sqrt{K M}$, and a time constant $\tau = R_p C_p$, the instantaneous open-circuit voltage in frequency domain can be related to the input force with the following transfer function [95],

$$\frac{V(s)}{F} = \frac{K_q}{C_p K} \frac{\omega_n^2}{s^2 + 2\zeta \omega_n s + \omega_n^2} \frac{s}{\tau s + 1}$$  \hspace{1cm} (4.11)

Applying the dimensionless frequency ratio $\gamma = \omega/\omega_n$, equation (4.11) becomes,

$$\frac{V(s)}{-X} = \frac{K_q}{C_p} \frac{\gamma^2}{1 - \gamma^2 + j2\zeta \gamma} \frac{s}{\tau s + 1}$$  \hspace{1cm} (4.12)

where $K_q$ is the charge generated per unit tip displacement, $C_p$ is the capacitance of the piezoelectric unimorph, $K$ is the spring constant. The output voltage of the unimorph vibration sensor depends on the static term (the materials properties and device structure), the dynamic term (second term), time constant of the equivalent RC circuit (third term), and vibration frequency. The frequency response of the output voltage for the vibration sensor can be calculated with different damping ratios and time constants. The frequency response of the magnitude $X$ of the output voltage divided by the input vibration amplitude with different damping ratios was shown in Fig. 4.7. The time constant for the fiber composite sample is 769s in our study.

![Figure 4.4](image.png)

**Figure 4.4.** The schematic of the MFCs unimorph vibration sensor
Figure 4.5. A simple mass-spring-damper structure for the vibration sensor

Figure 4.6. The equivalent circuit of the PZT fiber composite

Figure 4.7. The frequency response of the magnitude $X$ of the output voltage divided by the input vibration amplitude with different damping ratios
Using the global properties and geometric parameters of the fiber composite and sheet metal substrate, the spring constant $K$, the charge generated per unit tip displacement $K_q$, the capacitance $C_p$ of the piezoelectric unimorph can be derived from the constituent equations for piezoelectric unimorph [96]. And the frequency response functions (FRFs) of this vibration sensor can be calculated by substituting the parameters for the piezoelectric unimorph into the one dimension dynamic model for piezoelectric device. The resonance frequency, effective frequency range and sensitivity of the vibration sensor can be obtained from the FRFs directly.

If a unimorph with the piezoelectric material layer excited in 33 mode is subjected to an applied electric voltage $V$ and an external force $F$ acting on the tip of the unimorph perpendicular to the length direction, the total energy of the unimorph bender can be expressed as [96],

$$U = -\frac{\tilde{d}_{33}^2 E_3^2 t_p t_m (s_{33}(t_m)^3 + s_{11}^m(t_p)^3)Lw}{2D} - \frac{3\tilde{d}_{33}^2 E_3 F s_{11}^m s_{33} t_p (t_m + t_p)L^2}{D} + \frac{2F^2 s_{11}^m s_{33}(\tilde{\sigma}_{33} t_m + s_{11}^m t_p)L^2}{Dw} + \frac{1}{2} \epsilon_{33} E_3^2 L w t_p$$

The generated tip deflection $\delta$ and electrical charge $Q$ can be expressed by the following constitutive equation,

$$\begin{bmatrix} \delta \\ Q \end{bmatrix} = \begin{bmatrix} 4s_{11}^m (s_{33} t_m + s_{11}^m t_p)L^3 \\ 3nd_{33} s_{11}^m s_{33} t_p (t_m + t_p)L \\ 3n d_{33} s_{11}^m s_{33} t_p (t_m + t_p)L \\ 3n d_{33} s_{11}^m s_{33} t_p (t_m + t_p)L \\ 3n d_{33} s_{11}^m s_{33} t_p (t_m + t_p)L \end{bmatrix} \begin{bmatrix} F \\ V \end{bmatrix}$$

where $D = (s_{11}^m)^2 (t_p)^4 + 4s_{11}^m \frac{1}{33} s_{33} t_m (t_p)^3 + 6s_{11}^m s_{33} (t_m)^2 (t_p)^2 + 4s_{11}^m s_{33} t_p (t_m)^3 + (s_{33}^p)^2 (t_m)^4$, the subscript $p$ denotes the upper piezoelectric material layer and subscript $m$ denotes the lower elastic metal layer; $s_{11}^m$ and $s_{33}^p$ are the elastic compliance of the elastic layer and the
piezoelectric layer; $t_m$ and $t_p$ are the thickness of elastic layer and piezoelectric layer; $\bar{d}_{33}$ and $\bar{\varepsilon}_{33}$ are the piezoelectric constant and dielectric constant of the piezoelectric material, $L$ and $w$ are the length and width of unimorph, $n$ is the capacitor number between every anode and cathode of the IDT and it is 140 in the sample. The dimension parameters and material properties for the fiber composite and sheet metal substrate used in our study were listed in Table 4.2 and Table 4.3.

To visualize the effect of dimensions and material properties of piezoelectric and elastic layers on the performance of the vibration sensor, we define

$$A = \frac{\bar{d}_{33}}{s_{11}} \frac{E_m}{E_p}, \quad B = \frac{t_m}{t_p}$$

When the applied voltage is zero, the tip displacement due to the force is $\delta = aF$, therefore the spring constant $K$ will be

$$K = \frac{1}{a} = \frac{wt_p^3}{4s_{33}L^3} \frac{1 + 4AB + 6AB^2 + 4AB^3 + A^2B^4}{AB + 1}$$

When the applied voltage is zero, the charge generated per unit tip displacement $K_q$ can also be obtained,

$$K_q = \frac{3n\bar{d}_{33}t_p^2w}{4s_{11}L^2} \frac{B(B + 1)}{AB + 1}$$

The capacitance of the piezoelectric unimorph bender is

$$C_p = n^2 \frac{wt_p \bar{d}_{33}}{L} (1 - k_{33}^2) \frac{AB (1 + AB^3)}{1 + 4AB + 6AB^2 + 4AB^3 + A^2B^4}$$

The voltage generation coefficient can then be obtained,
\[
\frac{K_q}{C_p K} = \frac{3d_{33}L^2}{n\varepsilon_{33}w t_p^2} \left(1 + 4AB + 6AB^2 + 4AB^3 + A^2B^4\right) - k_{33}^2 AB(1 + AB^3)
\]  

(4.19)

Since \(t \ll L\), and \(w \ll L\), by choosing appropriate device dimension and the elastic substrate material, the quantities related to the thickness ratio and Young’s modulus ratio could be optimized [86, 91]. The voltage generation coefficient of the vibration sensor with different substrate materials change with the MFCs and the substrate materials thickness ratio were shown in Fig. 4.8. Compared to the original 3-1 mode unimorph, the low electromechanical coupling mode is changed to 3-3 mode with increased piezoelectric coefficient in the numerator part, negatively increased electromechanical coupling coefficient in the denominator part, parameter second-order proportional to the \(L/t_p\). And if PZT fiber composite is used as the piezoelectric material, the dielectric constant in the denominator part will also decrease much. All these factors will increase the voltage generation coefficient of the device and high sensitivity is expected for the PZT fiber composite vibration sensor.

![Figure 4.8. The voltage generation coefficient change with the thickness ratio B for different substrate materials](image-url)
The fundamental bending resonance frequency of a piezoelectric unimorph is given by [97],

\[
\omega_n = \frac{3.52 \tau_p}{2L^2} \sqrt{\frac{E_p}{3 \rho_p}} \left[ \frac{1 + 4AB + 6AB^2 + 4AB^3 + A^2 B^4}{(1 + BC)(AB + 1)} \right]^{1/2}
\]

(4.20)

where C is the density ratio \( \rho_m / \rho_p \) of the elastic layer and the piezoelectric layer. A low resonance frequency is often desirable for the working mode of the vibration sensor. Flexural vibration mode or bending mode is often chosen since it has the lowest resonance frequency compared to other mode.

### 4.1.4 Distributed parameter electromechanical model for piezoelectric unimorph

A distributed parameter electromechanical model was also proposed for cantilevered piezoelectric energy harvesters [98]. In this model, the piezoelectric material is excited in 3-1 mode and exact analytical solution can be acquired with Euler-Bernoulli beam assumptions. This model can also be utilized to analyze piezoelectric unimorph vibration sensors. After modification, the FRF of the steady state output voltage for the piezoelectric unimorph excited in 3-3 mode can be expressed as [98],

\[
u(t) = \sum_{r=1}^{\infty} \frac{j m \omega^3 \phi_r \gamma_r}{\omega_r^2 - \omega^2 + j 2 \zeta_r \omega, \omega} \tau e^{-j \omega t} + \sum_{r=1}^{\infty} \frac{j \omega \zeta_r \phi_r}{\omega_r^2 - \omega^2 + j 2 \zeta_r \omega, \omega} \tau c e^{-j \omega t}
\]

(4.21)

where \( Y_0 \) is the amplitude of the base translation, \( m \) is the mass per unit length of the beam, \( \omega \) is the driving frequency.
\[ \varphi_r = -\frac{d_{33} E_p t_{pc} L}{\varepsilon_{33} t_p} \frac{d\phi_r(x)}{dx} \bigg|_{x=L} \] (4.22)

\[ \gamma_r = \int_{x=0}^{L} \phi_r(x) dx \] (4.23)

where \( t_{pc} \) is the distance from the center of the PZT layer to the neutral plane,

\[ t_{pc} = \frac{t_m A(1 + B)}{2(1 + AB)} \] (4.24)

\[ \phi_r(x) = \sqrt{\frac{1}{mL}} \left[ \cosh \frac{\lambda_r}{L} - \cos \frac{\lambda_r}{L} x - \sigma_r \left( \sin \frac{\lambda_r}{L} x - \sin \frac{\lambda_r}{L} L x \right) \right] \] (4.25)

is the \( r \)th mode mass normalized eigenfunction of the clamped-free beam. The \( \lambda_r \)'s are the dimensionless frequency numbers obtained from the characteristic equation given by

\[ 1 + \cos \lambda \cosh \lambda = 0 \] (4.26)

and \( \sigma_r \) is expressed as

\[ \sigma_r = \frac{\sinh \lambda_r - \sin \lambda_r}{\cosh \lambda_r + \cos \lambda_r} \] (4.27)

\[ \omega_r = \lambda_r^2 \sqrt{\frac{YI}{mL^2}} \] (4.28)

is the \( r \)th mode undamped natural frequency and \( YI \) is the bending stiffness of the composite cross section given by,

\[ YI = \frac{3}{w} \left[ \frac{E_m (t_b^3 - t_a^3) + E_p (t_c^3 - t_b^3)}{3} \right] \] (4.29)

\[ t_a = -\frac{t_p (1 + 2B + AB^2)}{2(1 + AB)} \] (4.30)

\[ t_b = -\frac{t_p (AB^2 - 1)}{2(1 + AB)} \] (4.31)
\[ t_c = \frac{t_p (1 + 2AB + AB^2)}{2(1 + AB)} \]  

(4.32)

where \( t_a \) is the position of the bottom of the substrate from the neutral plane, \( t_b \) is the position of the bottom of the PZT layer from the neutral plane, \( t_c \) is the position of the top of the PZT from the neutral plane. The mechanical damping ratio that includes the effects of both strain rate damping and viscous air damping is given by

\[ \xi_r = \frac{c_s I \omega_r}{2YI} + \frac{c_a}{2m \omega_r} \]  

(4.33)

where \( c_s \) is the equivalent coefficient of strain rate damping, \( I \) is the equivalent area moment of inertia of the composite cross section, \( c_a \) is the viscous air damping coefficient.

\[ \chi_r = -\frac{E_p d_{33} w}{2L} \left( t_c^2 - t_b^2 \right) \frac{d\phi(x)}{dx} \bigg|_{x=L} \]  

(4.34)

is the mode coupling term and the time constant of the circuit is given by

\[ \tau_c = \frac{R_p \bar{e}_{33} w \ell_p}{L} \]  

(4.35)

The FRF of the output voltage for the vibration sensor can be calculated using expressions (4.21-4.35) of the distributed parameter electromechanical model.

### 4.1.5 Experiment

To validate the theoretical estimation, the vibration sensor was mounted on a LDS shaker (model V203) and driven by a LDS power amplifier (PA25E). The signal fed into the LDS power amplifier was generated by a lock-in amplifier (model SR850). The experiment setup was shown in Fig. 4.9. The fundamental resonance frequency of the unimorph was 50Hz by calculation and
the open-circuit output voltage in the frequency range 0 to 1000Hz was recorded in our experiment. A reference accelerometer (PCB U352C22) with a sensitivity 9.66 mV/g was also mounted on the shaker to measure the input acceleration. When the shaker was excited in the z-axis direction by the signal of the LDS controller, the signals generated by both the vibration sensor and the accelerometer were fed back into the lock-in amplifier and the amplitude and phase of the signals were recorded by Labview software simultaneously. The block diagram of the experiment measurement system was shown in Fig. 4.10. The open-circuit voltage per unit vibration amplitude versus frequency curve from 0 to 1000Hz was compared with two models calculation results and shown in Fig. 4.11. The damping ratios $\zeta$ used in the two models calculation are all assumed to be 0.02. The first three resonance frequencies in the experiment are 50Hz, 315Hz, and 896Hz, respectively. The fundamental resonance frequency calculated by lumped parameter model is 50 Hz which is the same as the experimental result. It is much lower than that of bulk PZT ceramic with the same size for the small elastic stiffness coefficient of the fiber composite. The first three resonance frequencies calculated by the distributed parameter mode are 48Hz, 301Hz, and 843Hz, respectively, which have 4%, 5%, and 6% differences from the experimental results. For low damping ratio condition, distributed parameter model is much more accurate than lumped parameter model to predict the output property at the frequency range around high order resonance frequency. If this vibration sensor is used in industrial environment, the damping ratio will be much higher than in the experimental condition as the high damping ratio conditions shown in Fig. 4.7. If the damping ratio 0.707 is used in the experiment, the high order resonance will be damped and the lumped parameter model is also an effective method to predict the vibration property at a wide frequency range.
Figure 4.9. The experiment setup with one MFCs glued on a sheet metal substrate and clamed to a LDS shaker.

