CANONICAL CORRELATION ANALYSIS IN CROSS-DOMAIN RECOMMENDATION

by

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Cross-domain recommendation has recently emerged as a hot topic in the field of recommender systems. The idea is to use rating information accumulated in one domain (known as a source or auxiliary domain) to improve the quality of recommendations in another domain (known as a target domain). One of the important problems in cross-domain recommendation is the selection of source domains appropriate for a target domain. Previous works mostly assume that the best domain pairs can be decided based on similarity of their nature (such as books and movies), or simulate domain pairs by splitting the same dataset into multiple domains. We argue that the success of cross-domain recommendations depends on domain characteristics and shared (latent) information among domains; therefore posing new questions: What makes a good auxiliary domain? How should we choose the best auxiliary domain for a specific target domain? In this dissertation we examine the success and failure of cross-domain collaborative filtering across three different datasets with various characteristics of domains. Our goals are to explore the added value of cross-domain recommendations in comparison with traditional within-domain recommendations, and to achieve some progress in uncovering the main mystery of cross-domain recommendation: how can we determine whether a pair of domains is a good candidate for applying cross-domain recommendation techniques? For the former goal, we propose a cross-domain collaborative filtering approach based on canonical correlation analysis. In order to address the latter goal, we investigate a canonical correlation approach as a possible predictor of successful domain pairs and examine a range of features of a single domain and domain pairs in order to see how they could be used to improve predictions. Eventually, we propose a domain-pair classifier that can distinguish between the beneficial and non-beneficial domain pairs before performing the recommendations.

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1.0 INTRODUCTION

Information overload is one of the byproducts of internet growth. As the amount of information increases on the web, users face the challenge of finding the most relevant and useful information and products on the internet. Information filtering approaches and systems, such as information retrieval approaches, search engines, and faceted search interfaces, aim to alleviate this problem by either finding the most relevant information for users or helping users to find the most relevant information in a fast and efficient way. Recommender systems (or recommendation systems) have emerged as one of the solutions to the information overload problem in 1990's [22].

The goal of recommender systems is to present the most desirable information and products (items) to users based on their preferences. Many of the recommender systems rely on user modeling approaches to approximate user preferences and build user profiles based on users' purchase history, click-stream logs, item ratings, etc. For example, collaborative-filtering recommender systems achieve their goal by finding users of a similar taste, create user models built on users' histories, and recommend the items liked by these users to each other¹.

Although recommender systems are the topic of much research² and are very common in commercial systems, they still suffer from many problems. One of the important problems in recommender systems is the cold-start problem. When a new user starts using the system, or a new item is introduced in it, there is little to no history that is known for that user

¹Of course this is a very simplistic and high-level interpretation of the idea behind collaborative filtering. Each of the collaborative filtering approaches have their own elaborated algorithm to implement such a general idea.

²As examples, one can refer to machine learning and user modeling conferences, such as RecSys, UMAP, and KDD.

or item. As a result, the recommender system that relies on user or item histories cannot build a reliable profile for that user or item. Consequently, this recommender system will not be able to recommend any items to the cold-start user or cannot recommend the cold-start item to any users. A whole body of recommender system literature aims to target the cold-start problem. As examples, we can name hybrid recommender systems [8], context-based recommender systems [2], and community-based recommender systems [61]. Cross-domain recommender systems [6] are one of the newest types of systems that promise to alleviate the cold-start problem.

Cross-domain recommendation has recently emerged as a hot topic in the field of recommender systems [20]. Their idea is to use rating information accumulated in one domain (known as a source or auxiliary domain) to improve the quality of recommendations in another domain (known as a target domain). The proponents of cross-domain recommendation claim that such a technique can be especially helpful when a user has few or no ratings in the target domain or when the quality of recommendation in the target domain is low, due to lack of other information. A modern user works with many systems and many information domains. While she may have a solid user profile in a system that she has previously used, beginning to use a new domain or system would potentially benefit from cross-domain information. In this thesis, we aim to examine the promise of cross-domain collaborative filtering recommender systems, by studying their feasibility and performance, understanding when they work well, and finding the best domains in which these recommenders work well. In the following sections, we introduce the challenges of cross-domain collaborative filtering systems, our problem statement and research questions, and the organization of this thesis.

1.1 CHALLENGES AND MOTIVATIONS

As mentioned earlier, cross-domain recommender systems promise to alleviate cold-start problem, provide better quality recommendations, and provide a better understanding of user preferences by transferring information from one or multiple source domains to the target domain. However, little of the research on cross-domain recommender systems has

studied these issues comprehensively. One of the main reasons for this circumstance is the difficulty of finding real-world cross-domain datasets. Most of the systems that have multiple domains of items are commercial systems. Many of these systems have limitations in providing their users' private data to the researchers.

To avoid this problem, many researchers have simulated different domains in one dataset by splitting the items into multiple sectors, and treating each sector as a domain. This split can be based on some item features, e.g. genre for movies, or totally random [6]. In these cases, the generalizability of approaches are not tested on real domains and their distributions. For example, it is more likely that two different genres of movies have a similar distribution of user ratings, compared to rating distributions of the movie and electronic products domains. Users pay attention to the similar characteristics of movies, such as actors, screenplay, and director, in addition to the genre, when they want to rate them. But the factors for rating an electronic product is completely different from the factors to rate a movie. For example, in electronic products, the year the product is built is a very important factor; most people would like to have the most recent products in that domain. But, there are some old movies that will always be on top of peoples' favorite lists. So, eventually if an approach is tested on different genres of movies, it will not necessarily work for every set of domains.

Another important problem in cross-domain recommendation is the selection of source domains appropriate for a target domain. Previous works mostly assume that the best domain pairs can be decided based on similarity of their nature (such as books and movies) [76, 60], or simulate domain pairs by splitting the same dataset into multiple domains [6]. While the majority of early works have typically focused on one or two pairs of intuitively related domains and return quite positive results, which confirms the hopes of cross-domain enthusiasts [7, 60, 76], there also exist mixed results for cross-domain recommendations [64]. We argue that the success of cross-domain recommendations depends on domain characteristics and shared (latent) information among domains, in addition to the cross-domain algorithm itself; therefore posing new questions: What makes a good auxiliary domain? Do the features used to define a good auxiliary domain work for all algorithms and all datasets? and How should we choose the best auxiliary domain for a specific target domain?

In the next section, we introduce the research questions that we study in this thesis, to work towards resolving these issues in cross-domain collaborative filtering.

1.2 OBJECTIVES AND PROBLEM STATEMENT

In this thesis, we aim to gain a more detailed understanding of cross-domain collaborative filtering and the factors that affect its performance. More specifically, we would like to study if cross-domain recommendations are feasible and beneficial and what can lead us to the auxiliary domains that provide the most benefit in cross-domain recommenders.

The improvement we achieve from cross-domain recommendation could result from the added information or the approach we employ to recommend items in the target domain. As discussed in [10] some methods can improve the recommendation result without transferring knowledge from source to target domain, and only by improving the algorithm of recommendation. On the other hand, sometimes just adding the extra information from a related source domain and using a single-domain algorithm on the extended data can also improve the recommendations, especially in the cold-start setting [60]. In this thesis, we propose to study each of these aspects: if the improvement we get from cross-domain recommendations are because of the extra information added by the auxiliary domain; or because of the algorithm used in the cross-domain recommender; or for both of these reasons.

Another important factor in the results of cross-domain recommendation is the selection of the auxiliary domain. As discussed in the previous section, most of the work in the literature are either based on the assumption of choosing naturally similar domains or subdividing a single domain into multiple simulated domains. However, we expect some auxiliary domains to be better choices compared to others. We hypothesize that some data characteristics, in addition to the nature of the auxiliary domain, can be important factors in choosing better source domains.

In addition to finding out if an auxiliary domain helps or not, we hypothesize that the amount of improvement we get from performing cross-domain recommendation using each pair of domains can be affected by some of the data characteristics. We expect that discov-

ering the key characteristics of a good auxiliary-target domain pair, leads us to establish an auxiliary domain classifier that can distinguish between beneficial and non-beneficial source domains for a specific target domain. Eventually, we hypothesize that we can find interesting relationships between the domains for cross-domain recommendation. We would like to know if the discovered domains are also "intuitively" related.

In summary, here are the questions we would like to study in this thesis:

- Q1: Is cross-domain recommendation feasible and beneficial?
 - Q1.1: Is the benefit gained from a cross-domain recommender because of the extra data or the used approach?
 - Q1.2: Does cross-domain recommendation benefit the cold-start situation?
- Q2: Are all source domains helpful to all target domains?
 - Q2.1: What are the factors that distinguish between a helpful source domain and a non-helpful one?
 - Q2.2: What are the factors that determine the amount of improvement we get using cross-domain recommendation based on specific source and target domains?
 - Q2.3: What is the nature of good domain-pair choices?
- Q3: Is classification of domain-pairs into beneficial and non-beneficial feasible?

To answer the above research questions, we propose to use Canonical Correlation Analysis (CCA) as a tool for both performing recommendations and distinguishing the helpful auxiliary domains. To study the feasibility and benefit of cross-domain recommenders (Q1), we propose a cross-domain recommender approach based on canonical correlation analysis (CD-CCA), including a large-scale implementation of it (CD-LCCA). We compare CD-CCA with other cross-domain algorithms as baselines to study the approach effect on cross-domain recommendation results. We run a single-domain algorithm on target domain data to research the effect of added information compared to cross-domain approaches (Q1.1). To answer research question Q1.2, we analyze the results based on the size of user profiles.

In addition to using CCA for delivering cross-domain recommendations, we propose to use it in finding the beneficial auxiliary domains. We define various factors extracted from CCA, such as average CCA correlation in all components and number of significant canonical correlations between components, as cross-domain data factors in our analysis. In addition to that, we use other cross-domain characteristics, such as KL-divergence, and other single-domain features, such as data sparsity, in our study. We experiment on three datasets with different natures and various number of domains to study different combinations of source and target domains. We perform both bivariate correlation analysis and multi-variable regression analysis on these factors to answer the the second research question and its sub-questions. To study Q2.2, we define an "Improvement Ratio" factor as a dependent variable and run bivariate correlation analysis and multi-variable regression on data characteristics. We study the qualifications of domain-pairs and their characteristics in more details to find out about the counter-intuitive domain-pairs (Q2.3). Based on these analyses, we build a domain-pair classifier and evaluate its accuracy in different settings: within one system (dataset) and between different systems (Q3).

Eventually, this thesis leads to building a framework that can evaluate fitness of domains for cross-domain recommendation, select the best domain pairs for cross-domain recommendation, and perform cross-domain recommendation based on the selected source and target domains. An overview of such framework with the steps to achieve these goals is shown in Figure 1.

To explore the feasibility of this thesis, we performed some preliminary work that was reported in the proposal document. Specifically, we used one of the three proposed datasets (the Yelp academic) to run a pilot study. We implemented and ran the proposed CCA-based cross-domain algorithm (CD-CCA) on the Yelp dataset and compared the results with one of the proposed baseline single-domain algorithms (SVD++) and its cross-domain form (CD-SVD). We analyzed the results to find out if the selected cross-domain recommender results improve because of the approach or the added information; we performed partial analysis on a subset of the single-domain data characteristics and recommendation results; partly analyzed a subset of the cross-domain data statistics for the improvement of the picked cross-domain algorithms over the single-domain one; and looked at the nature of various domain pairs to get a deeper understanding of the analysis results.

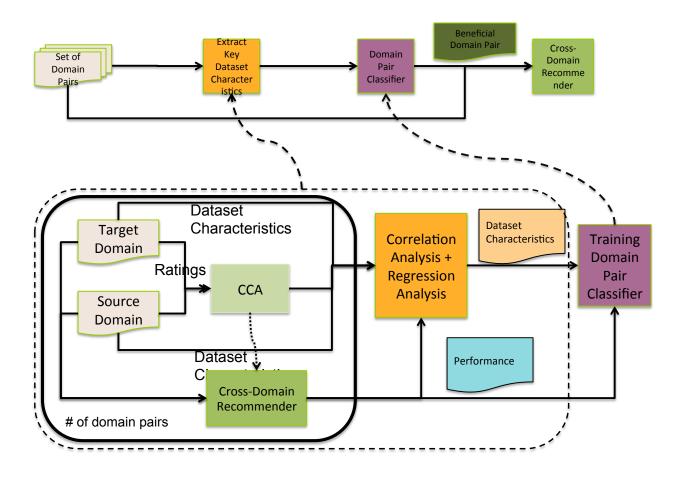


Figure 1: The proposed framework and tasks

1.3 ORGANIZATION OF THE THESIS

The rest of this dissertation is organized as follows. In Chapter 2, we review the closely related work in the literature to this dissertation and provide the background information required for the thesis. In Chapter 3, we introduce our proposed cross-domain algorithms and the baseline algorithms. In Chapter 4, we introduce the datasets that we are using in the experiments. Chapter 5 is dedicated to general experiments on and comparison of the proposed approaches and the baseline algorithms to answer research question Q1.1. In Chapter 6, we analyze the results for the cold-start situation to answer Q1.2. Chapter 7 includes an introduction to the dataset features we want to use in finding the appropriate domain pairs, the correlation analysis, and the regression analysis of these features with the error of single and cross-domain algorithms to answer Q2.1 and Q2.2. We then examine the domain pairs to understand if the correlation and regression results are in coordination with the intuitions about closely-related domain pairs (Q2.3). In Chapter 8 we introduce a domain classifier to find the best auxiliary domains and experiment with the classifier to examine its feasibility (Q3). Finally, in Chapter 9, we summarize the results of the research questions and list the contributions, limitations, delimitations, and possible extensions to this dissertation. Auxiliary materials are provided in Appendices A to C.

2.0 BACKGROUND AND RELATED WORK

In this chapter, we first introduce the notations that we will be using through this dissertation. Then, we briefly review the literature for recommender systems and various types of cross-domain recommenders. After that, we review a body of related collaborative filtering approaches that are not introduced as cross-domain, but are closely related to this ares. Eventually, we provide a summary of Canonical Correlation Analysis (CCA) and Large-Scale Canonical Correlation Analysis (L-CCA), as backgrounds for the proposed algorithms, and survey the previous application of CCA in the recommender systems fields of research.

2.1 NOTATION USED IN THIS DOCUMENT

In the subsequent chapters we will use the following notation:

- Matrices are shown in capital letters: X
- Vectors are shown in lowercase: w
- $y_{i,j}$ represents the value of Y in row i and column j
- X^T shows the transpose of matrix X and w^T shows the transpose of vector w
- X^{-1} represents the inverse of X
- \hat{Y} shows the estimated values for Y
- \tilde{Y} shows an incomplete matrix

The following is the definition of terms used in this proposal:

• **Domain** According to [34], domains can be categorized as system, data, and temporal domains. These categories represent, respectively, different datasets that a recommender

system is built upon, various representation of user preferences (explicit or implicit), and various time points in which the data is gathered. In this proposal, we define domains based on the nature of items that exist in the domains, e.g., books vs. movies.

- Target Domain is the domain in which recommendations are performed. The recommended items are chosen from this domain.
- Auxiliary or Source Domain is the domain from which knowledge is transferred to help recommendations in the target domain.

2.2 SINGLE AND CROSS-DOMAIN RECOMMENDER SYSTEMS

Recommender (Recommendation) Systems aim to alleviate the information overload problem by helping users to select items from the provided item or information space. The first recommender system was introduced more than twenty years ago by Goldberg et al. to deal with the increasing amount of messages that users received by email [22]. This system utilized a technique called Collaborative Filtering (CF) to provide recommendations to a user based on past actions performed by herself and her nearest neighbors. At first, traditional recommender systems followed this trend of using collaborative filtering approaches [58]. After a while, rule-based, content-based, and hybrid approaches emerged to address various problems in recommender systems [47].

In rule-based recommender systems, decisions are made based on some rules that are extracted, either manually or automatically, from user profiles. In traditional cases, this method depended on knowledge engineering abilities of the system designers to build a suitable rule base for specific characteristics of the domain and market [57].

Content-based recommender systems, provide recommendations to users based on comparing items or products to the items that user had showed interest to. A user profile in these systems represents explanations of product contents that user chose before. These recommender systems usually rely on Information Retrieval techniques such as classification, clustering, and text analysis [49]. Unlike collaborative filtering methods, user profiles are created individually in these systems, only based on the items seen or rated by the user

herself. We can name Letizia [39] and NewsWeeder [33] as first examples of content-based recommender systems.

Collaborative filtering-based recommender systems have achieved an acceptable success in e-commerce sites [23, 63]. These models usually include matching item ratings of current user (like rating on books, or movies) to similar users (close neighbors) to recommend items that are not yet seen/rated by this user.

Hybrid recommender systems were developed with the goal of solving the problems of content-based and collaborative filtering recommenders. These recommenders use various resources of information and combine both collaborative filtering and content-based methods [48, 38, 14, 2].