Figure 4.10. The block diagram of the experiment measurement system.

Figure 4.11. Experimental and calculation results of the frequency response of output voltage per unit vibration amplitude for a MFCs unimorph.
4.2 STRAIN SENSOR FOR SOFT MATERIAL STRAIN MEASUREMENT

4.2.1 Introduction

Polymeric materials have been widely used in electronic and electromechanical transduction field [99]. The behavior of the material under an external electric field is important for material selection. Because the polymer material to be characterized is very soft, the external electric field induced strain in thin polymer film is still very difficult to be determined accurately without any constraint being imposed to the sample. And typical mechanical testing is destructive for tissue/soft material and specimens are required to be cut to a suitable shape to fit the tester [100]. Conventionally, strain (or displacement) response in a mechanical structure of material can be characterized by various techniques, which can be grouped into two categories: the noncontact methods and contact methods [64].

In the case of noncontact methods such as the laser strain micrometry are used, two laser beams are needed to focus on the opposite faces of the sample for the out-of-plane strain measurement. Furthermore, the laser beam should be reflected at the ends of the structure or sample in characterizing the transverse strain response of it. The major benefit for this method is its non-contact nature. The measurement results of the laser are very accurate based on the requirements that the laser beam is aligned properly and the measured surface of the sample can reflect enough light. However, a laser instrument is usually too bulky to be easily carried on and the technique is so delicate that laboratory conditions are required for its use. Furthermore, flexural vibration mode in the structure may be excited in the strain measurement for thin and soft sample, which will cause errors to the final result [65]. An optical microscope is another
noncontact instrument, which can only characterize the strain response at low strain response region, due to its limited resolution [66].

The contact methods such as differential capacitive sensor or linear variable differential transformer (LVDT) have been developed for strain/displacement measurement. These two techniques either measures the voltage output of two differential parallel plate capacitors or that of two differential transformers to reflect the displacement change of structure. But complex circuit requirements and sensitivity to vibration keep these two methods from being very practical for strain measurement. In the situation where a strain gauge is used and the sensor will not affect the original structure, the strain can be acquired by measuring the electric voltage change with external stress exerted on the structure. Piezoresistive and piezoelectric materials are commonly used for strain sensors. Adhesives are used to attach the strain sensor to the host structure prior to measurement [101]. This method is very simple for large structures but may not be suitable for smaller ones. The size of the strain sensor and even the thickness of the adhesives can influence the behavior of small structures under test.

Atomic force microscope using a cantilever beam with high sensitivity in detecting small force has inspired the idea that using piezoelectric bimorph cantilever beam to characterize the electric field induced strain in soft and thin polymeric samples without imposing large stress or mechanical constrains in the sample [102, 103]. A bimorph based dilatometer was then developed to characterize the electric field induced strain response in soft and thin free standing polymer films in the out of plane direction [104]. This dilatometer can work over a relatively wide frequency range from 0.1 Hz to 1 kHz and it is capable of detecting displacement down to subangstrom range with high accuracy. And another dilatometer was developed for the measurement of the transverse strain response in electrostrictive PVDF film [105]. Many other
works also focused to compare the design of the dilatometer using different sensor heads and platforms and to improve the performance as stability and reliability of it [106]. The sensitivity of the piezoelectric bimorph dilatometer depends on the design and assembles of the piezoelectric configuration and amplification device strongly [107]. And careful preparation of piezoelectric device will be very important for the final performance of the device. The bimorph based dilatometer is a suitable choice for measuring the field induced strain at low frequencies in thin and soft polymer films under high voltage [108].

The bulk PZT ceramic in the original piezoelectric bimorph design is commonly used for sensors due to its high piezoelectric coefficient and wide bandwidth. But several disadvantages are also accompanied with it, such as high dielectric constant, low elastic compliance and so on. The high dielectric constant of bulk PZT reduces the electromechanical coupling coefficient of it and converts less electric energy from the same mechanical deformation compared to piezoelectric materials with low dielectric constant [86]. The low elastic compliance of bulk PZT makes it too hard to be applied for very soft polymer material. And the bulk PZT is very brittle and unable to withstand large deformation of the sample which limits its strain measurement range.

Two alternative methods have been developed to overcome these disadvantages [92]. One uses thin film deposition of PZT on the substrate [93] and the other uses packaged PZT composites. PZT thin film needs complex technical processes to be integrated on the substrate and has low charge output. A piezoelectric composite sensor or actuator comprises of one piezoelectric material layer sandwiched between two soft thin encapsulating layers. 1-3 piezoelectric composites which are most commonly used are composed of piezoelectric ceramic rods embedded in a non-piezoelectric matrix [10]. PZT fiber composites can decouple the lateral
effect applied to the sensor synchronously and a large sensitivity can be obtained from the sensor [11]. They also have the benefits such as lower dielectric constant, improved elastic compliance and improved electromechanical coupling coefficient and are suitable for strain sensor application. Both $d_{31}$ and $d_{33}$ Macro Fiber Composites (MFCs) transducers as shown in Fig. 4.12 have been developed and are currently produced by Smart Material (Dresden, Germany) [92]. Unlike the piezo-fibers in Active-Fiber Composites (AFCs), the piezo-fibers in MFCs have rectangular cross section, which increases the electrode contact and capacitance of the MFCs compared to AFCs.

![MFCs sample](image)

**Figure 4.12.** The schematic and photo of the MFCs sample

From the above consideration, a PZT fiber composite piezoelectric unimorph strain sensor was proposed to characterize the electric field induced strain response in the out-of-plane direction of soft polymer material samples. The polymer film sample expands and contracts under an external electric field in the $z$ direction, and generates a bending and consequently an electrical output in the unimorph by piezoelectric effect. The electrical output is proportional to the sensor tip displacement. The strain-dependent charge generation has been utilized for strain sensing in the polymer sample quantitatively [87-90]. The global parameters of the fiber
composite were substituted into lumped parameter constituent equations for piezoelectric unimorph to acquire the input-output transfer function of the strain sensor. The PZT fiber composite with different substrate materials were analyzed for sensitivity and softness improvement. The schematic of the test bench for high resolution displacement measurement is shown in Fig. 4.13. Laser displacement meter was also used to verify the accuracy of the strain sensor. Then the data was used to calculate the electrostrictive coefficient of the silicone elastomer material.

![Figure 4.13. The schematic of the test bench for high resolution soft material strain measurement](image)

### 4.2.2 Lumped parameter transfer function

The PZT fiber composite sample which was poled on dual sides along length (or 3-) directions with IDT was glued on the substrate material with epoxy to fabricate the piezoelectric unimorph and this device could work as a strain sensor. The schematic of the unimorph was shown in Fig. 4.14. A simple mass-spring-damper structure can be used to model the dynamic behavior of the
strain sensor, in which the mass $M$ of the device is restrained by a damper $D$ and spring $K$ as shown in Fig. 4.15. The equivalent circuit of the fiber composite was shown in Fig. 4.16. If a sinusoidal force $F(t) = -MX\omega^2 \sin \omega t$ acts on the strain sensor, which consists of a leakage resistance $R_p$, a dielectric capacitance $C_p$ of the piezoelectric material and has a natural frequency $\omega_n = \sqrt{K/M}$, a vibration frequency $s = j\omega$, a damping ratio $\zeta = D/2\sqrt{KM}$, and a time constant $\tau = R_pC_p$, the instantaneous open-circuit voltage in frequency domain can be related to the input force with the following transfer function [109],

$$\frac{V(s)}{F} = \frac{K_q}{C_pK} \frac{\omega_n^2}{s^2 + 2\zeta\omega_n^2 s + \omega_n^2} \frac{\tau s}{\tau s + 1}$$  \hspace{1cm} (4.36)

Applying the dimensionless frequency ratio $\gamma = \omega/\omega_n$, Eq. (4.36) becomes,

$$\frac{V(s)}{F} = \frac{K_q}{C_p} \frac{\gamma^2}{1 - \gamma^2 + j2\zeta\gamma} \frac{\tau s}{\tau s + 1}$$  \hspace{1cm} (4.37)

where $K_q$ is the charge generated per unit tip displacement, $C_p$ is the capacitance of the piezoelectric unimorph, $K$ is the spring constant. The output voltage of the unimorph strain sensor depends on the static term (the materials properties and device structure), the dynamic term (second term), time constant of the equivalent RC circuit (third term), and vibration frequency. The time constant for the fiber composite sample is 769s in our study. Using the global properties and geometric parameters of the fiber composite and substrate material, the spring constant $K$, the charge generated per unit tip displacement $K_q$, the capacitance $C_p$ of the piezoelectric unimorph can be derived from the constituent equations for it [96]. And the frequency response functions (FRFs) of this strain sensor can be calculated by substituting the parameters for the piezoelectric unimorph into the one dimension dynamic model for
piezoelectric device. The resonance frequency, effective frequency range and sensitivity of the strain sensor can be obtained from the FRFs directly.

![Figure 4.14. The schematic of the MFCs unimorph strain sensor](image)

![Figure 4.15. A simple mass-spring-damper structure for the strain sensor](image)

![Figure 4.16. The equivalent circuit of the PZT fiber composite](image)

To visualize the effect of dimensions and material properties of piezoelectric and elastic layers on the performance of the strain sensor, we define
$A = \frac{s_{33}^p}{s_{11}^m} = \frac{E_m}{E_p}, \quad B = \frac{t_m}{t_p}$

(4.38)

where the subscript $p$ denotes the upper piezoelectric material layer and subscript $m$ denotes the lower elastic metal layer; $s_{11}^m$ and $s_{33}^p$ are the elastic compliance of the elastic layer and the piezoelectric layer; $t_m$ and $t_p$ are the thickness of elastic layer and piezoelectric layer. When the applied voltage is zero, the tip displacement due to the force is $\delta = aF$, therefore the spring constant $K$ will be

$$K = \frac{1}{a} = \frac{\omega t_p^3}{4S_{33}L^3} \frac{1 + 4AB + 6AB^2 + 4AB^3 + A^2B^4}{AB + 1}$$

(4.39)

When applied voltage is zero, the charge generated per unit tip displacement $K_q$ is [109],

$$K_q = \frac{3nd_{33}t_p^2\omega AB(B + 1)}{4S_{33}L^2 AB + 1}$$

(4.40)

The capacitance of the piezoelectric unimorph bender is [109],

$$C_p = n^2 \frac{\omega t_p \bar{e}_{33}}{L} (1 - k_{33}^2 \frac{AB(1 + AB^3)}{1 + 4AB + 6AB^2 + 4AB^3 + A^2B^4})$$

(4.41)

The voltage generated per unit tip displacement can then be obtained,

$$K_q / C_p = \frac{3d_{33}t_p}{4nS_{33} \bar{e}_{33}L} \frac{AB(B + 1)}{(AB + 1)(1 - k_{33}^2 AB(1 + AB^3)/(1 + 4AB + 6AB^2 + 4AB^3 + A^2B^4))}$$

(4.42)

where $d_{33}$ and $\bar{e}_{33}$ are the piezoelectric constant and dielectric constant of the piezoelectric material, $L$ and $w$ are the length and width of unimorph, $n$ is the capacitor number between every anode and cathode of the IDT. The gap distance between IDT is 0.5 mm and the gap number $n$ for the MFCs (M8507-P1) is 170.
Since $t \ll L$, and $w \ll L$, by choosing appropriate device dimensions and substrate materials, the unimorph parameters which relate to A or B could be optimized [91]. Steel, brass, aluminum, and polyimide were chosen as substrate materials. The dimension parameters and material properties for the fiber composites and substrate materials used in our study were listed in Table 4.4 and Table 4.5. The elastic stiffness coefficient ratios A for steel, brass, aluminum and polyimide substrates were 6.67, 3.67, 2.33, and 0.11 respectively. To locate the neutral plane position of the unimorph in the substrate material, B should be larger than 0.39, 0.52, 0.66, and 3.02 respectively. The voltage generated per unit tip displacement of the strain sensor with different substrate materials change with the thickness ratio B were shown in Fig. 4.17. The charge generated per unit tip displacement of the strain sensor with different substrate materials change with the thickness ratio B were shown in Fig. 4.18. The spring constant of the strain sensor with different substrate materials change with the thickness ratio B were shown in Fig. 4.19. The voltage and charge sensitivity for the unimorph with metal substrates increase quickly as the thickness ratio B increases. But they increase very slowly with polymer substrate as the thickness ratio B increases. The spring constants for the unimorph with different substrates have the same trend. So the unimorph with metal substrate is suitable for high sensitivity application and the one with polymer substrate is suitable for high flexibility application.

<table>
<thead>
<tr>
<th>Materials</th>
<th>Length (mm)</th>
<th>Width (mm)</th>
<th>Thickness (mm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>MFC (M8507-P1)</td>
<td>85</td>
<td>7</td>
<td>0.30</td>
</tr>
<tr>
<td>Original bimorph</td>
<td>10</td>
<td>1.5</td>
<td>0.30</td>
</tr>
<tr>
<td>Steel</td>
<td>70</td>
<td>7</td>
<td>0.117</td>
</tr>
<tr>
<td>Brass</td>
<td>70</td>
<td>7</td>
<td>0.156</td>
</tr>
<tr>
<td>Aluminum</td>
<td>70</td>
<td>7</td>
<td>0.198</td>
</tr>
<tr>
<td>Polyimide</td>
<td>70</td>
<td>7</td>
<td>0.906</td>
</tr>
</tbody>
</table>
Table 4.5. Material properties of bimorph, MFCs and substrates

<table>
<thead>
<tr>
<th>Materials</th>
<th>E (10^10 N/m^2)</th>
<th>ρ (kg/m^3)</th>
<th>$\bar{d}<em>{33}$ or $d</em>{31}$ (10^-12 m/V)</th>
<th>$\varepsilon_{33}/\varepsilon_o$</th>
</tr>
</thead>
<tbody>
<tr>
<td>MFCs</td>
<td>3.03</td>
<td>4250</td>
<td>400</td>
<td>717</td>
</tr>
<tr>
<td>Original bimorph</td>
<td>6.06</td>
<td>7600</td>
<td>-274</td>
<td>1400</td>
</tr>
<tr>
<td>Steel</td>
<td>20</td>
<td>7800</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Brass</td>
<td>11</td>
<td>8500</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Aluminum</td>
<td>7</td>
<td>2700</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Polyimide</td>
<td>0.32</td>
<td>1430</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Figure 4.17. Voltage sensitivity of the strain sensor change with the thickness ratio B with different substrate materials

Figure 4.18. Charge sensitivity of the strain sensor change with the thickness ratio B with different substrate materials
Figure 4.19. Spring constant of the strain sensor change with the thickness ratio \( B \) with different substrate materials

For the bimorph strain sensor, the charge generated per unit tip displacement is \([110, 111]\),

\[
K_{qo} = \frac{3d_{31}E_p tw}{8L} \quad (4.43)
\]

The spring constant of the piezoelectric bimorph bender is

\[
K_o = \frac{E_p w t^3}{4L^3} \quad (4.44)
\]

The capacitance of the piezoelectric bimorph bender is

\[
C_{po} = \frac{8wL}{t} \quad (4.45)
\]

The voltage generated per unit tip displacement is

\[
K_{qo}/C_{po} = \frac{3d_{31}E_p t^2}{8\varepsilon L^2} \quad (4.46)
\]

The relative ratio of the voltage generation coefficients of the unimorph to the bimorph is,

\[
\frac{K_q}{K_{qo}} = \frac{\bar{d}_{33} \varepsilon L}{n\bar{\varepsilon}_{33} E_p d_{31} \varepsilon_{33} f} \frac{AB/(AB+1)}{(1-k_{33}AB(1+AB^3)/(1+4AB+6AB^2+4AB^3+A^2B^4))} \quad (4.47)
\]
By substituting the material parameters into Eq. 4.47, it can be approximately simplified to

\[
\frac{K_d}{K_q} \approx \frac{5AB}{(AB + 1)(1 - k_{33}^2(AB + A^3))(1 + 4AB + 6AB^2 + 4AB^3 + A^2B^4)}
\]  

(4.48)

The relative ratio of the spring constants of the unimorph to the original bimorph is,

\[
\frac{K}{K_o} = \frac{1}{s_{33}E_p} \frac{1 + 4AB + 6AB^2 + 4AB^3 + A^2B^4}{(AB + 1)(1 + B)^3}
\]  

(4.49)

By substituting the material parameters into Eq. 4.49, it can be approximately simplified to

\[
\frac{K}{K_o} \approx \frac{1 + 4AB + 6AB^2 + 4AB^3 + A^2B^4}{2(AB + 1)(1 + B)^3}
\]  

(4.50)

The voltage sensitivity relative ratio of the unimorph to the bimorph change with the thickness ratio B with different substrate materials were shown in Fig. 4.20. The spring constant relative ratio of the unimorph to the bimorph change with the thickness ratio B with different substrate materials were shown in Fig. 4.21. The voltage sensitivity relative ratio of the unimorph with brass or aluminum substrates to the bimorph increases quickly as the thickness ratio B increases. But the spring constant relative ratio of the unimorph with brass or aluminum substrates to the bimorph increases slowly as the thickness ratio B increases. So these unimorph strain sensors with brass or aluminum substrates are suitable for measuring the samples which has moderate strength with high sensitivity. Compared to the original design, the low electromechanical coupling 3-1 mode bimorph is changed to 3-3 mode unimorph with increased piezoelectric coefficient in the numerator part, negatively increased electromechanical coupling coefficient in the denominator part, and a performance parameter which is proportional to $L/nt$ and caused by equivalent capacitance variation. If PZT fiber composite is used as the piezoelectric material, the dielectric constant in the denominator part will also decrease much. All of these factors are the reasons for the high sensitivity of the unimorph fiber composite strain sensor. The voltage
sensitivity relative ratio of the unimorph with polyimide substrate to the bimorph increases slowly as the thickness ratio B increases. But the spring constant relative ratio of the unimorph with polyimide substrate to the bimorph decreases much and later keeps 1/8 as the thickness ratio B increases. So the unimorph strain sensor with polyimide substrate is suitable for measuring very soft polymer samples with moderate sensitivity and without any destructive effect.

Figure 4.20. Voltage sensitivity relative ratio of the unimorph to the bimorph change with the thickness ratio B with different substrate materials

Figure 4.21. Spring constant relative ratio of the unimorph to the bimorph change with the thickness ratio B with different substrate materials

The fundamental bending resonance frequency of a piezoelectric unimorph is \[97\],

\[
\omega_n = \frac{3.52t_p}{2L^2} \sqrt{\frac{E_p}{3\rho_p}} \left[\frac{1 + 4AB + 6AB^2 + 4AB^3 + A^2B^4}{(1 + BC)(AB + 1)}\right]^{1/2}
\]

(4.51)
where C is the density ratio $\rho_m / \rho_p$ of the elastic layer to the piezoelectric layer. This resonance frequency is useful to predict the effective operating frequency range of the strain sensor. At approximately 1/5 of the resonance frequency, the response of the sensor is 5% over the response at calibration frequency. There is 5% measured error left compared to the result at calibration frequency. At approximately 1/3 of the resonance frequency, the error increases to 10% compared to the result at calibration frequency. The effective operating frequency should be lower than 1/3 of the resonance frequency.

### 4.2.3 Experiment

A sinusoidal signal was generated by a lock-in amplifier (SR850) and amplified by a LDS power amplifier (PA25E) to drive a thin PZT disk to generate the displacement for sensor calibration. The peak to peak vertical displacement was firstly measured by a Fotonic sensor system (MTI-2000). The PZT disk sample vibrated in bending mode under an external electric field and the generated displacement was transferred to the sensor by contacting the sensor tip to the sample. The other end of the strain sensor is clamped at a solid support. An electrical output which is proportional to the sensor head displacement is generated. The peak to peak output voltage from the sensor was sent back to the lock-in amplifier. The experiment setup for the displacement measurement was shown in Fig. 4.22. With the displacement and voltage values, the sensitivity of the strain sensor could be acquired and verified by comparing with the calculation result. A 0.0472V voltage was generated from the strain sensor with 1um displacement at the sensor tip and the voltage sensitivity of it was 0.0518V/um by calculation. The calculation and experiment results have 8.9% error. After calibration, this strain sensor could be used to quantitatively measure the displacement and strain of the soft polymer sample.
Figure 4.22. The experiment setup for the high resolution displacement measurement

Poly(dimethylsiloxane) (PDMS) is highly elastic and biologically inert and it has superior compatibility with human tissue [112]. So it is widely used in medical applications such as surgical implants and catheters [113, 114]. PDMS was chosen as the soft polymer sample material in our experiment. Its strain and electrostrictive coefficient were measured which could be utilized for the cell culture control application. ELASTOSIL® RT 601 (Wacker Chemical, Adrian, MI) was spin coated to thin film to form the PDMS sheet. This silicone resin is composed of two components: component A contains platinum catalyst, and component B contains the crosslinker. The two components were mixed at 9:1 by volume fraction. The same procedure as calibration was used to excite and measure the PDMS sheet. The block diagram of the measurement system for the strain $S$ and electrostrictive coefficient $R$ of soft polymer material was shown in Fig. 4.23. The output voltage and the sensitivity of the strain sensor were used to calculate the displacement of the thin film. Combining with the film thickness, the strain and the electrical field strength $E_0$ in the film could be calculated. Then the electrostrictive coefficient of the polymer could be calculated by the following equation.

$$S = RE_0^2 (1 - 2 \cos 2\omega t) / 2$$

(4.52)

The strain change with the square of the electric field strength at a specific frequency 10Hz was shown in Fig. 4.24. They have a good linear relationship. The electrostrictive coefficient of the
PDMS sheet at different frequencies was shown in Fig. 4.25. The electrostrictive coefficient decreased from $-7.19 \times 10^{-17} \text{ m}^2/\text{V}^2$ to $-7.14 \times 10^{-17} \text{ m}^2/\text{V}^2$ as the exciting frequency increased from 1Hz to 10Hz.

**Figure 4.23.** The block diagram of the measurement system for the strain and electrostrictive coefficient of soft polymer material

![Block diagram](image)

**Figure 4.24.** The strain versus the square of electric field at the frequency 10Hz for the PDMS sheet

![Graph](image)

**Figure 4.25.** The electrostrictive coefficient of the PDMS thin film at different frequencies
The sensor tip will exert a force to the soft polymer sample during measurement, which will also introduce an error to the final displacement or strain result as shown in Fig. 4.26. A correction factor $\gamma$ which is defined as the real displacement $\Delta_0$ to the measured displacement $\Delta$ will be introduced to the measurement result. From Newton’s third law, the force from the sensor tip equals to the force generated by the deformation ($\Delta - \Delta_0$) in the sample.

$$K\Delta = A(\Delta - \Delta_0)Y_p / a_p$$

(4.53)

where $K$ is the spring constant of the strain sensor from Eq. (4.39), $A$ is the contacting area of the sensor tip with the sample, $Y_p$ is the Young’s modulus and $a_p$ is the thickness of the sample, respectively. So the correction factor $\gamma$ can be expressed as,

$$\gamma = \Delta_0 / \Delta = 1 - Ka_p / AY_p$$

(4.54)

A small measurement error requires $\Delta_0 / \Delta$ be nearly equal to one [106]. That is to say,

$$\frac{AY_p}{Ka_p} = \frac{AY_p}{a_p} \frac{4S_{13}L^3}{w^3} \frac{AB + 1}{1 + 4AB + 6AB^2 + 4AB^3 + A^2B^4} \gg 1$$

(4.55)

As the length of the strain sensor and contacting area of the sensor tip to the sample increase and the width and thickness of the strain sensor decrease, the softness of the strain sensor increases much and most of the displacement was transferred to the strain sensor during measurement. The error due to the force at the sensor tip in hard and thin polymer sample is smaller than that in soft and thick polymer sample. Considering that the spring constant $K$ is 24N/m for the strain sensor, the contacting area $A$ is 1mm$^2$, the Young’s modulus $Y_p$ is 6N/mm$^2$ and the thickness $a_p$ is 10um for the polymer sample in our study, the correction factor will be 0.99996 and the strain sensor has a very high accuracy. From this correction factor, we can make the conclusion that this strain sensor can still keep a high accuracy even for polymer sample much softer than PDMS.
4.3 CONCLUSION

A low frequency vibration sensor was fabricated with a MFCs glued on a sheet metal substrate. A new physical model was proposed to calculate the global properties of the MFCs. This model could predict the piezoelectric coefficient of the MFCs very accurately. The FRFs for the output voltage of the vibration sensor were derived from the lumped and distributed parameters’ constituent equations for piezoelectric unimorph with piezoelectric material excited in 3-3 mode using IDT. The output voltage per unit vibration amplitude of the vibration sensor was calculated with the global parameters of the fiber composite substituted into the FRFs. An experiment was carried out to validate the calculation results predicted by the theoretical model. From the experimental results, the output voltage is proportional to the acceleration exerted by the shaker at a given frequency. The output voltage per unit vibration amplitude increases together with the frequency when the frequency is lower than the fundamental resonant frequency. It also keeps constant at a wide frequency range higher than the fundamental resonant frequency when the system has a suitable high damping ratio. The PZT fiber composite is proved by experiment to

Figure 4.26. The displacement error caused by the force from the sensor tip
be a suitable choice for low frequency vibration sensors and works well as a self-standing active device.

A strain sensor was also proposed with this fiber composite unimorph to characterize electric field induced strain response in the out-of-plane direction of soft polymer material sample. It is also suitable for surface morphology and soft material elastic modulus characterization. By changing the substrate material and its relative thickness ratio to the fiber composite, the design of the strain sensor could be optimized for sensitivity or softness improvement. Compared to the original bimorph design, this new design can keep high sensitivity and high flexibility features simultaneously. This newly developed strain sensor worked well over a suitable frequency range. The experiment result was also validated with the calculation and the result from a laser displacement meter. The consistency among three of them indicates that this strain sensor is suitable for strain, elastic modulus and surface morphology measurement with high sensitivity and reliability, especially for soft material with low elastic modulus.
5.0 PZT FIBER COMPOSITE SENSOR FOR MEDICAL APPLICATION

5.1 INTRODUCTION

Hypertension, heart diseases, diabetes, and obesity have seriously threatened human’s healthy life. They are usually caused by dietary habits, lack of exercise, and the daily living stresses of modern society. So daily everyday monitoring of some physiological parameters, including pulse rate, blood pressure and breathing, will help to prevent illnesses and offer valuable information for the diagnosis and treatment of these diseases [115].