As the heterogeneity of data sources are increasing on the web, and due to the sparsity of data in each of these data sources, cross-domain recommendation has emerged as a research topic in the recent years. Although cross-domain recommendation is a recent field of study, it has gained increasing attention and is a promising way to develop new methods to improve recommendations, especially in a cold-start setting [60]. Cross-domain recommender systems aim to take advantage of information among related source (auxiliary) domains to recommend items in a target domain [20]. In some cases, the recommendation in the source and target domains can be performed simultaneously [36, 82], and in other cases, the recommendations are only delivered in the target domain [50].

A limitation of a significant number of works in cross-domain recommendation area is that they provide empirical results based on an artificial setting where either a single-domain dataset is subdivided into separate domains, e.g., separating the movie domain based on their genres [6, 11], or different user and items sets are used [52]. This is due to limited available cross-domain datasets. In order to overcome such a limitation, Dooms et al. mined twitter for structured rating tweets (such as "I liked X video on YouTube") for IMDB, Pandora, and Goodreads ratings, and YouTube likes [13], with the hopes of capturing some users with ratings in more than one system. Also, Zhang et al. developed a tool to record and analyze user browsing actions in web browsers, and provide browser-oriented cross-site recommendations [81].

Work on cross-domain recommendations includes collaborative filtering [21, 25, 28, 42,

60], content-based [7, 15, 29, 62, 68], and hybrid [18, 9, 74] approaches. In the following, we review the major work in each of these three categories and discuss the challenges in this field.

The research presented in this dissertation, and the proposed approaches, focus on cross-domain collaborative filtering approaches that share a common set of users between the source and target domains. To understand which features are important in finding the best-matched domain pairs, we design a set of comprehensive experiments and perform cross-domain collaborative filtering on multiple datasets. We use canonical correlation analysis as the main feature that can lead us to selection of best source domains for a target domain. To the best of our knowledge, we have the first comprehensive analysis for domain pair selection in cross-domain collaborative filtering.

2.2.1 Content-Based Cross-Domain Recommendations

There are few works in pure content-based cross-domain recommendation literature.

For example, Fernandez-Tobias et al. presented an ongoing research on a generic knowledge-based description framework built upon semantic networks in [19]. They automatically extracted information about two different domains, such as architecture and music, which are available in Linked Data repositories and performed weight spreading on the resulting concept graph to identify items in the target domain that were related to items of the source domain.

Low et al. used a hierarchical Bayesian model based on Latent Dirichlet Allocation and on latent side features for cross-property integration in Yahoo News and Yahoo Front Page [43].

Sahebi and Walker proposed a generic framework for content-based cross-domain recommendations in [62]. In this framework, an efficient method of feature augmentation is proposed to implement adaptation of domains. Instead of defining the notion of domain based on item descriptions, user-based domains are introduced. They applied their method in the job recommendation problem on Linkedin data.

Elkahky et al. proposed a content-based multi-view deep learning approach to cross-

domain recommendations in [15]. They ran their experiments on Windows application recommendation, news recommendation, and movie/TV recommendation domains using search engine logs from Bing Web vertical, news article browsing history from Bing news vertical, app download logs from Windows AppStore, and movie/TV view logs from Xbox data plus public co-authorship data.

2.2.2 Collaborative Filtering Cross-Domain Recommenders

Cross-domain collaborative filtering aims to transfer user's rating pattern from source (auxiliary) domains to a target domain for the purpose of alleviating the sparsity problem and providing better target recommendations. Most of the work on cross-domain collaborative filtering has been either on manually picked, naturally close domains (e.g. movie and music) or on one domain that is randomly split into datasets considered as distinct domains.

As an example of recent work, Tirushi and Kuflik presented initial results of a work in progress that ranked and mapped between pairs of domains based on the ability to create recommendations in domain one using ratings of items from the other domain [70]. They collected 2,148 Facebook profiles, which contained items (likes) in four domains: Music, Movies, TV shows, and Books. Their initial results, with cross-domain collaborative filtering on a joint space of domains, showed that there are differences between the source domains with respect to the quality of the recommendations.

Zhang et al. proposed MCF and MCF-LF methods that exploit the relationships between domains and perform multiple collaborative filtering tasks simultaneously [82]. They used a probabilistic framework which uses probabilistic matrix factorization to model the rating problem in each domain and allows the knowledge to be adaptively transferred across different domains by automatically learning a link function between domains. Their experiments were performed on MovieLens and Book Crossing datasets separately, each of which are divided randomly into five simulated domains. This approach does not need shared users or items between the domains.

In [26] constrained collective matrix factorization (CCMF) was proposed as an extension of collective matrix factorization ([66]) to iteratively factorize the rating matrices in source

and target domain. The authors added a constraint on the user feature matrices for target domain and auxiliary domain. This approach assumes sharing users in the datasets and the experiments are on a simulated dataset sampled from the Netflix dataset and a real dataset crawled from Douban. Klami et al. also provided a method based on collective matrix factorization (CMF) [30]. This method allows each of the matrices to have a separate low-rank structure independent of the other matrices, as well as structures that are shared only by a subset of them. They tested the method on MovieLens and Flickr data.

Lu et al. proposed Selective Transfer Learning that transfers the data using a criterion based on empirical prediction error and its variance [45]. It extends Gaussian Probabilistic Latent Semantic Analysis (GPLSA) to Transferred Gaussian Probabilistic Latent Semantic Analysis (TGPLSA) model, then applies TGPLSA as base model over weighted instances for Selective Transfer Learning for Collaborative Filtering (STLCF). In this case, the approach needs either shared users or shared items.

Moreno et al. proposed a transfer learning technique (TALMUD) that extracts knowledge from multiple domains containing rich data (e.g., movies and music) and generates recommendations for a sparse target domain (e.g., games) [50]. The approach learns the degree of relatedness between different source domains and the target domain, without requiring overlapping users between domains. They tested their approach on Netflix, Jester, Music Loads, and Games Loads data.

Zhao et al. proposed a framework to construct entity correspondence between domains with limited shared user or items [83]. They used active learning to facilitate knowledge transfer across recommender systems based on Maximum-Margin Matrix Factorization. Their setting of source and target domains is as following: Netflix \rightarrow Netflix, DoubanMovie \rightarrow DoubanBook and Netflix \rightarrow DoubanMovie.

Hu et al. proposed a generalized Cross Domain Triadic Factorization (CDTF) model over the triadic relation user-item-domain based on CP tensor decomposition [25]. They leveraged user explicit and implicit feedback respectively, along with a genetic algorithm based weight parameters tuning algorithm to trade off influence among domains optimally. They experimented on Amazon data (music CDs, DVDs and VHS video tape domains) and social network dataset provided by KDD Cup 2012 with 4 anonymous item domains.

Twin-Bridge Transfer Learning (TBT) proposed in [65] reduces the sparsity in target data by transferring knowledge from dense auxiliary data with either shared user or item sets and the similarity graphs of users and items constructed from the learned latent factors. The authors tested their approach on MovieLens10M and Epinions datasets separately with simulated domains created by random separation of datasets.

Wu et al. proposed a fusion multi-domain semantic topics and syntax classes model based on hidden Markov model with latent Dirichlet allocation (HMM-LDA) [77]. In every sub-domain, the model uses HMM-LDA to extract sub-domain topic and class features. Then, the fusion model combines the multiple sub-domain models to extract the whole domain features. They used MovieLens and Book-Crossing dataset (book and movie as source, movie as target) for their experiments. This approach does not require shared users or items.

Xin et al. proposed a nonlinear transfer learning model, and used the radial basis function (RBF) kernel to map user features of multiple sites [78]. This approach consists of two steps: first, the initial feature vectors for users/items in source and target domains are learned separately using probabilistic matrix factorization; then, a group of regression functions (using support vector machine) are used to map the user latent feature in the auxiliary domain to the user latent feature in the target domain. The kernel trick is used in this second step. In this approach the users should be shared in the domains. Douban (movies) and DianPing (restaurants) are the datasets the authors experimented on.

Loni et al. used factorization machines on Amazon data (books, music CDs, DVDs and video tapes) for cross-domain collaborative filtering [42].

Gao et al. [21] proposed a cluster-level based latent factor model for cross-domain recommendations. They based their optimization problems on a joint non-negative matrix tri-factorization. The assumption behind this factorization is that there is a common latent rating pattern across the two domains (in addition to domain-specific latent rating patterns) that drives the useful shared information. They tested their method on MovieLens, EachMovie, and Book-Crossing datasets.

Iwata and Takeuchi proposed a method based on matrix factorization, assuming that latent vectors in different domains are generated from a common Gaussian distribution with

a full covariance matrix [27]. Neither users nor items were shared across domains. They tried their method on Movielens, EachMovie, Netflix, and Amazon review rating (Book, DVD, Electronics, Kitchen, Music and Video).