Breathing is an important physiological activity to maintain human life, provide oxygen to the body and exhale carbon dioxide. Several physiological problems, such as respiratory diseases, epilepsy, and neuromuscular diseases which may cause respiratory failure, will cause breathing cessation or obstructive apnea, which may eventually develop into a life-threatening condition. And irregular cardiac rhythms and breathing cessation are usually thought to be the causes for sudden infant death syndrome (SIDS or cot death) and sudden adult death syndrome (SADS) [116]. As an illustration of the magnitude of the population affected by breathing apnea, more than 18 million American adults have sleep apnea. In the National Science Foundation (NSF) released 2005 Sleep in America poll, more than one in four respondents (26%) are at risk for sleep apnea, or pauses in breathing during sleep. Sleep apnea is a serious sleep disorder associated with hypertension and stroke. 8% of respondents experienced or had been observed
having pauses in their breathing during sleep at least three nights per week [117]. Therefore it is necessary to detect breathing cessation and introduce medical therapy timely. Breathing airflow monitoring is an effective method to detect and monitor respiratory disorders or cessation [118]. Respiratory rate and depth are also important parameters during respiration. Respiratory rate is the number of breaths taken by a person within a certain amount of time. Respiratory depth can be estimated by the volume of air inhaled or exhaled. Average respiratory rate for a healthy adult at rest usually ranges from 12 to 20 times per minute (0.2-0.33Hz) [119, 120]. And it will arrive 35-45 times for adults during strenuous exercise. With such a slow rate, more accurate records will be acquired by counting the number of breaths over a long time. Clearly, there is an urgent need for suitable breathing sensors which are portable, reliable, and easy for daily use.

Several kinds of technologies and devices have been developed to monitor and measure breathing, such as inductive pneumotachograph, thermistors and thermocouples, oximetry, nasal prongs, and thoraco-abdominal band [121]. Airflow can be sensed by changes of temperature, humidity, component, or sound in breathed air [122]. Thermistors and thermocouples are most ordinary used devices for measuring the temperature change caused by exhalation and inhalation [123]. These devices have the capability to detect total airflow absence such as apneas with a very time-consuming process, and their low sensitivity to respiratory airflow makes quantitative information and detailed diagnosis of breathing disorders impossible [124]. Oximetry technique detects infrared light absorbed by oxygen in blood to predict breathing condition. This method uses signal emitter and receiver powered by outer energy source which is not convenient and power efficient. Nasal prongs and oesophageal manometry pressure sensor sometimes are very uncomfortable and cannot be tolerated by patients [125]. Pneumotachograph needs to combine other recording instrument and is not suitable for routine diagnosis. Electrical impedance
plethysmography measures impedance variations across the chest accompanying with expansion and contraction of the chest provoked by breathing to discover respiration indirectly [126]. The impedance plethysmography signal has strong background noise and is easily to be disturbed by patient movement or change in posture [127]. The last two methods are suitable to be performed in hospital, but are not practical in homecare. A respiratory measurement system is expected to be developed, which is small, portable, comfort, low-cost, home-based, active (without outer energy source), and can monitor breathing quantitatively.

Piezoelectric sensors and actuators have been widely applied to vibration detection and control applications for their simple structures and high energy conversion efficiency. Bimorph or unimorph are typical structures for pressure, impact, acceleration and vibration measurements [128]. Piezoelectric single crystals, piezoelectric ceramics, and polymers are usually chosen for electromechanical sensors and actuators applications. Piezoelectric lead zirconate titanate (PZT) ceramics are commonly used for sensors and transducers due to their high piezoelectric coefficients and large bandwidth. But the brittleness and hardness of bulk PZT piezoelectric ceramics make them difficult to be used on curved, movable, and unstable structure that is subjected to large deformation. Fateful errors in measurement can happen due to brittle fracture. In addition, the mismatch of acoustic impedances makes it less effective to use PZT ceramics device for human physiological activity monitoring. Piezoelectric polymers with high flexibility can keep a steady contact onto the human body [129]. But their low electromechanical coupling coefficient leads to low sensitivity in detecting subtle physiological signals. Two alternative methods have been developed to overcome these disadvantages [92]. One uses thin film deposition of PZT on the substrate [93] and the other uses packaged PZT composites. PZT thin film needs complex technical processes to be integrated on the substrate and has low charge
output. Compared to piezoelectric membrane, piezoelectric composites can be much thicker and generate much more charge. High flexibility can also be expected for PZT composites by choosing appropriate polymer matrix, thus they can be used to develop wearable and comfortable biomedical sensors without disturbing daily activities [130]. Devices made up of piezoelectric composites may provide better sensitivity to detect detailed information with diagnostic value.

Piezoelectric composites usually comprise of one piezoelectric material layer between two soft thin encapsulating layers. 1-3 piezoelectric composites which are most commonly used are composed of piezoelectric ceramic rods embedded in a non-piezoelectric matrix. PZT fiber composites can substantially decouple the lateral effect applied to the sensor synchronously and a large sensitivity can be obtained from the sensor [11]. The benefits of using PZT fiber composites membrane include lower dielectric constant, improved elastic compliance and improved electromechanical coupling coefficient that are well suitable for vibration detection and sensor application. Both $d_{31}$ and $d_{33}$ MFCs transducers have been developed and are currently produced by Smart Material Corp, Sarasota, Florida. This MFCs transducer can also be used as force, strain, pressure, acceleration, acoustics emission sensors and applied to several different fields, including medical diagnosis, physiological monitoring, and so on [131, 132].

5.2 **RECTANGULAR PZT FIBER COMPOSITE BREATHING SENSOR**

5.2.1 **Theoretical derivation**

In this study, a fiber composite breathing sensor was fabricated and experimentally studied for monitoring respiratory rate and depth under different physiological conditions. Firstly, the
constitutive relation for the 1-3 PZT fiber composite on interdigitated transducer (IDT) electrodes was derived under several mechanical and electric assumptions. And a new physical model was proposed to calculate the material parameters of the fiber composite and validated with mixing rule. The properties of single PZT fiber and epoxy were substituted into this model to acquire the global properties of fiber composites. Then, the physical character of the MFCs was analyzed to assure the feasibility of using the fiber composite to detect low frequency breathing signal. The global parameters of the fiber composite were substituted into piezoelectric equations to obtain the input-output transfer function of the breathing sensor at a specific frequency. Finally, one MFCs sample M2814-P1 as shown in Fig. 5.1 was glued on a breath mask to fabricate a breathing sensor (Fig. 5.2). Breathing signals with different physiological characters were measured, compared and analyzed. The location of the MFCs in the mask and the packaging of the breathing sensor were also investigated to assure the accuracy and sensitivity and to eliminate error and noise of the breathing sensor.

Figure 5.1. The MFCs sample

Figure 5.2. A photograph of the MFCs breathing sensor
A physical model has been derived [109] and will be briefly presented here for the material parameters of the 1-3 PZT fiber composite on interdigitated transducer (IDT) electrodes. The strain and electric field are chosen as the independent coordinates and the composite plate is laid in the y-z plane with the fibers lying along the z axes. The constitutive relations for the composite will give the stress and electric displacement for every point in the plate. The elastic and dielectric constants of the ceramic phase will be distinguished from those of the polymer phase by the superscripts E and S, respectively. The stress, strain, field, and displacement in the different phases will be distinguished by a superscript p for the polymer phase and a superscript c for the ceramic phase in the following expressions.

In the y direction, the two different phases have the same stress value and strain will be replaced by stress as the independent coordinate for expressing essential physics meaning reasonably. The piezoelectric ceramic is poled along the fiber direction. With these approximations, the constitutive relations within the ceramic phase are [9, 94],

\[ T_1^c = \frac{C_{11}^E}{c_{11}^E} S_1^c + \frac{C_{12}^E}{c_{11}^E} S_2^c + \frac{C_{13}^E}{c_{11}^E} S_3^c + \frac{C_{12}^E}{c_{11}^E} S_{31}^c \]

\[ S_2^c = -\frac{C_{12}^E}{c_{11}^E} S_1^c + \frac{1}{c_{11}^E} T_2^c - \frac{C_{13}^E}{c_{11}^E} S_3^c + \frac{C_{31}^E}{c_{11}^E} E_3^c \]

\[ T_3^c = \frac{C_{13}^E}{c_{11}^E} S_1^c + \frac{C_{13}^E}{c_{11}^E} S_2^c + \frac{C_{33}^E}{c_{11}^E} S_3^c + \frac{C_{31}^E}{c_{11}^E} S_{31}^c + \frac{C_{33}^E}{c_{11}^E} E_3^c \]

\[ D_3^c = \frac{C_{11}^E}{c_{11}^E} S_1^c + \frac{C_{31}^E}{c_{11}^E} S_2^c + \frac{C_{33}^E}{c_{11}^E} S_3^c + \frac{C_{31}^E}{c_{11}^E} S_{31}^c + \frac{C_{33}^E S_3^c}{c_{11}^E} E_3^c \]

The strains are the same in ceramic and polymer during longitudinal vibration along the z direction when the composite has such fine spatial scale that stop-band resonances are at much higher frequencies than the longitudinal resonance. The electric fields are also the same in both...
phases for the composite are applied voltage by IDT and equipotential. Along x direction, the composite as a whole moves together and the strains are the same in both phases. The lateral stresses are equal in both phases along y direction. Since the lateral periodicity is sufficiently fine, the effective total stress along x or z direction, total strain along y direction and total electric displacement along z direction can be acquired by averaging the contributions of the constituent phases. The average value is the sum of values in the two phases, where the contribution for each phase is in proportional to the volume fraction of each phase. With these approximations, the constitutive relations for the composite can be written in a matrix format when the combinations for all variables are simultaneously carried out,

\[
\begin{bmatrix}
  \overline{T}_1 \\
  \overline{S}_2 \\
  \overline{T}_3 \\
  \overline{D}_3
\end{bmatrix}
= \nu
\begin{bmatrix}
  T^c_1 \\
  S^c_2 \\
  T^c_3 \\
  D^c_3
\end{bmatrix}
+ (1-\nu)
\begin{bmatrix}
  T^p_1 \\
  S^p_2 \\
  T^p_3 \\
  D^p_3
\end{bmatrix}
= \overline{A}
\begin{bmatrix}
  \overline{S}_1 \\
  \overline{T}_2 \\
  \overline{S}_3 \\
  \overline{E}_3
\end{bmatrix}
\] (5.2)

where \( \nu \) and \((1-\nu)\) are the volume fractions of ceramic and polymer in the composite, \( \overline{A} \) is the combined coefficient matrix of the two phases. Equation (5.2) can be rewritten as,

\[
\begin{bmatrix}
  \overline{T}_1 \\
  \overline{T}_2 \\
  \overline{T}_3 \\
  \overline{D}_3
\end{bmatrix}
= \begin{bmatrix}
  c_{11} & c_{12} & c_{13} & -e_{31} \\
  c_{12} & c_{22} & c_{23} & -e_{32} \\
  c_{13} & c_{23} & c_{33} & -e_{33} \\
  e_{31} & e_{32} & e_{33} & E_{33}
\end{bmatrix}
A
\begin{bmatrix}
  \overline{S}_1 \\
  \overline{S}_2 \\
  \overline{S}_3 \\
  \overline{E}_3
\end{bmatrix}
\] (5.3)

\[
\begin{aligned}
\overline{c}_{11} &= (1-\nu)c_{11} + \nu c_{11}^E - \frac{\nu(1-\nu)(c_{12}^E - c_{12})^2}{(1-\nu)c_{11}^E + \nu c_{11}} \\
\overline{c}_{12} &= \frac{(1-\nu)c_{12}c_{11}^E + \nu c_{12}c_{11}}{(1-\nu)c_{11}^E + \nu c_{11}} \\
\overline{c}_{13} &= (1-\nu)c_{12} + \nu c_{12}^E - \frac{\nu(1-\nu)(c_{12}^E - c_{12})(c_{13} - c_{13}^E)}{(1-\nu)c_{11}^E + \nu c_{11}}
\end{aligned}
\] (5.4a, 5.4b, 5.4c)
\[-c_{22} = \frac{c_{11}c_{11}^E}{(1-\nu)c_{11}^E + \nu c_{11}} \quad (5.4d)\]

\[-c_{23} = \frac{(1-\nu)c_{12}c_{11}^E + \nu c_{13}c_{11}}{(1-\nu)c_{11}^E + \nu c_{11}} \quad (5.4e)\]

\[-c_{33} = (1-\nu)c_{11} + \nu c_{33}^E - \frac{\nu(1-\nu)(c_{12} - c_{13}^E)^2}{(1-\nu)c_{11}^E + \nu c_{11}} \quad (5.4f)\]

\[-e_{31} = \nu(e_{31} + \frac{e_{31}(1-\nu)(c_{12} - c_{12}^E)}{(1-\nu)c_{11}^E + \nu c_{11}}) \quad (5.4g)\]

\[-e_{32} = \nu c_{32} \quad (5.4h)\]

\[-e_{33} = \nu(e_{33} + \frac{(1-\nu)(c_{12} - c_{13}^E)e_{31}}{(1-\nu)c_{11}^E + \nu c_{11}}) \quad (5.4i)\]

\[-\varepsilon_{33} = (1-\nu)e_{11} + \nu \varepsilon_{33}^E + \frac{e_{31}e_{31}(1-\nu)}{(1-\nu)c_{11}^E + \nu c_{11}} \quad (5.4j)\]

The composite's material parameters are given in expressions (5.4) in terms of the material parameters of the constituent phases and their proportions. The ratios of the equivalent elastic stiffness coefficient in 1 and 3 directions over the original elastic stiffness coefficient change with PZT fiber volume fraction were shown in Fig. 5.3. The ratios of the equivalent piezoelectric coefficient in 1 and 3 directions over the original piezoelectric coefficient change with fibers’ volume fraction were shown in Fig. 5.4.
The PZT fiber composite sample used for the fabrication of breath sensor includes 34 PZT fibers and the volume fraction \( \nu \) of the PZT fibers is nearly 0.51 by estimation. Unlike the piezo-fibers in Active-Fiber Composites (AFCs), the piezo-fibers in MFCs have rectangular cross section, which increases the electrode contact and capacitance of the MFCs compared to AFCs. Elastic stiffness, piezoelectric and dielectric constants of single PZT fiber and epoxy (the polymer phase) were cited from the data given in references [92, 94] and are listed in Table 5.1. The geometrical data of single PZT fiber and the PZT fiber composite are listed in Table 5.2. The distance between IDT electrodes is 0.4mm, which is twice the thickness of the fibers. So the x and y components of the electric fields can nearly be thought to be zero for the longitudinal vibration modeling. Using these coefficients and geometrical data, the global properties of the PZT fiber composite can be calculated from Eq. (5.4) and the results are listed in Table 5.1.
piezoelectric strain coefficient $d_{33}$ and elastic modulus $E$ of the fiber composite are listed in Table 5.3, which will be used for performance estimation of the breath sensor. The calculated piezoelectric strain coefficient matches with data provided by the vendor, and the calculated Young’s modulus and Poisson’s ratio also agree well with the values provided by the company.

Table 5.1. Composite component and global material properties

<table>
<thead>
<tr>
<th>Material</th>
<th>$c_{11}^E (10^{10} \text{N/m}^2)$</th>
<th>12.7</th>
<th>Fiber composite</th>
<th>$c_{11} (10^{10} \text{N/m}^2)$</th>
<th>4.29</th>
</tr>
</thead>
<tbody>
<tr>
<td>PZT 5H fiber</td>
<td>$c_{11}^E (10^{10} \text{N/m}^2)$</td>
<td>8.0</td>
<td>$c_{12} (10^{10} \text{N/m}^2)$</td>
<td>0.47</td>
<td></td>
</tr>
<tr>
<td></td>
<td>$c_{12} (10^{10} \text{N/m}^2)$</td>
<td>8.5</td>
<td>$c_{13} (10^{10} \text{N/m}^2)$</td>
<td>1.96</td>
<td></td>
</tr>
<tr>
<td></td>
<td>$c_{33} (10^{10} \text{N/m}^2)$</td>
<td>11.7</td>
<td>$c_{22} (10^{10} \text{N/m}^2)$</td>
<td>0.58</td>
<td></td>
</tr>
<tr>
<td></td>
<td>$e_{31} (\text{C/m}^2)$</td>
<td>-4.4</td>
<td>$e_{23} (10^{10} \text{N/m}^2)$</td>
<td>0.48</td>
<td></td>
</tr>
<tr>
<td></td>
<td>$e_{33} (\text{C/m}^2)$</td>
<td>15.5</td>
<td>$e_{33} (10^{10} \text{N/m}^2)$</td>
<td>3.47</td>
<td></td>
</tr>
<tr>
<td></td>
<td>$\varepsilon_{33}/\varepsilon_0$</td>
<td>1400</td>
<td>$\varepsilon_{33}/\varepsilon_0$</td>
<td>-0.91</td>
<td></td>
</tr>
</tbody>
</table>

Table 5.2. Geometric properties of PZT fiber, MFCs and sheet metal substrate

<table>
<thead>
<tr>
<th>Materials</th>
<th>Length (mm)</th>
<th>Width (mm)</th>
<th>Thickness (mm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>PZT fiber</td>
<td>28</td>
<td>0.35</td>
<td>0.18</td>
</tr>
<tr>
<td>MFCs</td>
<td>28</td>
<td>14</td>
<td>0.30</td>
</tr>
<tr>
<td>Steel</td>
<td>28</td>
<td>14</td>
<td>0.117</td>
</tr>
<tr>
<td>Brass</td>
<td>28</td>
<td>14</td>
<td>0.156</td>
</tr>
<tr>
<td>Aluminum</td>
<td>28</td>
<td>14</td>
<td>0.198</td>
</tr>
<tr>
<td>Polyimide</td>
<td>28</td>
<td>14</td>
<td>0.906</td>
</tr>
</tbody>
</table>

Table 5.3. MFCs and sheet metal substrate material properties

<table>
<thead>
<tr>
<th>Materials</th>
<th>$E (10^{10} \text{N/m}^2)$</th>
<th>$\rho (\text{kg/m}^3)$</th>
<th>$\varepsilon_{33}/\varepsilon_0$</th>
</tr>
</thead>
<tbody>
<tr>
<td>MFCs (calculation)</td>
<td>3.47</td>
<td>4250</td>
<td>717</td>
</tr>
<tr>
<td>MFCs (standard)</td>
<td>3.03</td>
<td>(Not provided)</td>
<td>400 (Not provided)</td>
</tr>
<tr>
<td>Steel</td>
<td>20</td>
<td>7800</td>
<td></td>
</tr>
<tr>
<td>Brass</td>
<td>11</td>
<td>8500</td>
<td></td>
</tr>
<tr>
<td>Aluminum</td>
<td>7</td>
<td>2700</td>
<td></td>
</tr>
<tr>
<td>Polyimide</td>
<td>0.32</td>
<td>1430</td>
<td></td>
</tr>
</tbody>
</table>

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The MFCs provided by Smart Material Corp were poled along the length direction with IDT electrodes. It was bonded on a thin metal substrate and glued on a breath mask using epoxy to form a cantilevered breathing sensor. The sheet metal substrate with a suitable thickness was chosen to make the neutral plane of the unimorph locate in the substrate material. The piezoelectric PZT fibers would experience compression or elongation when excited by periodic air caused by breath, thus electrical output signal will record the breath signal patterns.

The equivalent circuit for the fiber composite is shown in Fig. 5.5, which consists of a leakage resistance $R_p$ and a dielectric capacitance $C_p$ of the piezoelectric material. The breathing sensor should not only generate sufficient amount of charge under applied pressure, but also maintain the charge for an enough long time to be measured by an instrument. The charge maintained time length is proportional to the time constant $\tau = R_p C_p$. Using $R_p = \rho h_p / A$ and $C_p = \varepsilon A / h_p$ for a piezoelectric device with resistivity $\rho$, dielectric permittivity $\varepsilon$, thickness $h_p$, and area $A$, the time constant changes to $\tau = \rho \varepsilon$. Thus the piezoelectric material’s properties determine the time constant. The lower frequency limit ($f_{LL}$) of a piezoelectric device is inversely proportional to the time constant $f_{LL} = 1/2 \pi R_p C_p$. The signal amplitude reduces to 70% and there is a 45° phase shift between input and output signals at this frequency limit. The amplitude error and phase shift are not acceptable below $f_{LL}$ for measuring the physical parameters. The time constant for the fiber composite sample is 769s in our study. The large time constant of the MFCs caused by high impedance of the PZT fiber is desirable for the MFCs to be used to measure the low frequency breathing signal.
As was shown in Fig. 5.6, one end of the breathing sensor is fixed on plastic frame of the breath mask and the other end is free to move. The pressure generated by human respiration acts on the sensor surface and stretches and compresses the PZT fibers in the MFCs to generate charge by piezoelectric effect. A simple mass-spring-damper structure can be used to model the dynamic behavior of the breathing sensor, in which the mass $M$ of the device is restrained by a damper $D$ and spring $K$ as shown in Fig. 5.7. If a breathing airflow with force $F$ acts on the breathing sensor, which has a natural frequency $\omega_n = \sqrt{K/M}$, a vibration frequency $s = j\omega$, a damping ratio $\zeta = D/2\sqrt{KM}$, and a time constant $\tau = R_p C_p$, the instantaneous open-circuit voltage in frequency domain can be expressed as [95],

$$V(s) = \frac{K_q}{C_p K} \frac{\omega_n^2}{s^2 + 2\zeta \omega_n s + \omega_n^2} \frac{\tau s}{\tau s + 1} F$$  \hspace{1cm} (5.5)$$

where $K_q$ is the charge generated per unit tip displacement, $C_p$ is the capacitance of the piezoelectric unimorph, $K$ is the spring constant. The force $F$ is proportional to the pressure induced by the breathing airflow,

$$F = P \cdot S$$  \hspace{1cm} (5.6)$$

where $S$ is the effective area of the breathing sensor with airflow pressure acting on. The output voltage can be related to the input pressure as,
\[
\frac{V(s)}{P} = \frac{K_a}{C_p K} \frac{\omega_n^2 s}{s^2 + 2\zeta \omega_n s + \omega_n^2} s + 1 S
\]  
(5.7)

The frequency response of the output voltage for the breathing sensor can be calculated with different damping ratios and time constants. The frequency response of the magnitude X of the output voltage divided by the input pressure with different damping ratios was shown in Fig. 5.8.

**Figure 5.6.** The schematic of the breathing sensor

**Figure 5.7.** A simple mass-spring-damper structure for the breathing sensor

**Figure 5.8.** The frequency response of the magnitude X of the output voltage divided by the input breathing pressure with different damping ratios
The expressions for the spring constant, the charge generated per unit tip displacement, the capacitance of the piezoelectric unimorph have been derived [109]. And the frequency response functions (FRFs) of this breathing sensor can be calculated by substituting the parameters for the piezoelectric unimorph into the one dimension dynamic model for piezoelectric device. The charge generated per unit tip displacement $K_q$ is,

$$
K_q = \frac{3nd_{33} t_p^2 w}{4s_{11}^m L^2} \frac{B(B+1)}{AB+1}
$$

(5.8)

The capacitance of the piezoelectric unimorph bender is

$$
C_p = n^2 w t_p \frac{\varepsilon_{33}^m}{L} (1-k_{33}^2) \frac{AB(1+AB^3)}{1+4AB+6AB^2+4AB^3+A^2B^4}
$$

(5.9)

The spring constant $K$ is

$$
K = \frac{w t_p^3}{4s_{33}^p L^2} \frac{1+4AB+6AB^2+4AB^3+A^2B^4}{AB+1}
$$

(5.10)

The voltage generation coefficient can then be obtained,

$$
\frac{K_q}{C_p K} = \frac{3d_{33}^p L^2}{n^2 \varepsilon_{33}^m w t_p^2} \frac{AB(B+1)}{(1+4AB+6AB^2+4AB^3+A^2B^4)-k_{33}^2 AB(1+AB^3)}
$$

(5.11)

where $A = \frac{s_{33}^p}{s_{11}^m} = \frac{E_m}{E_p}$, $B = t_m/t_p$, the subscript $p$ denotes the upper piezoelectric material layer and subscript $m$ denotes the lower elastic metal layer; $s_{11}^m$ and $s_{33}^p$ are the elastic compliance of the elastic layer and the piezoelectric layer; $t_m$ and $t_p$ are the thickness of elastic layer and piezoelectric layer; $d_{33}$ and $\varepsilon_{33}$ are the piezoelectric constant and dielectric constant of the piezoelectric material, $L$ and $w$ are the length and width of unimorph, $k_{33}$ is the electromechanical coupling coefficient of the piezoelectric material in 33 mode, $n$ is the capacitor number between every anode and cathode of the IDT and it is 56 in the sample.
Compared to the 3-1 mode unimorph, the low electromechanical coupling mode is changed to 3-3 mode with increased piezoelectric coefficient in the numerator part, negatively increased electromechanical coupling coefficient in the denominator part, parameter second-order proportional to the $L/t_p$. And if PZT fiber composite is used as the piezoelectric material, the dielectric constant in the denominator part will also decrease much. All these factors will increase the voltage generation coefficient of the device and high sensitivity is expected for the PZT fiber composite breathing sensor.

By choosing appropriate device dimension and the elastic substrate material, the quantities related to the thickness ratio and Young’s modulus ratio could be optimized. Steel, brass, aluminum, and polyimide were chosen as substrate materials. The dimension parameters and material properties for the fiber composite and substrate materials used in our study were listed in Table 5.2 and Table 5.3. The elastic stiffness coefficient ratios $A$ for steel, brass, aluminum and polyimide substrates were 6.67, 3.67, 2.33, and 0.11 respectively. To locate the neutral plane position of the unimorph in the substrate material, $B$ should be larger than 0.39, 0.52, 0.66, and 3.02 respectively. The voltage generation coefficients of the breathing sensors with different substrate materials versus the thickness ratio $B$ were shown in Fig. 5.9. The voltage sensitivities of the breathing sensors with metal substrates increase and later decrease quickly as thickness ratio $B$ increases. The voltage sensitivity for the breathing sensor with polyimide substrate increases and later decreases slowly as thickness ratio $B$ increases. At some specific thickness ratios, the unimorph with different substrates can have the same sensitivity. The unimorph with steel substrate has the highest sensitivity with a suitable thickness ratio $B$. 
Figure 5.9. The voltage generation coefficients versus the thickness ratio $B$ for the breathing sensors with different substrate materials

The fundamental bending frequency of a piezoelectric unimorph is given by [97],

$$\omega_n = \frac{3.52 t_p}{2L^2} \sqrt{\frac{E_p}{3\rho_p} \left[ 1 + 4AB + 6AB^2 + 4AB^3 + A^2B^4 \right]}^{1/2}$$

(5.12)

where $C$ is the density ratio $\rho_n / \rho_p$ of the elastic layer and the piezoelectric layer.