Liu et al. proposed the notion of Hyper-Structure Transfer (HST) and its model called the Minimal Orthogonal Tensor Approximation with Residuals (MOTAR) that transfers nonlinearly correlated knowledge between domains [41]. This approach works on the domains with shared users. Movielens and DBLP (each citation is a rating, each category of MS research is a domain) are the datasets they have tested their approach on.

Mirbakhsh and Ling proposed cross-domain clustering-based matrix factorization on Amazon dataset (DVD, music, video, electronics, kitchen and housewares, and toys and games) and Epinions dataset (10 categories with the most observed ratings) in [46].

2.2.3 Hybrid Cross-Domain Recommendations

Many of the literature on transferring knowledge in recommender systems fall into the category of hybrid recommender systems. Specially since some literature consider hybrid-recommendations as cross-domain recommendation [34]. In these approaches two or more of the following types of information is used: user behavior data (such as user ratings, purchases, and logs), user content profile (such as user tags, the content of items consumed by users, or the semantic network behind them), and user social profile.

As an example of hybrid, cross-domain recommendation method, Acar et al. formulated the problem as a coupled matrix and tensor factorization (CMTF) problem, in which heterogeneous datasets are modeled by fitting outer-product models to higher-order tensors and matrices [1]. They proposed an optimization approach called CMTF-OPT, which is a gradient-based optimization approach for joint analysis of matrices and higher-order tensors. However, their data in their experiments is not cross-domain: they randomly generated matrices and tensors in a simulation.

Wang et al. proposed a Tag Transfer Learning (TTL) method that transfers tag topics instead of user-item rating patterns [74]. They used "MovieLens 10M Ratings, 100k Tags" data to perform this transformation on the movies domain only. Dong and Zhao analyzed the

feasibility of tag-based cross domain rating prediction based on K-nearest neighbor model [12]. They reported the associative tag pairs of user preferences on items across domains on Douban dataset. This dataset consists of user rating and tag information on books, movies, and music in the Chinese Douban website.

Roy et al. recommended media (video) in social networks (twitter) with online stream LDA method (OSLDA) in [59]. They built a common topic space between the domain of social stream and video to do that.

In [32] Krohn-Grimberghe et al. added social data for recommendation by extending Bayesian personalized ranking (BPR) framework to the multi-relational case. They experimented on three social network datasets: Blogcatalog, Flickr, and YouTube; each dataset consists of relation between users and labels (target), and social relation between users and other users (auxiliary).

Enrich et al. proposed three tag-based rating prediction models using UserItemTags, UserItemRelTags, and ItemRelTags [16]. They experimented on MovieLens 10M and LibraryThing datasets.

Shapira et al. extracted users' favorite items and preferences in the domain of recommendation from Facebook content published by users on their personal pages [64]. They gathered the data about preferences related to other domains to allow cross-domain recommendation. They performed a field study with 95 subjects.

Chen et al. proposed a generalized cross domain framework that integrates social network information with collaborative-filtering data using tensor factorization [9]. They recommended users, tags, and items with topic based social regularization (FUSE) on the data from MovieLens dataset (source) and LibraryThing (target).

In [18], Fernandez-Tobias et al. adapted the gSVD++ algorithm to propose TagGSV++ that introduces a new set of latent variables, and enriches both user and item profiles with independent sets of tag factors on MovieLens and LibraryThing data.

Co-Citation Selection (CCS) [69], was proposed based on collaborative filtering on cocitation networks, in which neighboring papers were selected and weighted into publication citation prediction.

2.2.4 Shared Data in Cross-Domain Recommenders

Many cross-domain algorithms assume that the source and target domains share at least one of the user or item spaces [45, 65, 78, 41]. In some cases, having partial shared user or item sets is sufficient [30, 83]. In other cross-domain approaches, the assumption is that no shared users or items are needed in the domains [36, 82, 77, 27].

However, there is some controversial literature regarding the no-sharing cross-domain approaches. Cremonesi and Quadrana provide empirical evidence in [10] that CBT (code book transfer, one of the pioneer no-sharing cross-domain approaches presented in [35]) improves the accuracy of recommendations without transferring knowledge from source to target domain. They show that the injection of the codebook in the target domain is equivalent to a two-matrix factorization algorithm without transfer of knowledge from the source domain and the increase of accuracy measured in this approach is due to a pitfall in the evaluation procedure.

2.2.5 Selecting the Best Auxiliary Domain

Although a considerable amount of work has recently been done on cross-domain recommendations, most of the research either assumes that the selected domains are related to each other or the experiments are conducted on simulated domains, generated from one domain.

In some of the previous works, such as [82, 45], the researchers focused on transferring some of the records from the source domain to the target domain based on some criterion or weighted transfer. However, they have not studied the general relatedness of the source and target domains.

In addition to our preliminary work, the only other work in this area is by Yi et al. [80]. They select auxiliary domains in movie recommendation (based on movie genres). They conclude that Kullback-Leibler (KL) divergence between non-overlapping user ratings and the number of overlapping users between target and auxiliary domains are indications of choosing a helpful domain. This study is limited to the MovieLens 1M dataset with simulated domains.

2.2.6 Related Collaborative Filtering Approaches

In some of the collaborative filtering approaches, transfer learning within one domain is used to alleviate the sparsity problem or add extra information for the recommendation. Although this is not considered cross-domain recommendation, these works worth noting as related work.

For example, Pan et al. proposed transfer by integrative factorization (TIF), that uses auxiliary uncertain ratings (a rating distribution as a rating spectrum involving uncertainty instead of an accurate point-wise score) to improve the performance of recommendation [53]. They integrated auxiliary data of uncertain ratings as additional constraints in the target matrix factorization problem, and learned an expected rating value for each uncertain rating. The experiments were not on different domains and the authors split the experimental data randomly and disturbed some of the ratings as the auxiliary rating profile. The experiments were done on MovieLens and Netflix datasets.

In their next paper, Pan et al. used additional auxiliary data in the form of binary ratings, transferring knowledge to a target numerical rating matrix of the same domain [54]. Their framework, Transfer by Collective Factorization (TCF), constructs a shared latent space collectively and learns the data-dependent effect separately. They experimented on Moviepilot rating data and Netflix data. Li et al. defined the collaborative filtering domains as a 2-D site-time coordinate system, on which multiple successive time-slices, can share group-level rating patterns [37]. They developed a generative model: ratings over site-time (ROST) and used MovieLens dataset to run their experiments.

Parimi and Caragea proposed a method based on a regularized latent factor model, using implicit feedback [55]. This approach can handle variable user overlap. The authors have tried the approach on last.fm (artist, friend, and tag domains) and DBLP (co-author, conference and reference domains) datasets.

In addition to the transfer learning approaches, context-aware recommenders are also close to cross-domain recommendation research field. For example, Liu et al. presented the Contextual Operating Tensor (COT) model, that represents the common semantic effects of contexts as a contextual operating tensor and represents a context as a latent vector [40].

They assumed that context combinations can operate the latent characteristics of entities. They experimented on Food (virtuality and hunger contexts), Adom (movie data companion, when, release, rec, and where as contexts), and Movielens-1M (hour and day timestamp as context) datasets.

Another set of related collaborative filtering approaches aim to improve the recommendations by introducing external rating information, in an aggregated format, to the target domain. For example, Adomavicius and Tuzhilin proposed using aggregated user ratings in a hierarchical recommender system [3]. Umyarov and Tuzhilin proposed to use aggregated ratings from various user segments, in the form of parameter constraints, to improve recommendations [71]. They later introduced a general class of methods that combined external aggregate information, in the form of average and variance of the ratings, along with individual ratings [72]. They experimented on MovieLens and Netflix data to show that the aggregate average ratings are good enough to improve the recommendations. Umyarov and Tuzhilin theoretically proved in [73] that adding the aggregate rating information results in better predictions of unknown ratings and empirically showed that it alleviates the cold-start problem. The proof is based on the idea that adding the aggregate ratings reduces the variance of estimated ratings, and thus, leads to less error.

2.3 CANONICAL CORRELATION ANALYSIS

We use canonical correlation analysis as a main building block of our proposed algorithm and as an important factor in the domain-pair selection experiments and analysis. In the following sections, we review regularized CCA and large-scale CCA to provide a background for the remaining chapters in the dissertation.

2.3.1 Regularized CCA

Canonical correlation analysis (CCA) is a multivariate statistical model that studies the interrelationships among sets of multiple dependent variables and multiple independent

variables. It is the most generalized member of the family of multivariate statistical techniques [24]. It is related to factor analysis in the sense that it creates composites of variables, and is related to discriminant analysis in finding independent dimensions for each variable set. The goal of this analysis is to produce the maximum correlation between the dimensions. As a result, canonical correlation finds the optimum structure or dimensionality of each variable set that maximizes the relationship between independent and dependent variable sets.