5.2.2 Experiment

One experiment was carried out to investigate the performance of MFCs breathing sensor under different physiological conditions. The block diagram of the respiration measurement system was shown in Fig. 5.10. Respiratory pressure deflected the breathing sensor and the voltage signal generated was fed into a dual mode amplifier (kistler, type 5010) to convert the high impedance charge input ($q$) into a voltage output. The output voltage from the charge amplifier was transferred to the computer by a GPIB controller (National Instrument) and recorded by a short LabVIEW program. The input insulation resistance of the dual mode amplifier was $10^{14} \Omega$. With the dimension parameters and resistivity ($10^{11} \Omega \cdot m$) of the PZT fibers, the resistance of the
PZT fiber composite was $3 \times 10^{11} \Omega$ by calculation which was much smaller than the amplifier input insulation resistance. The charge mode of the dual mode amplifier is suitable for the PZT fiber composite output voltage measurement. Long time constant was selected in a quasistatic mode for measuring low frequency breathing signal. The transducer sensitivity was set to 100pC/MU and the scale 50MU/V was used. 5000pC charge can generate 1V output voltage in the experiment. The capacitance of the PZT fiber composite was 22pF measured by an impedance analyzer (Agilent 4294A). So the voltage relation is that 227V output voltage of the fiber composite will generate 1V output voltage from the charge amplifier.

![Figure 5.10](image.png)

**Figure 5.10.** The block diagram of the respiration measurement system

Two graduate students in the Lab voluntarily participated in the breathing sensor test. Their normal breathing signals (rate and depth) were recorded and compared in Fig. 5.11. Person A had 12.5 breaths per minute and the peak to peak voltage from the charge amplifier was 1.75 V. Person B had 15 breaths per minute and the peak to peak voltage from the charge amplifier was 2 V. The breathing frequency was much lower than the resonance frequency of the sensor which was 301 Hz by calculation. The frequency accuracy of this breathing sensor was validated by comparing the breathing cycle’s number (12.5, 15) with data (12-20) from other literature [119, 120]. Person A is very thin and keeps doing exercise regularly. Person B is also very thin but seldom takes any exercise. If background information is combined to be considered, this breathing sensor can predict actual physiological status accurately. Normal and fast breathing
signals for person A were recorded and compared in Fig. 5.12. Fast breathing signal was recorded 5 minutes after a long-distance running for person A. It included 29 breaths per minute and the peak to peak voltage from the charge amplifier was 3V. The maximum expiratory pressure will generate a 1.5V output voltage from the charge amplifier. The output voltage of the PZT fiber composite is 340V from the voltage relation. From Eq. (5.11) and Fig. 5.9, the force generated by expiratory pressure is 0.75N. If the effective area of the breathing airflow is assumed to be 1cm², the expiratory pressure is 7.5×10³ Pa which equals to 75cm water. The same expiratory pressure was measured by a U-shaped tube filled with water, and it was 67cm water in the experiment. From the expiratory pressures measured by the two different ways, this breathing sensor was proved to have high accuracy and could predict breathing pressure quantitatively. The reliability of this breathing sensor was also validated and the output voltage was compatible after 100 times operation.

![Figure 5.11. Normal breathing signals comparison for different persons](image)

![Figure 5.12. Normal and fast breathing signals comparison for the same person](image)
5.2.3 Discussion

The location of the MFCs in the breath mask will affect the sensitivity and accuracy of the output signal patterns significantly. For better sensitivity and repeatable monitoring results, it is desirable that the breathing signal only comes from nose and will not be superposed by the signal from mouth breathing. In addition, the MFCs sensor should be well positioned for effective coupling between the breathing airflow and mechanical deflection of the device. This also requires that the surface of the MFCs breathing sensor is perpendicular to the breathing airflow direction. Breathing airflow can be restricted only from nose just with mouse closed.

The packaging of the breathing sensor is also an important factor to determine the final measurement result. Suitable packaging can acquire most of the signal and eliminate noise and error. Leakage of breathing airflow may happen in the cotton part of the mask. Plastic thin film was glued onto the inside surface of the mask to seal it and avoid leakage. Three noise sources, such as environment, internal, and sensor, should be considered in sensor design. Airflows from environment may act on the sensor surface and disturb the breathing signal. The mask contains a plastic cover in front of the MFCs to avoid them. Pyroelectric or thermoelectric effects of the piezoelectric material caused by temperature variations may also generate noise signal to the output voltage. Constant temperature was kept during measurement. Other physiological signals, such as sphygmus, heart-beat, may excite vibration signal which will transmit across the body to the sensor. The cotton part of the breath mask can isolate these signals from the MFCs and retain the breathing signal acting on the MFCs. MOS-FET of the charge amplifier has a leakage current lower than $\pm 0.03$ pC/s which will cause nearly a $\pm 3$ mV/s signal drift. The maximum drift in one minute time range is 0.18V which is much smaller to the output voltage. Low noise cable was
used to connect the breathing sensor to the charge amplifier to avoid triboelectric effect. The sensor was fixed during measurement to eliminate vibration influence.

5.3 ANNULAR PZT FIBER COMPOSITE BREATHING SENSOR

5.3.1 Theoretical derivation

In this study, an annular structure PZT fiber composite was fabricated with PZT fibers and polyimide thin film as shown in Fig. 5.13. It was glued onto a mask and utilized as a breathing sensor to monitor respiratory rate and depth under different physiological conditions as shown in Fig. 5.14. The global properties of the PZT fiber composite were predicted with mixing rule and the composite was assumed to be a piece of homogeneous piezoelectric thin film. The inner radius deflection and output voltage relation of this breathing sensor was derived with polar coordinate piezoelectric constitutive equations. The breathing pressure was replaced by an equivalent concentrated force. Then the relation between the force and the inner radius deflection for this breathing sensor was derived for the final input-output transfer function of the breathing pressure and the output voltage. Breathing signals under different physiological characters were measured, compared and analyzed. The packaging of the breathing sensor was emphasized to assure the accuracy and sensitivity of the output signal and several technical details were considered and modified to eliminate error and lower noise. The performances of this axisymmetric annular configuration were compared with commercial rectangular MFCs [133] for improvement and industrial batch manufacturing feasibility analysis.
This composite sample includes 53 PZT fibers and the fibers’ volume fraction $\alpha$ is nearly 0.042 by calculation. Dimension parameters of single PZT fiber, polyimide substrate and the annular IDT electrode as shown in Fig. 5.15 were listed in Table 5.4. The gold IDT electrode was very thin and its thickness was assumed to be zero in our calculation. Material properties of single PZT fiber and polyimide were listed in Table 5.5. The properties of single PZT fiber and polyimide were applied into mixing rule to validate the global properties of the composite. The tensile modulus of $d_{33}$ PZT fiber composite is [92],

$$E_L = \alpha E_L^P + (1 - \alpha) E_L^M$$

(5.13)

The major Poisson’s ratio of $d_{33}$ PZT fiber composite is,

$$\nu_{LT} = \alpha \nu_{L,T}^P + (1 - \alpha) \nu_{L,T}^M$$

(5.14)

The piezoelectric constant of $d_{33}$ PZT fiber composite is,

$$d_{33} = \frac{1}{E_L} (\alpha d_{33}^P E_L^P)$$

(5.15)
The dielectric constant of $d_{33}$ PZT fiber composite is,

$$
\varepsilon_{33}^T = \alpha \varepsilon_{33}^{TP} + (1 - \alpha) \varepsilon_{33}^{TM}
$$

(5.16)

In these expressions, $P$ denotes the piezoelectric material and $M$ denotes the matrix material. $L$ denotes the longitudinal contribution and $T$ denotes the transverse one. The equivalent global parameters for the composite were calculated and listed in Table 5.5. The effective piezoelectric constant was 60% of the calculation result because only 60% volume fraction of the PZT fibers between the IDT fingers was poled and had piezoelectric effect.

Figure 5.15. A photograph of the annular IDT electrode

Table 5.4. Geometric properties of PZT fiber, polyimide substrate and annular IDT electrode

<table>
<thead>
<tr>
<th>Material</th>
<th>Length (mm)</th>
<th>Diameter (mm)</th>
<th>Type</th>
</tr>
</thead>
<tbody>
<tr>
<td>PZT fiber</td>
<td>6</td>
<td>0.1</td>
<td>5H2</td>
</tr>
<tr>
<td>Polyimide</td>
<td>Inner radius (mm)</td>
<td>Outer radius (mm)</td>
<td>Thickness (mm)</td>
</tr>
<tr>
<td>Polyimide</td>
<td>2</td>
<td>10</td>
<td>0.19</td>
</tr>
<tr>
<td>Gold IDT</td>
<td>Finger wider (mm)</td>
<td>Finger space (mm)</td>
<td>Covering angle (º)</td>
</tr>
<tr>
<td>Gold IDT</td>
<td>0.2</td>
<td>0.3</td>
<td>324</td>
</tr>
</tbody>
</table>

Table 5.5. Single PZT fiber, polyimide and composite material properties

<table>
<thead>
<tr>
<th>Materials</th>
<th>E ($10^{10}$ N/m$^2$)</th>
<th>Poisson’s ratio</th>
<th>$d_{33}$ ($10^{-12}$ m/V)</th>
<th>$\varepsilon_{33}^T/\varepsilon_o$</th>
</tr>
</thead>
<tbody>
<tr>
<td>PZT fiber</td>
<td>6.2</td>
<td>0.3</td>
<td>400</td>
<td>2200</td>
</tr>
<tr>
<td>Polyimide</td>
<td>0.32</td>
<td>0.34</td>
<td>0</td>
<td>3.5</td>
</tr>
<tr>
<td>Composite</td>
<td>0.57</td>
<td>0.34</td>
<td>110(effective)</td>
<td>95.8</td>
</tr>
</tbody>
</table>
The annular PZT fiber composite was poled on one side along radius direction by an annular IDT electrode. The outer edge of it was clamped to the mask and the inner edge of it was free to move up and down without any twisting and tilt. The pressure generated from human respiration acted vertically on the sensor surface and deflected it. The deflection stretched and compressed the PZT fibers and generated charge by piezoelectric effect. The pressure was assumed to distribute uniformly along the inner edge which was then replaced by an equivalent concentrated load applied to the center of the sample in the modeling. A schematic configuration of the breathing sensor was illustrated in Fig. 5.16. The same equivalent circuit and the mass-spring-damper structure can also be used to model this annular breathing sensor.

![Schematic Configuration of the Annular Breathing Sensor](image)

**Figure 5.16.** A schematic configuration of the annular breathing sensor: (a) A lateral view with uniform breathing pressure, (b) A lateral view with an equivalent concentrated force

To determine the flexural mode of the annular piezoelectric structure, several assumptions were made to simplify the analytical solution [134]. (a) The composite thickness is much larger than the flexural deflection. The stress and the strain along the z-axis are equal to zero inside the composite. (b) The composites vibrate in a small range and the neutral plane never changes during vibration. The surfaces normal to the neutral plane before the flexion remain to keep vertical to this plane after bending [135-137]. (c) The flexural deflection in z
direction only depends upon the radius and time. (d) The flexural deflection is continuous between different material phases which are glued together. The strains \( S_r \) and \( S_\theta \) are the same for different material phases and other strain components are equal to zero. The radius displacement \( \mu \) and the electric voltage \( V \) were chosen as the mechanical and electric variables to derive the mechanical response owing to a prescribed time-dependent electric input [138]. An impulsive type input was chosen as a representative and the annular ring was assumed to be open-circuited. The piezoelectric constitutive equations in the polar coordinate are,

\[
T_r = C_{11} \frac{d\mu}{dr} + C_{12} \frac{\mu}{r} - hD_r
\]

(5.17)

\[
T_\theta = C_{12} \frac{d\mu}{dr} + C_{11} \frac{\mu}{r} - hD_r
\]

(5.18)

\[
E_r = -h\left(\frac{d\mu}{dr} - \frac{\mu}{r}\right) + \frac{D_r}{\varepsilon}
\]

(5.19)

where \( (T_r, T_\theta) \) are the radial and tangential direction components of stress, \( (C_{11}, C_{12}) \) are the normal and shear elastic stiffness, \( (D_r, E_r) \) are the radius direction components of the electric displacement \( D \) and the electric field intensity \( E \), \( h \) is the piezoelectric constant and \( \varepsilon \) is the permittivity.

The equation of motion of the annular disk in the radial direction can be expressed as,

\[
\frac{\partial T_r}{\partial r} + \frac{T_r - T_\theta}{r} = \rho \frac{\partial^2 \mu}{\partial t^2}
\]

(5.20)

Using equations (5.17) and (5.18), equation (5.20) changes to

\[
\frac{\partial^2 \mu}{\partial r^2} + \frac{1}{r} \frac{\partial \mu}{\partial r} - \frac{\mu}{r^2} - \frac{h}{C_{11}} \frac{\partial D_r}{\partial r} = \frac{\rho}{C_{11}} \frac{\partial^2 \mu}{\partial t^2}
\]

(5.21)

The free electric charge density is zero in the composite. From Gauss’s law, we get

\[
\text{div} D = 0
\]

(5.22)
In polar coordinate, equation (5.22) changes to

$$\frac{\partial D_r}{\partial r} + \frac{1}{r} \frac{\partial D_\theta}{\partial \theta} = 0 \tag{5.23}$$

The electric field is in radius direction and the electric displacement never varies in tangential direction,

$$\frac{\partial D_r}{\partial r} = 0 \tag{5.24}$$

Combining equations (5.21) and (5.24) together, we get

$$\frac{\partial^2 \mu}{\partial r^2} + \frac{1}{r} \frac{\partial \mu}{\partial r} - \frac{\mu}{r^2} = \frac{1}{v^2} \frac{\partial^2 \mu}{\partial t^2}$$

$$v = (C_{11} / \rho)^{1/2} \tag{5.26}$$

Laplace transform is used to solve equation (5.25) to acquire the mechanical response and input voltage relation. If $\overline{\mu}$ is the Laplace transform (of parameter $p$) of $\mu$,.

$$\overline{\mu}(r, p) = \int_0^\infty \mu(r, t)e^{-pt} dt \quad (p > 0) \tag{5.27}$$

Taking the Laplace transform of (5.25), we get

$$\frac{d^2 \overline{\mu}}{dr^2} + \frac{1}{r} \frac{d \overline{\mu}}{dr} - \frac{p^2}{v^2} + \frac{1}{r^2} \overline{\mu} = 0 \tag{5.28}$$

$$\overline{\mu} = AI_1\left(\frac{pr}{v}\right) + BK_1\left(\frac{pr}{v}\right) \tag{5.29}$$

where $I_1$ and $K_1$ are first order modified Bessel functions of the first and second kind, $A$ and $B$ are constants to be determined from boundary conditions. Taking the Laplace transform of (5.19),

$$\overline{E_r} = -h\left(\frac{d \overline{\mu}}{dr} - \frac{\overline{\mu}}{r}\right) + \frac{\overline{D_r}}{\varepsilon} \tag{5.30}$$
For the annular ring is open-circuited, the surface charge $\vec{Q}$ is zero and $D_i$ generated from $\vec{Q}$ is also zero. If potentials between all IDT electrode pairs are added together, the total potential $\bar{V}$

$$
\bar{V} = \int_{r_1}^{r_2} E_r \, dr = -h[(\vec{\mu})_{r=r_2} - (\vec{\mu})_{r=r_1}] + h \int_{r_1}^{r_2} \frac{\vec{\mu}}{r} \, dr \tag{5.31}
$$

where $r_1$, $r_2$ are the inner and outer radiuses of the ring. Submitting (5.29) into (5.31),

$$
\bar{V} = -h[A[I_1(\frac{pr_2}{\nu}) - I_1(\frac{pr_1}{\nu})] + B[K_1(\frac{pr_2}{\nu}) - K_1(\frac{pr_1}{\nu})]]
$$

$$
+ h \int_{r_1}^{r_2} \{A \frac{I_1(pr/v)}{r} + B \frac{K_1(pr/v)}{r}\} \, dr \tag{5.32}
$$

The impulsive voltage introduced to the annular ring is

$$
V = V_0 \delta(t) \tag{5.33}
$$

where $\delta(t)$ is the Dirac’s delta function. For the Laplace transform of delta-function is unity,

$$
\bar{V} = V_0 \tag{5.34}
$$

For the outer edge of the annular ring is rigidly fixed,

$$
(\vec{\mu})_{r=r_2} = 0 \tag{5.35}
$$

If boundary conditions (5.34) and (5.35) are substituted into equations (5.29) and (5.32),

$$
Aa_{11} + Ba_{12} = V_0 \tag{5.36}
$$

$$
AI_1(\frac{pr_2}{\nu}) + BK_1(\frac{pr_2}{\nu}) = 0 \tag{5.37}
$$

$$
a_{11} = h[I_1(\frac{pr_1}{\nu}) + h \int_{r_1}^{r_2} \frac{I_1(pr/v)}{r} \, dr] \tag{5.38}
$$

$$
a_{12} = h[K_1(\frac{pr_1}{\nu}) + h \int_{r_1}^{r_2} \frac{K_1(pr/v)}{r} \, dr] \tag{5.39}
$$
$A$, $B$ can be solved from equations (5.36) and (5.37),

$$A = V_0 \frac{K_1(pr_2/v)}{a_{11}K_1(pr_2/v) - a_{12}I_1(pr_2/v)}$$  \hspace{1cm} (5.40)

$$B = -V_0 \frac{I_1(pr_2/v)}{a_{11}K_1(pr_2/v) - a_{12}I_1(pr_2/v)}$$  \hspace{1cm} (5.41)

The mechanical displacement $\mu$ corresponding to the impulsive voltage can be derived by using inverse Laplace transform on equation (5.29) with $A$ and $B$ substituted into it. The deflection at the inner edge $r = r_i$ can be expressed as

$$(\mu)_{r=r_i} = V_0 \frac{K_1(pr_2/v)I_1(pr_i/v) - I_1(pr_2/v)K_1(pr_i/v)}{a_{11}K_1(pr_2/v) - a_{12}I_1(pr_2/v)}$$  \hspace{1cm} (5.42)

$$(\mu)_{r=r_i} = \frac{1}{2\pi} \int_{\gamma-i\infty}^{\gamma+i\infty} e^{s}\left[\frac{K_1(pr_2/v)I_1(pr_i/v) - I_1(pr_2/v)K_1(pr_i/v)}{a_{11}K_1(pr_2/v) - a_{12}I_1(pr_2/v)}\right] dp$$  \hspace{1cm} (5.43)

By several steps of calculation [138], the deflection can be expressed as

$$(\mu)_{r=r_i} = \text{Real part of} \sum_{n=1}^{\infty} \frac{ie^{i\alpha_n \nu} (A_n - iB_n) [J_1(\alpha_n r_i)Y_1(\alpha_n r_2) - J_1(\alpha_n r_2)Y_1(\alpha_n r_i)]}{h(A_n^2 + B_n^2)}$$  \hspace{1cm} (5.44)

where $J_1$ and $Y_1$ are first order Bessel functions of the first and second kind, $p = i\alpha_n \nu$, $A_n$ and $B_n$ are complicated expressions including $J_0$, $Y_0$, $J_1$ and $Y_1$. By using the series expansions for $J_1(\alpha_n r)$ and $Y_1(\alpha_n r)$, we can derive the relation between inner edge deflection and input voltage after Laplace transform if square and higher orders expressions of the expansions are neglected when $p$ is small.

$$\left(\overline{\mu}\right)_{r=r_i} \sim \frac{V_0}{h} \frac{(r_i/r_2 - r_2/r_i)}{(r_1/r_2 - r_2/r_1) + (r_2 - r_1)/r_2 - r_2(1/r_1 - 1/r_2)} \sim \frac{V_0}{2h} (1 + r_i/r_2)$$  \hspace{1cm} (5.45)

After taking the inverse Laplace transform, the relation changes to

$$(\mu)_{r=r_i} \sim V_0 (1 + r_i/r_2)\delta(t)/2h$$  \hspace{1cm} (5.46)
If the input signal changes to other waveforms, this deflection and voltage relation still retains validity under small range bending or vibration.

The relation between applied force $F$ and vertical deflection $\mu_z$ at $r = r_i$ can be derived from a series of expressions in references [139],

$$F = \frac{4\pi Et^4}{r_2^3[3(1-\nu^2)]^{3/2}} (\gamma_1 \mu_z + \gamma_3 \mu_z^3 + \cdots)$$  \hspace{1cm} (5.47)

where $t$ is the thickness of the ring, $\gamma_1$ and $\gamma_3$ are constants. Under small range bending,

$$\gamma_1 = \frac{1 - r_i / r_2}{(1 - r_i / r_2)^2 - (r_i / r_2)(\log(r_i / r_2))^2}$$  \hspace{1cm} (5.48)

$$\gamma_3(r_2) = \frac{d\gamma_3(r_2)}{dr} = \gamma_3(r_1) = \frac{d\gamma_3(r_1)}{dr} = 0$$  \hspace{1cm} (5.49)

So high order expressions of $\mu_z$ in equation (5.47) can be neglected. The relation between vertical deflection $\mu_z$ and radius deflection $\mu$ is

$$\mu_z = \sqrt{3(1-\nu^2)} \frac{\mu}{t} \bigg|_{r=r_i} $$  \hspace{1cm} (5.50)

Combining equations (5.46), (5.47), (5.50) and the annular ring area expression, the respiration pressure and output voltage relation of the annular PZT fiber composite breathing sensor is

$$\frac{V}{P} = \frac{3r_2^2(1-\nu^2)h}{2Et^3} [(r_2 - r_i)^2 - (r_i r_2)(\log(r_i / r_2))^2]$$  \hspace{1cm} (5.51)

If the piezoelectric coefficient $h$ is changed to $d_{33}$, equation (5.51) will change to

$$\frac{V}{P} = \frac{3(1-\nu^2)d_{33} r_2^4}{2\epsilon t^3} [(1 - r_i / r_2)^2 - (r_i / r_2)(\log(r_i / r_2))^2]$$  \hspace{1cm} (5.52)

The sensitivity of the breathing sensor is proportional to the biquadratic of the composite outer radius $r_2$ and inversely proportional to the cubic of the composite thickness $t$. But the breathing pressure usually focuses on a small area which sets a upper limit for $r_2$. The sensitivity
change with the inner radius to outer radius ratio was shown in Fig. 5.17. If the outer radius is set to a unit length, the sensitivity decreases as the inner radius of the annular ring increases. Because the breathing pressure will pass the center hole and has no effect to the output voltage. But a hole in the center is a must to keep the breathing airflow not been blocked. Using equations (5.14-5.16) and the material parameters of the PZT fiber and polyimide listed in table 5.5, the figure of merit \( (1 - \nu^2)d_{33}/\varepsilon \) of the breathing sensor change with the volume fraction \( \alpha \) of the PZT fibers was calculated and shown in Fig. 5.18. 5% PZT fibers in the composite can acquire the maximum figure of merit from the calculation. The sensitivity increases firstly for the piezoelectric coefficient in the numerator part increases together with the volume fraction of the PZT fibers. Then it decreases as more and more PZT fibers are added into the composite for the Young’s modulus and dielectric constant of the composite in the denominator part increase much quicker than the piezoelectric coefficient.

**Figure 5.17.** The sensitivity of the breathing sensor change with the inner radius to outer radius ratio

**Figure 5.18.** The sensitivity of the breathing sensor change with fibers’ volume fraction in the composite
5.3.2 Experiment

One experiment was carried out to investigate the performance of this breathing sensor under different physiological conditions. The block diagram of the respiration measurement system was shown in Fig. 5.19. Respiratory pressure deflected the inner edge of the annular breathing sensor and the voltage output generated from the deflection was fed into a dual mode amplifier (kistler, type 5010) to convert the high impedance charge input \( q \) into a voltage output. The output voltage from the charge amplifier was transferred to the computer by a GPIB controller (National Instrument) and recorded by a short LabVIEW program. The input insulation resistance of the dual mode amplifier was \( 10^{14} \Omega \). With the dimension parameters and resistivity \( (10^{11} \Omega \text{m}) \) of the PZT fibers, the resistance of the PZT fiber composite was \( 4.5 \times 10^{12} \Omega \) by calculation which was much smaller than the amplifier input insulation resistance. The charge mode of the dual mode amplifier is suitable for the PZT fiber composite output voltage measurement. Long time constant was selected in a quasistatic mode for measuring low frequency respiration phenomena. The transducer sensitivity was set to 10pC/MU and the scale 10MU/V was used. 100pC charge can generate 1V output voltage in the experiment. The capacitance of the PZT fiber composite was 3pf measured by an impedance analyzer (Agilent 4294A). So the voltage relation is that 34V output voltage of the fiber composite will generate 1V output voltage from the charge amplifier.

Two graduate students in the Lab voluntarily participated in the breathing sensor test. Their normal breathing signals (rate and depth) were recorded and compared in Fig. 5.20. Person A had 12.5 breaths per minute and the peak to peak voltage from the charge amplifier was 0.18V. Person B had 17 breaths per minute and the peak to peak voltage from the charge amplifier was 0.17V. The frequency accuracy of this breathing sensor was validated by comparing the
breathing cycle number (12.5, 17) with data (12-20) from other literatures [119, 120]. Person A is very thin and keeps doing exercise regularly. Person B is also very thin but seldom takes any exercise. If background information is combined to be considered, this breathing sensor can predict actual physiological status accurately. Normal and fast breathing signals for person A were recorded and compared in Fig. 5.21. Fast breathing signal was recorded 5 minutes after a long-distance running for person A. It included 29 breaths per minute and the peak to peak voltage from the charge amplifier was 1.8V. The maximum expiratory pressure will generate a 0.9V output voltage from the charge amplifier. The output voltage of the PZT fiber composite is 30.6V from the voltage relation. From Eq. (5.52), Fig. 5.17 and Fig. 5.18, the expiratory pressure is 6*10³ Pa by calculation which equals to 60cm water. The same expiratory pressure was measured by a U-shaped tube filled with water, and it was 67cm water in the experiment. From the expiratory pressures measured by the two different ways, this breathing sensor was proved to have high accuracy and could predict breathing pressure quantitatively. The reliability of this breathing sensor was also validated and the output voltage was compatible after 100 times operation.