In other words, if we have $X \in \mathbb{R}^{m \times n}$ and $Y \in \mathbb{R}^{p \times n}$, CCA finds two projection vectors $w_x \in \mathbb{R}^m$ and $w_y \in \mathbb{R}^p$ that maximize the correlation coefficient:

$$\rho = \frac{w_x^T X Y^T w_y}{\sqrt{(w_x^T X X^T w_x)(w_y^T Y Y^T w_y)}}$$
(2.1)

Since Equation 2.1 is not affected by re-scaling of w_x and w_y (the multiplication of these vectors by a constant α does not change the value of ρ), we can maximize ρ as follows.

$$\max_{w_x, w_y} w_x^T X Y^T w_y$$
 subject to $w_x^T X X^T w_x = 1, w_y^T Y Y^T w_y = 1$ (2.2)

It can be shown that solving Equation 2.2 is equivalent to finding the eigenvectors of top eigenvalues of the generalized eigenvalue problem in Equation 2.3, in which η is the eigenvalue that corresponds to the eigenvector w_x .

$$XY^T(YY^T)^{-1}YX^Tw_x = \eta XX^Tw_x \tag{2.3}$$

To compute multiple projection vectors, we can solve the optimization problem in Equation 2.4, in which matrix W consists of multiple projection vectors.

$$\max_{W} Trace(W^{T}XY^{T}(YY^{T})^{-1}YX^{T}W)$$
 subject to $W^{T}XX^{T}W = I$ (2.4)

To avoid the over-fitting of ρ and the singularity of XX^T , a term λI is added to Equation 2.3. We have the constraint $\lambda > 0$ in this regularization term. Eventually, the regularized CCA attempts to solve the generalized eigenvalue problem in Equation 2.5.

$$XY^{T}(YY^{T})^{-1}YX^{T}w_{x} = \eta(XX^{T} + \lambda I)w_{x}$$

$$(2.5)$$

Sun et al. solve the regularized CCA problem, using a least squares formulation of it, with the Least Angle Regression algorithm [67].

```
Input: \mathbf{X} \in n \times p_1, \mathbf{Y} \in n \times p_2: Data matrices. k_{\text{cca}}: Number of top canonical variables we want to extract. t_1: Number of orthogonal iterations. k_{\text{pc}}: Number of top singular vectors for LING t_2: Number of GD iterations for LING Output: \mathbf{X}_{k_{\text{cca}}} \in n \times k_{\text{cca}}, \mathbf{Y}_{k_{\text{cca}}} \in n \times k_{\text{cca}}: Top k_{\text{cca}} canonical variables of \mathbf{X} and \mathbf{Y}. 1. Generate a p_1 \times k_{\text{cca}} dimensional random matrix \mathbf{G} with i.i.d standard normal entries. 2. Let \mathbf{X}_0 = \mathbf{X}\mathbf{G}, \hat{\mathbf{X}}_0 = \mathbf{Q}\mathbf{R}(\mathbf{X}_0) 3. for t = 1 to t_1 do \mathbf{Y}_t = \mathbf{LING}(\hat{\mathbf{X}}_{t-1}, \mathbf{Y}, k_{\text{pc}}, t_2), \hat{\mathbf{Y}}_t = \mathbf{Q}\mathbf{R}(\mathbf{Y}_t) \mathbf{X}_t = \mathbf{LING}(\hat{\mathbf{Y}}_t, \mathbf{X}, k_{\text{pc}}, t_2), \hat{\mathbf{X}}_t = \mathbf{Q}\mathbf{R}(\mathbf{X}_t) end for t = 1 to t_1 do t = 1 to t_2 do t = 1 to t_3 do t = 1 to t_4 do t = 1 to t_4
```

Figure 2: L-CCA algorithm as presented in [44]

2.3.2 Large-Scale CCA

Calculating CCA can be very resource-consuming especially in the traditional approaches that should calculate QR-decompositions or singular value decomposition of large data matrices. To avoid these time and memory consuming operations, Lu and Foster developed an iterative algorithm that can approximate CCA on very large datasets [44]. They establish an error analysis for the case of having finite number of iterations in the algorithm and prove that the algorithm converges to the real value of CCA in case of infinite iterations.

This approach relies on LING, a gradient-based least squares algorithm that can work on large-scale matrices. As we have seen in the previous section, CCA can be computed as an iterative least squares problem. So, to compute CCA in L-CCA, first a projection of one of the data matrices on a randomly-generated small matrix is generated, to reduce the size of the matrix. Then, a QR-decomposition of this smaller matrix is calculated. After that, the CCA is calculated iteratively, by applying LING on the reduced-sized QR-decompositions of the original data matrices, in each iteration. Every time after running LING, a QR-decomposition is calculated for numerical stability. A summary of this algorithm that is presented in [44] is shown in Figure 2.

The LING algorithm relies on the intuition that the projection of independent variables on the least square estimates, can be divided (column-wise) into two smaller orthogonal components, each of which is related to the top (or bottom) singular vectors of the data. Then, it computes the first orthogonal component using randomized SVD, and the second one using gradient descent algorithm.

To be more specific, considering the least-squares problem of $Y = X\beta$, then $X\beta^* = X(X^TX)^{-1}X^TY$ is the projection of Y into column space of X^1 . Calculating $(X^TX)^{-1}$ takes a long time for a large $X_{n\times p}$. To calculate $X\beta^*$ without the need of calculating $(X^TX)^{-1}$, Lu and Foster rely on splitting the singular vectors of X.

If U_1 is the top k_{pc} singular vectors of X, and U_2 is the remaining $p - k_{pc}$ singular vectors, $X\beta^*$ can be divided into two orthogonal vectors as in Equation 2.6. Then, they calculate the first term using randomized SVD, since $K_{pc} < p$. Let $Y_r = Y - U_1U_1^TY$. Then the second term can be calculated using gradient descent for $Y_r = X\beta_r$.

$$X\beta^* = U_1 U_1^T Y + U_2 U_2^T Y (2.6)$$

Lu and Foster provide an error bound for the Ling algorithm and an error bound for L-CCA based on that in [44].

2.3.3 CCA in Recommender Systems

CCA has been used in different literature for the single-domain recommenders with various resources or to find the correlation between the content (such as text or image) of the resources in cross-domain recommender systems. To the best of our knowledge, it has not yet been used in a pure, rating-based, cross-domain collaborative filtering setting. For example, in the area of recommender systems, Faridani has used CCA to predict hotel ratings from textual comments of the hotels and their sentiment analysis [17]. Elkahky et al. use CCA as a baseline user modeling approach for their proposed recommendation system in [15]. They provide content-based cross-domain recommendations in the domains of apps, news, movies, and TV shows using a multi-view deep learning model. In [51], Ohkushi has used Kernel CCA in context-aware setting to find the relationship between music pieces and human motion to recommend music to users. Yang et al. [79] have proposed a feature learning algorithm that

 $^{^{1}\}beta^{*}$ is the estimate for β

uses CCA for inferring features of semantic information in the data. However, Yang et al. have not yet used their model in recommender systems.

3.0 CCA-BASED CROSS-DOMAIN ALGORITHMS

In this chapter, we propose cross-domain collaborative filtering algorithms based on regularized CCA and large-scale CCA. We base our approaches on canonical correlation analysis, because we hypothesize that this tool can lead us to a better understanding of the relationship between the domain pairs and thus, a better cross-domain recommendation results. The proposed approaches can be categorized into cross-domain collaborative filtering methods that require a shared set of users between the source and target domains. These approaches are used in finding the answers to the research questions presented in this thesis. In the last sections of this chapter, we introduce the baseline algorithms that we use in the experiments to compare the results with the proposed algorithms.

3.1 CD-CCA

As explained in Section 2.3.1, CCA evaluates the latent linear correlations between two sets of variables. To draw an analogy between CCA and cross-domain recommender, we suppose that there are n common users between the source and target domains. We consider the source (auxiliary) domain in cross-domain recommender as the independent variable set X (with n users and m items), and the target domain as the dependent variable set Y (with n users and p items). Note that here we are working on $m \times n$ and $p \times n$ item-user matrices, as opposed to the usual user-item matrices in collaborative filtering. The value p in Equation 2.1 shows the maximum canonical correlation that can be achieved by rotating the X and Y spaces in direction of w_x and w_y , respectively. In other words, CCA calculates the components of each domain, that are consisted of sets of items from each of the domains,

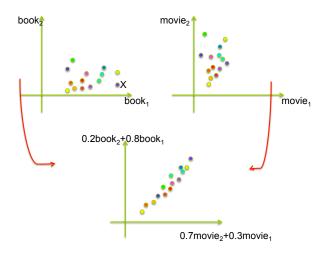


Figure 3: A toy example of CCA in cross-domain recommender system setting

which are most similar to each other based on user rating behavior. Also, it determines how much the two components are correlated to one another.

As an example this analogy, we can look at Figure 3. In this example, we assume that we have "books" (upper left-hand side) and "movies" (upper right-hand side) domains. We assume that each domain has two items in it: "book1" and "book2" are a set of dependent variables in the "books" domain and "movie1" and "movie2" are a set of independent variables in the "movies" domain. The axes show user ratings on these items in the domains. Each user in each domain is represented by one dot. Users are separated by dots with different colors: the purple dot in the "books" domain shows the rating of the same user as the purple dot in the "movies" domain. For example, the user marked by "X" has a high rating on "book1" and a low rating on "book2". CCA finds the components of each of the "books" and "movies" domains so that the correlation between user ratings, represented in these components, are maximized (the lower picture). These components are linear combinations of items in the two domains. In this example, the component found by CCA in the "books" domain is a linear combination of 0.2 of rating values on "book1" and 0.8 of rating values on "book2".

As a result, if we know the ratings in the source domain X and ratings in the target

domain Y, we can find the w_x and w_y that maximize the canonical correlation between X and Y. In other words, with the projections vectors w_x and w_y , we know how the ratings of a combination of items in the source domain affect the ratings of an item in the target domain. Consequently, after adding the user ratings of the source domain X, we can understand how all of the ratings of a user in the source domain affect the same user's ratings in the target domain. Eventually, we can estimate the ratings of users in the target domain \hat{Y} by using the projection vectors, the source domain ratings, and the canonical correlation value [75]. The calculation of estimated rating (\hat{Y}) is shown in Equation 3.1. Thus far, this approach only focuses on the first canonical component (projection vectors) that maximize the correlation $(\rho \text{ or R-statistic})$. There are other components between the domains that can indicate different projection vectors and correlations (R-Statistics) for each pair of them. In this case of multiple projections, the estimated rating matrix \hat{Y} is calculated as in Equation 3.2. Here, if we assume that c pairs of projection vectors are calculated, P is a diagonal $c \times c$ matrix, in which the diagonal elements are ρ s for each canonical component; W_x is a $m \times c$ matrix consisted of c projection vectors of size $m \times 1$; and W_y is a $p \times c$ matrix of c projection vectors of size $p \in 1$.

$$\hat{Y} = w_y \rho w_x^T X \tag{3.1}$$

$$\hat{Y} = W_y P W_x^T X \tag{3.2}$$

If the target rating matrix is incomplete and has some missing values (\tilde{Y}) , we can estimate W_x and W_y (\hat{W}_x and \hat{W}_y) by calculating the canonical correlations between the source rating matrix X and incomplete target matrix \tilde{Y} . Then, we can use the estimated projection vectors \hat{w}_x and \hat{w}_y to estimate a complete rating matrix \hat{Y} . More specifically, if we want to predict the unknown rating of user i on item j in the incomplete target domain $(\hat{y}_{j,i})$, we follow Equation 3.3 after finding \hat{W}_x and \hat{W}_y on matrices X and \tilde{Y} . Here, $X_{k,i}$ is the rating of user i on item k; $\hat{W}_{y_{j,l}}$ refers to the target projection element for the item j and component l; and $\hat{W}_{X_{k,l}}$ is the source projection element for the item k and component l.

$$\hat{y}_{i,i} = \sum_{l=1}^{c} \hat{W}_{y_{i,l}} P_{l,l} \sum_{k=1}^{m} \hat{W}_{X_{k,l}} X_{k,i}$$
(3.3)

As an abbreviation, we use the name CD-CCA for this CCA-based cross-domain recommender. The process of mapping between source and target domains in CD-CCA is shown in Figure 4.

One of the problems with this CD-CCA algorithm is its scalability. Calculating matrix multiplications in large scale and dense format can be difficult in terms of both memory and processing requirements. As a result, in the next section, we propose a new algorithm (called CD-LCCA) that uses large-scale CCA [44] to alleviate this problem.

3.2 CD-LCCA

As we have seen in section 2.3.2, large scale CCA finds a lower-dimensional representation of each of the input matrices and then calculates the canonical correlation analysis between these two matrices. To base our cross-domain recommender algorithm on LCCA, suppose that we have a $n \times m$ source domain rating matrix X and a $n \times p$ target domain rating matrix Y. Here, n represents the number of shared users between the source and target domains; m shows the number of items in the source domain; and p shows the number of items in the target domain. Suppose that X_c $(n \times x_c)$ is the lower dimensional matrix that represents the source domain rating matrix X, and Y_c $(n \times y_c)$ is the lower dimensional matrix that represents the target rating matrix Y in the LCCA algorithm. Then, if we calculate the canonical correlations between X_c and Y_c , we will have $X_cW_{x_c}$ $(n \times k_{cca})$ and $Y_cW_{y_c}$ $(n \times k_{cca})$ as canonical variates and P $(k_{cca} \times k_{cca})$ as the canonical correlation between these variates. Thus, we can map X_c to Y_c (and vice versa) based on these canonical correlations and variates. For example, Y_c can be achieved using Equation 3.4.

$$Y_c = X_c W_{x_c} P W_{y_c}^T \tag{3.4}$$

Although Equation 3.4 maps the source and target domains by building a relationship between their lower dimensional representations $(X_c \text{ and } Y_c)$, we need to be able to map the original source and target matrices (X and Y) to be able to estimate user ratings in them. To build a relationship between the original source and target domain matrices, we first look

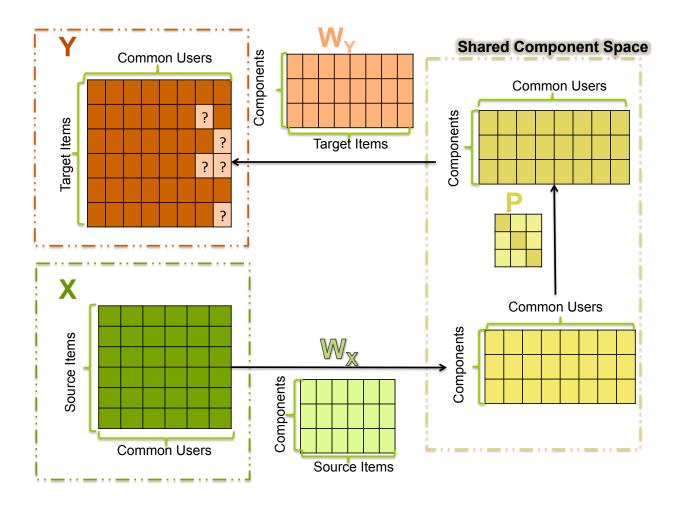


Figure 4: Mapping between source and target domains in CD-CCA

at the relationship between each domain matrix and its lower dimensional representation. Considering the source domain matrix (X), we build X_c in the first step of LCCA by solving an iterative least square problem, having a QR-decomposition in each iteration. Although we loose the mapping information between X and X_c in this iterative process, having both X and final X_c matrices, we can restore the mapping that happens between them. Since X_c is a lower dimensional projection of X, we can write their relationship as in Equation 3.5. Here, X_c matrix X_c matrix X_c matrix X_c matrix X_c matrix X_c matrix X_c .

$$X_c = XM (3.5)$$

Consequently, we can find the mapping M by the inverse relationship between X and X_c using Equation 3.6.

$$M = X^{-1}X_c \tag{3.6}$$

The same can be applied to find the mapping of target rating matrices Y and its lower-dimensional representation Y_c (Equation 3.7).

$$N = Y^{-1}Y_c \tag{3.7}$$

So, we can also rebuild Y based on N and Y_c ($Y = Y_c N^{-1}$). Combining Equations 3.7, 3.6, and 3.4, we can now map between the original source and target rating matrices as presented in Equation 3.8 and have an estimation of user ratings in the target domain (\hat{Y}).

$$\hat{Y} = XMW_{x_c}PW_{y_c}^{-1}N^{-1} \tag{3.8}$$

As a result, if we would like to estimate the rating of user i on item j, we can use:

$$\hat{y}_{i,j} = \sum_{q=1}^{m} X_{i,q} \sum_{o=1}^{c_x} M_{q,o} \sum_{l=1}^{k_{cca}} W_{x_{co,l}} P_{l,l} \sum_{r=1}^{c_y} W_{y_{cl,r}} N_{r,j}^{-1}$$
(3.9)

Since X and Y matrices are sparse, we take advantage of this property in Matlab implementation to reduce the memory requirements. Having $U = X_c W_{x_c}$ as an output of Matlab's

"canoncor" function, we can skip this multiplication. Calculating N is fast and efficient using the "mldivide" function¹. We can thus calculate \hat{Y} using Equation 3.10.

$$\hat{Y} = UPWy_c^{-1}N^{-1} \tag{3.10}$$

Note that U, W_{yc} , and N (and thus the calculated matrix \hat{Y}) are dense matrices. The density of U, W_{yc} , and N is not problematic in terms of memory because they are all low-dimensional matrices (compared to \hat{Y}). To be more memory-efficient in calculating \hat{Y} , we first break Equation 3.10 to a multiplication of two dense matrices (A and B) in lower dimensions. Then, we strip away the unnecessary values from these two matrices and transform them to the Matlab's sparse format. By multiplying these new sparse matrices, we will achieve a sparse estimation of Y.