![Figure 5.19. A block diagram of the respiration measurement system](image-url)

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5.3.3 Discussion

Several comparability and differences can be found from the experiment results of the two breathing sensors [133]. The breathing frequencies measured by them are compatible and both of them can record signal fluctuations accurately. The output voltage of the rectangular sample is 67 times larger than that of the annular one during normal breathing process and 11 times larger during fast breathing process. The effective volume of PZT fibers is 60 mm$^3$ for the rectangular sample and 1.5 mm$^3$ for the annular one. If the PZT fibers inside them are assumed to have the same piezoelectric coefficient, the output voltage of the rectangular sample should be 40 times larger than that of the annular one. So the annular design has 4 times higher efficiency than the
rectangular one. This high efficiency accounts for suitable substrate material in the sample. The rectangular fiber composite is a standard commercial product and its neutral plane locates on the center plane of the PZT fibers. The output voltage generated from stretching effect at one side of the neutral plane during bending counteracts that from compression effect at the other side. A steel substrate was glued onto the fiber composite to change the neutral plane position. The annular sample was fabricated manually with PZT fibers and a polyimide thin film glued together. The film with suitable thickness was chosen to make the neutral plane locate at the polyimide part. Because the fibers in the rectangular sample are much thicker than those in the annular one, polyimide thin films with a small stiffness coefficient are not suitable for changing the neutral plane position of the rectangular sample which will make the sample too thicker to have practical use. The steel substrate with a large stiffness coefficient made the sample vibrate in a small range and generated little charge which caused the low efficiency of the rectangular breathing sensor.

The signal amplitude differences from the two breathing sensors are 67 times during normal breathing condition and 11 times during fast breathing condition. This multiple difference was caused by the configuration differences between them. The rectangular MFCs were fixed to the mask with one end clamped and the other end free. So mouth airflow and nose airflow nearly had the same effect to the final output voltage in any condition and only nose airflow was considered in measurement. The annular PZT fiber composite located at the center of the mask with outer edge clamped and inner edge free. Mouth respiration had much stronger effect than nose respiration during fast breathing which accounted for the 6 times output difference from the two breathing sensors between fast and normal breathing. The wire connection of the annular fiber composite which will introduce noise into the output signal is an
important factor that should be paid more attention to than in the rectangular design. For the rectangular design, the welds connecting the leads and the IDT located at one side of the clamping point where the MFCs were supported and the composite located at the other side. So environment vibration had little or no effect to the MFCs. But for the annular design, both of the welds and the composite were inside of the clamped outer edge and environment disturbance would affect the output signal more obviously. So the two leads of the annular design were glued to the mask to lower the environment disturbance.

Compared to the rectangular design, this annular breathing sensor has several benefits. Small vibration amplitude due to configuration factor makes its output signals more stable. And its surface has a much larger possibility to be perpendicular to the breathing airflow direction. The higher efficiency of this annular design makes it much more useful for actual application. But the annular structure also has two small disadvantages. The fibers were placed manually with a mask as shown in Fig. 5.22 which was a time-cost process. The volume fraction of the PZT fibers in the composite has an upper limit near the outer edge of the annular ring. In industrial batch manufacturing, the fibers can be changed to sector components which will increase the volume fraction and special instrument can be designed to place the PZT material into the composite. This annular design is a promising choice for future medical application.

![Figure 5.22. A photograph of the mask for fixing the PZT fibers](image)
5.4 CONCLUSION

Breathing is an important physiological phenomenon and several methods and instruments can be utilized to detect and monitor breathing signal. Piezoelectric sensor is one of the alternatives for biomedical applications and the PZT fiber composite is chosen as the sensing component in this study. Large electromechanical coupling coefficient of single PZT fiber and high flexibility of polyimide make the PZT fiber composite become a suitable choice for physiological activities monitoring. A breathing sensor was fabricated with a piece of MFCs unimorph glued onto an ordinary mask. The MFCs global properties were calculated by substituting the properties of single PZT fiber and epoxy into mixing rule and validated with the data from technical manual. The MFCs are suitable for exploring low frequency breathing signal for its small lower frequency limit and large time constant. Constitutive relations for piezoelectric unimorph and one dimension dynamic model for piezoelectric device were used to derive the relation between output voltage of the sensor and breathing airflow pressure. Three experiments were carried out to compare breathing signals under different physiological conditions. Several fabrication, packaging, and instrument details were considered to improve the accuracy and sensitivity and to lower error and noise of this breathing sensor. The annular PZT fiber composite was fabricated with PZT fibers glued onto polyimide thin film and the composite was glued onto a mask to fabricate the breathing sensor. Properties of single PZT fiber and polyimide were characterized to calculate the global properties of the composite by mixing rule. Then the composite was assumed to be a piece of homogeneous annular piezoelectric plate and polar coordinate piezoelectric constitutive equations were utilized to derive the inner edge deflection and output voltage relation of this breathing sensor. The relation between the equivalent concentrated force for the breathing pressure and the inner radius deflection was derived with plate deflection
expressions to acquire the final breathing pressure-output voltage relation. Experiments were carried out to compare breathing signals under different physiological conditions. This annular structure was also compared with rectangular configuration for performance improvement and industrial batch manufacturing feasibility analysis. These two breathing sensors can be utilized for breathing rate and depth monitoring and breathing diseases precaution and they are nice choices for daily use and diagnostic purpose.
6.0 CONCLUSIONS AND FUTURE WORK

6.1 MAJOR ACCOMPLISHMENTS

The research work in this dissertation is focused on experimental investigation and modeling of piezoelectric and piezoresistive composite sensor. The following is a summary of the major accomplishments.

(1) A novel ZnO nanowires-polymer nanocomposite was fabricated and characterized and its piezoresistive property was utilized to work as a strain sensor.

- Single crystal zinc-oxide nanowires were synthesized through a simple hydrothermal route and subsequently mixed with polyimide matrix to form ZnO nanocomposites film. Superimposed a.c. and d.c. electric fields were applied to microscopically tailor the alignment of ZnO nanowires in polyimide matrix by using IDT to form anisotropic nanocomposites. Polarization-electric field loops of the nanocomposites were measured before and after curing the samples; and the results indicate that net electric polarization in the nanocomposites can be induced by this field-assisted alignment technique due to the intrinsic polar property of ZnO nanowires. The conductivity, dielectric constant and electrical I-V curve of ZnO nanocomposites change with weight ratio of ZnO nanowires were characterized.
A novel ZnO nanowires-polyimide nanocomposite strain sensor was proposed based on the piezoresistive effect of ZnO nanowires. Static piezoresistive effect of the nanocomposite was investigated and large gauge factor was acquired for this nanocomposite. This strain sensor was then utilized to measure the static and dynamic strain in a cantilever beam and the results were verified with calculation and measurement result from laser.

(2) Development of PZT fiber composite low frequency vibration sensor and strain sensor

A low frequency vibration sensor was fabricated and experimentally studied. The constitutive relation for the 1-3 PZT fiber composite on IDT electrodes was derived and a new physical model for the material parameters was presented and validated with mixing rule. The properties of single PZT fiber were characterized and applied into this model to calculate the global properties of PZT fiber composite. The global parameters of the composite were substituted into lumped and distributed parameters’ constituent equations for piezoelectric unimorph to theoretically predict the sensitivity and effective frequency response range of the vibration sensor. The output voltage of the vibration sensor is proportional to input acceleration and the voltage per unit input displacement keeps stable in a wide frequency range with a suitable damping ratio. The PZT fiber composite works on well as a self-standing wireless low frequency vibration sensor and this vibration sensor can reflect vibration amplitude accurately.

A strain sensor was also proposed with this fiber composite unimorph to characterize electric field induced strain response in the out-of-plane direction of soft polymer material sample. It is also suitable for surface morphology and soft material elastic modulus characterization. By changing the substrate material and its relative thickness
ratio to the fiber composite, the design of the strain sensor could be optimized for sensitivity or softness improvement. Compared to the original bimorph design, this new design can keep high sensitivity and high flexibility features simultaneously. This newly developed strain sensor worked well over a suitable frequency range. The experiment result was also validated with the calculation and the result from a laser displacement meter. The consistency among three of them indicates that this strain sensor is suitable for strain, elastic modulus and surface morphology measurement with high sensitivity and reliability, especially for soft material with low elastic modulus.

(3) Theoretical modeling and experimental investigation of two PZT fiber composite breathing sensors with different configurations

- A rectangular breathing sensor and an annular one were fabricated for monitoring breathing rate and depth. Properties of single PZT fiber and polyimide were characterized and global properties for both of the fiber composites were calculated by mixing rule. They are suitable for exploring low frequency breathing signal for their small lower frequency limit and large time constant. Output voltage of the rectangular breathing sensor at a specific frequency was derived with piezoelectric constituent equations and could be utilized to direct sensor design. Polar coordinate piezoelectric constitutive equations and plate deflection expressions were utilized to derive the breathing pressure and output voltage relation of the annular one.

- Both of these two sensors were tested under different physiological conditions. Several fabrication, packaging, and instrument details were considered to improve the accuracy and sensitivity and to lower error and noise of the breathing sensors. The annular design has also been compared with the rectangular one for performance improvement and
industrial batch manufacturing feasibility analysis. Both of them are excellent for monitoring breathing rate and depth and nice choices for daily use and diagnose purpose.

6.2 FUTURE WORK

Heartbeat monitoring is important in daily life of human. Sleep heartbeat monitoring [140] and fetal heartbeat monitoring [141] are two important parts which have attracted increasing interest in the past years. Sleep apnea syndrome (SAS) is one of the common sleep disorders and it is of clinical importance to be able to diagnose SAS in early stage. Overnight polysomnography is widely recognized as the gold-standard for sleep research, which simultaneously measures airflow, body movement, electroencephalogram (EEG), electroolfactogram (EOG), electrocardiogram (ECG), and so on [142]. However, the measurement requires attachment of many sensors such as thermistors and electrodes, to patients’ body which may cause patients discomfort. Several methods have been developed to assess physiological information during sleep in non-invasive and unconstrained manners. Visual information measured with cameras was used to achieve in-sleep respiration monitoring [143, 144]. Although these methods need no contact with patients, there are limitations that the measurement systems are costly and not appropriate for public healthcare and at-home medical applications.

Alternative attempts have been made to measure pressure fluctuation induced by heartbeat and respiration during sleep, using air mattresses [145, 146], an under-pillow sensor [147], and pressure sensors [148, 149]. In the pneumatic biomeasurement method [145], human movements act on the air in a mattress, and a supersensitive pressure sensor is used to detect the corresponding air pressure changes. Thin film pressure sensors made of piezoresistive polymer
are attached to the surface of bed, and respiration and posture signals are obtained from the pressure distribution [148]. After the pressure fluctuation due to respiration and heartbeat has been measured, there is another problem that how to extract these components correctly. To this end, traditional methods are usually based on filtering with predefined frequency bands [145, 146]. On the other hand, wavelet transformation (WT) is an alternative approach [147, 149]. All the methods mentioned have their own advantage and disadvantage.

Fetal heart rate (FHR) measurement is one of the most important approaches used for monitoring the cardiac status of fetal human beings. In order to intensify antenatal surveillance, the routine FHR test should be performed with a long-term monitoring device that is portable and easy to use at home. A standard test of fetal health is the fetal nonstress test (NST), performed routinely in hospitals by means of CW Doppler ultrasound. The instrumentation provides a time record of the fetal heart rate, as well as indications of fetal movement, on a strip chart recorder. A normal NST requires three separate FHR accelerations of at least 15 beats per min over its baseline. Each acceleration event is to be stimulated by an associated fetal movement. These three movement/acceleration events are to occur during any 20-min observation window. The availability of a portable instrument would allow the expectant mother to perform the NST in the home comfortably on a daily basis instead of during less frequent and less convenient clinical visits. Furthermore, such testing at home would be more thorough from an obstetrical surveillance point of view. Unfortunately, ultrasonic instrumentation lends itself poorly to portable home use for two reasons: it is expensive and bulky, and it requires accurate sensor alignment which may lie beyond the capability of nonexpert hands.

In addition, a passive acoustic approach, like the one based on the analysis of the fetal heart sounds, where no energy is transmitted to the fetus, should be preferred to invasive
methods as the ultrasound cardiotocography. The acoustical method can be realized using low-power electronic instrumentation [150] and no acoustic energy is transmitted to the body. Some efforts were made and most of them were aimed at the development of sensitive acoustic sensors to improve the signal-to-noise ratio of the fetal heart sound signal. Examples are the inductive-type sensor [151], the cantilever type accelerometer [152], the optical scanning technique [153], and the set of piezoelectric elements [154]. These instruments stimulate the interest of developing a portable instrument based on using piezoelectric material with high piezoelectric coefficient to detect the fetal heart sounds for the long-term monitoring of the fetus.

In this study, we propose a novel heart rate sensor for noninvasive and unconstrained measurement of heartbeat. A flexible PZT composite thin film sensor is used for signal acquisition. Piezoelectric film sensors are utilized in unconstrained cardio-respiratory monitoring, for reasons that these sensors are sensitive and only respond to dynamic change of pressure. Also, thin thickness of these sensors enables that they can be easily attached to bodies, used in daily life, and may not affect the activities. A polyvinylidene fluoride (PVDF) piezopolymer sensor has been developed for unconstrained in sleep cardio-respiratory monitoring [149]. However, one major disadvantage of PVDF material is the difficulty in soldering PVDF to make electric connection. Usually, conductive epoxy or spring clips are used which may then lead to problems of stability and fatigue durability. The piezoelectric sensor used in this study is made of PZT thin film. The PZT thin film is spin-coated with liquid silicon rubber for biomedical compatibility and flexibility improvement. This sensor shows excellent thermal and chemical stability, and this property facilitates a variety of practical applications.
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