To this end, we compute $A = Wy_c^{-1}N^{-1}$ (which is a $k_{cca} \times p$ matrix), and B = UP (which is a $n \times k_{cca}$ matrix). Since we need to calculate the rating values only for test users and test items, not all rows and columns of A and B are required. If $S \subseteq \{1..n\}$ shows the set of test users, and $I \subseteq \{1..p\}$ represents the set of target items we need to estimated user ratings on, we can build the sparse sub-matrix of A (\tilde{A}) and the sparse sub-matrix of B (\tilde{B}) as following:

$$\tilde{A}_{i,:} = \begin{cases} A_{i,:}, & \text{if } i \in S \\ 0, & \text{otherwise} \end{cases}$$
(3.11)

$$\tilde{B}_{i,:} = \begin{cases} B_{:,i}, & \text{if } i \in I \\ 0, & \text{otherwise} \end{cases}$$
(3.12)

Eventually, we will have²:

$$\hat{Y} = \tilde{A}\tilde{B} \tag{3.13}$$

¹If the source matrix size is too big and "mldivide" function takes too long, we take advantage of the column-wise independence of "mldivide" (or the fact that $[A|B]^{-1}C = [A^{-1}C|B^{-1}C]$). Thus, we separate the source matrix into multiple smaller matrices, using column-wise partitioning. Then, we apply the "mldivide" function on each of these matrices and eventually join the results together. In other words: $N = Y^{-1}Y_c = ([Y_1|Y_2]^{-1}Y_c) = [Y_1^{-1}Y_c|Y_2^{-1}Y_c]$.

²The matrix multiplication tricks explained here are for using Matlab. Since Matlab is more efficient in working with matrices, compared to having "for" loops, we use these tricks. If another language is used for implementing this algorithm, we can use Equation 3.9 with looping over Σ s to have a fast implementation of the algorithm.

3.3 BASELINE ALGORITHMS

To study the improvement of cross-domain algorithms over single-domain ones and to select the best domain matches, we need to compare cross-domain algorithms with the singledomain ones. Also, to study the performance of the proposed algorithm, we need to compare and contrast it with other state-of-the-art cross-domain algorithms. Additionally, we will study if the improvements achieved using cross-domain recommendations are because of the additional data provided to them, or because of the algorithm itself. To do this, we use both domains' data as an input to the single-domain algorithm and compare it with other cross-domain baselines and the single-domain algorithm with target domain's data.

As baseline algorithms, in addition to CD-CCA, we run the SVD++ algorithm [31]³, Rating-Matrix Generative Model (RMGM) [36], and Collective Matrix Factorization (CMF) [66] as some of the previous work compared their results to these algorithms.

3.3.1 SVD++

SVD++[31] is a single-domain algorithm, based on matrix factorization. In this algorithm, the rating matrix is decomposed into two smaller matrices: user-factor matrix (Q) and itemfactor matrix (P). This decomposition is shown in Equation 3.14. Here, \hat{r}_{ui} represents the estimated rating of user u on item i; q_i shows the user vector, e.g. the row representing user in the user-factor matrix; and p_u shows the item vector, e.g. the row representing the item in the item-factor matrix. The user-factor matrix can be interpreted as user interests in the discovered factors and the item-factor matrix shows how much each item belongs to each factor.

$$\hat{r}_{ui} = q_i^T p_u \tag{3.14}$$

This decomposition is solved as an optimization problem. The goal is to minimize the Root Mean Squared Error (RMSE) of predicted vs. actual user ratings. Since users can have a bias in their ratings (e.g. a user may rate most of the products higher than average),

³Using GraphChi Software (http://graphchi.org)

this algorithm corrects for the user bias using user averages (b_u) . Similarly, item-bias (b_i) and general bias (μ) are added to the optimization problem. In addition to these biases, there is implicit information regarding the items that users choose to rate, regardless of their rating value. To account for this information, a second set of item factors (y_j) is added to characterize users based on the set of items they have rated. Since users do not rate all of the available items, the actual user-rating matrix is sparse. Thus, SVD++ only uses the observed ratings of each user in estimating the P and Q matrices. In order to achieve this, a set R_u that represents the items rated by users is used.

Eventually, Equation 3.15 shows the final formulation for estimating user u's rating on item i.

$$\hat{r}_{ui} = \mu + b_i + b_u + q_i^T (p_u + |R(u)|^{-\frac{1}{2}} \sum_{j \in R(u)} y_j)$$
(3.15)

3.3.1.1 SD-SVD and CD-SVD In this thesis, we use SVD++ in two modes: single-domain and cross-domain. In the single domain mode (SD-SVD), we only use the target domain ratings to predict the test user ratings in the target domain. This serves as a baseline for studying if extra domain information helps in achieving better recommendations. For the cross-domain mode (CD-SVD), we add the source domain item space to the target domain item space, as if the two categories are coming from the same (single) domain. This is done by concatenating the source and target domain rating matrices. We run the SVD++ algorithm on the joined domain matrices. By studying this algorithm as a baseline for other cross-domain algorithms, we can study if the improvement of cross-domain recommenders is because of the added data of the target domain, or because of the approach to integrate this data. Figure 5 shows the cross-domain setup for the SVD++ algorithm.

3.3.2 Rating Matrix Generative Model (RMGM)

Rating Matrix Generative Model (RMGM) [36] is a generative model that creates a shared cluster-level matrix, which represents the relatedness across multiple rating matrices. In this model, rating of a user on an item is drawn from both a user-item joint mixture model and

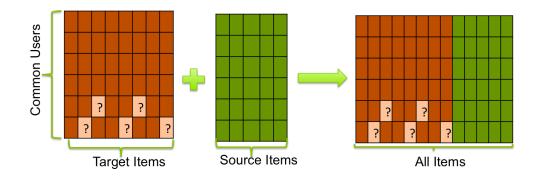


Figure 5: Cross-Domain Setup for SVD++

a corresponding ratings from this cluster-level rating model. An adaptation of Expectation Maximization (EM) algorithm is used for training the model.

This algorithm works for categorical ratings and requires to have the number of user and item clusters as its input. Since it is a generative model, it can work for unobserved or new users. However, since it relies on the shared cluster of users and items, it has problems when there is a high skewness in the ratings. When having high skewness in the ratings, users usually only rate the most popular items. In this case, the groupings of items and users based on ratings will not result in clear clusters. As a result, the error of this algorithm increases in these cases. The same happens when there is an extreme case of sparsity, or an extreme case of cold-start. RMGM will not be able to generate clear groupings of extreme cold-start users and this leads to a larger error. Additionally, RMGM does not require shared users or shared items between the source and target domains.

3.3.3 Collective Matrix Factorization (CMF)

Collective Matrix Factorization (CMF) was proposed by Singh and Gordon in 2008 [66] for learning multiple relationships in the same domain (e.g. predicting the movie ratings of users in the Netflix dataset, considering the genre relationship of movies from the Internet Movie DataBase). Although it was not proposed as a cross-domain algorithm, it has been used as a baseline in many cross-domain recommendation studies [26, 30].

This approach simultaneously factors several matrices by sharing parameters, learned for common entities in the relations, among factors. More specifically, if there are two data matrices X and Y, it factorizes these matrices into factors U, V, and Z, such that $X \approx f_1(UV^T)$ and $Y \approx f_2(VZ^T)$. To find the appropriate factors, CMF uses the L_2 losses, once for approximating X with U and V, and once for approximating Y with V and Z; and minimizes the weighted average loss over these two losses. This optimization is done by alternating projection algorithm, updating for one of the factors at each time using a Newton-Raphson step.

In the cross-domain interpretation of this algorithm, the assumption is that V represents the shared user factors, and it is shared between the source and target domains. It requires the source and target domains to have the same set of users.

CMF has problem in fitting accurate item factors for fat source and target domain rating matrices. This algorithm tries to represent user preferences, and items in both source and target domains via the same number of factors. In other words, the number of factors in V and Z are the same and equal to the number of user factors in U. Thus, if the number of users is much smaller than the number of items in the source or target domains, the number of factors to represent the tastes of a small set of users may not be enough to represent the large number of items. Also, it the number of items in the source and target domains are very different, the number of factors used to represent them may be very different. In this case, CMF has to either sacrifice the representation accuracy of one domain and use a small number of factors for both domains, or has to incorporate more factors and increase the risk of over-fitting for the domain with smaller number of items.

3.4 SUMMARY

In this chapter we introduced our proposed algorithms CD-CCA and CD-LCCA. We also presented a brief introduction to the baseline algorithms used in this thesis and explained their strengths and weaknesses.

CD-CCA and CD-LCCA are both built on canonical correlation analysis that finds the

linear interrelationships between a set of dependent and a set of independent variables. Many factorization-based recommender algorithms, including the proposed and baseline algorithms in this dissertation, work based on assuming linear relationships between item vectors or domains. Although using only linear relationships is a limitation for these algorithms, they have shown reasonable performances in recommender systems literature. However, there are ways to incorporate non-linear relationships in the proposed algorithms. One of which is using kernel-CCA [4] instead of linear CCA to find the relationship between the source and target domains. However, using kernel-CCA for recommendation requires a mapping from the source domain space to the kernel space and from the kernel space back to the target space.

Table 1 shows a summary of the proposed and baseline algorithms with some of their properties. While CD-CCA, CD-LCCA, CMF, and RMGM are all algorithms that are designed to map between two or more domains, CD-SVD is a single-domain algorithm that receives a union of source and target domain ratings as its input. CMF, CD-SVD, and SD-SVD are all based on matrix factorization models. CD-CCA is similar to these algorithms in the sense that it maps the user-item rating matrices into a lower-dimensional space. The same is true for RMGM.

RMGM does not require any shared users or items between the domains, while other cross-domain algorithms need to have shared users. Also, RMGM works on categorical input data. So, it cannot process the Supermarket dataset directly as its input. The rest of the algorithms assume to have a continuous input space. The output of these algorithms are also continuous values. Since many recommender system datasets have nominal ratings of users on items, this can be a limitation of these algorithms.

As we will see in the next chapters of this dissertation, these algorithms are different in their running times. CD-CCA, CD-LCCA, and SVD++ are among the fastest algorithms. RMGM and CMF are slower. Also, as discussed in this chapter, each of these algorithms have their own limitations. For example, RMGM performs poorly in cases of extreme coldstart, skewed, or sparse data; CMF works better in domains with tall user-item matrices, CD-SVD cannot handle the extra noise added through source domain ratings, and CD-CCA assumes that it has access to a full matrix of ratings.

Table 1: Proposed and baseline algorithms and their properties

Speed	Fact	T COD T	Dolotinoly, foot	retatively last	Vower of over	very slow		Relatively slow		Fast		
Weakness	Single domain	Singic domain	Not explicit cross-domain,	weak noise handling	weak handling of skewness,	sparsity, extreme cold-start		weak handling of fat	user-item matrices,	noise	Assumes full matrices,	needs more users vs. items
Input data type	continuous	Communación	ono tinitono	COILLINGUS	oot oom on 1	categorical		continuous		sinoitaitas o	Confininguas	
Sharing	1		Champel 1160mg	olidieu useis	No chemina	Sildilig			Shared users		Sharod 11gorg	Silated users
Approach	Matrix factorization on	target domain	Matrix factorization	Union source-target domains	Shared user-item clusters	Joint user-item mixture	and clusters	Matrix factorization,	Joint domains,	Shared user factors	CCA based factorization	COM-Dasca tactorization
Algorithm	SD-SVD		מעט מט	UV2-UV	NJNA	IUMOIM			CMF		CD-CCA and	CD-LCCA
Domain	Single	Singic	Cross									

4.0 DATASETS

We use the following three datasets for carrying our experiments in this thesis: the Yelp dataset, the Imhonet dataset, and the Supermarket dataset. Each of these datasets have different characteristics that make them suitable for our purposes and provide different views to the proposed analyses. Each of the datasets contain a different nature of items in the domains: the Yelp dataset contains user ratings or preferences on "business services", the Imhonet dataset contains user ratings or preferences on online items, and the Supermarket dataset includes the actual supermarket purchase history of customers. The Yelp and Supermarket datasets have an average size with more domains, while the Imhonet dataset is a large dataset with four domains. The Yelp and Imhonet datasets include user ratings; while the Supermarket dataset includes the amount of money the customers have spent on goods and their purchase frequency. Table 2 shows these characteristics of each of the datasets. We explain each of these datasets in the following sections.

4.1 YELP ACADEMIC DATASET

The Yelp academic dataset is available in http://www.yelp.com/academic_dataset by Yelp for academic purposes. The dataset contains user reviews on business services from various categories and subcategories. It includes a business category hierarchy with 510 unique categories and 21 parent business categories (or super categories). As an example "Active Life" is a parent category with subcategories, such as "Aquariums" and "Diving", and sub-subcategories, such as "Scuba Diving". User reviews include a textual review plus user ratings on the service. Each rating can be between one and five stars. Each business

Table 2: General Characteristics of Datasets

	Yelp	Imhonet	Supermarket	
Type of Domain	business services	online items	supermarket goods	
Type of Feedback	ratings + reviews	ratings	purchase history	
Number of Domains	21	4	22	
Data Size	average	large	average	
	(>100K)	(>1M)	(>100K)	
Average Sparsity	sparse	most sparse	least sparse	
Average Skewness	skewed	most skewed	least skewed	
Shape of User-Item Rating Matrix	tallest	both tall and fat	fattest	
Sample Domains	Restaurants, Health services, Home services	Movies, Games, Perfumes, Books	Fruits and vegetables, Outdoor appliances	

Table 3: Basic Statistics for Yelp Academic Dataset.

	Min	Max	Average	Median	Review	Average	Median	Review
	Review	Review	Review	Review	Num	Review	Review	Score
	Num	Num	Num	Num	Variance	Score	Score	Variance
Businesses	3	862	20.19	6	1874.6	3.67	3.5	0.7437
Users	0	5807	38.86	7	13901.48	3.74	3.86	0.9320

can be related to more than one categories and parent categories. For example, a restaurant can belong to both "Food" and "Restaurants" parent categories, while a grocery store only belongs to the "Foods" category. For simplicity, we consider only one parent category for each business. We try to pick the most descriptive category for each business; e.g. "Restaurants" for a restaurant.

In the Yelp academic dataset, there are 229, 908 reviews on 11, 537 businesses from 43, 874 users. The reviews are gathered from local businesses of four states: Arizona, California, South Carolina, and Colorado. Table 3 shows some basic statistics from this dataset.

Preprocessing of this dataset includes the following steps: importing the dataset from JSON format to the sparse matrix format, finding the shared users across category pairs, reducing the domain pairs' records to include only the shared users and the rated items by them, separating the category pairs with enough information for the analysis, and separation of test, train, and evaluation data.

4.2 IMHONET DATASET

Imhonet dataset is an anonymized dataset obtained from an online Russian social system called Imhonet. Imhonet is relatively unique in several aspects including its diverse nature. It allows users to rate and review a range of items from books and movies to mobile phones

Table 4: Basic Statistics for Imhonet Dataset.

	Book	Game	Movie	Perfume
user size	362448	72307	426897	19717
item size	167384	12768	90793	3640
density	2.22E-04	0.0014	7.30E-04	0.0035
record number	13438520	1324945	28281946	253948
max number of rating per user	29524	1173	30014	2436
max number of rating per item	84805	9069	87848	5336
average number of rating per user	37.0771	18.2339	6.63E+03	12.8796
average number of rating per item	80.2856	103.7708	311.4992	69.7659
median number of rating per user	20	7	20	6
median number of rating per item	3	5	5	7
var of number of rating per user	1.13E+04	1.10E+00	3.05E+04	894.296
var of number of rating per item	1.04E + 06	2.02E+05	5.48E + 06	1.01E+05

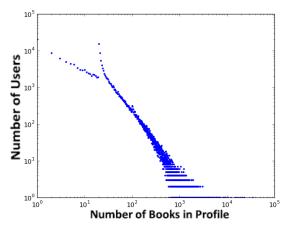
and architectural monuments¹. This system also contains many aspects of a social network, including friendships, blogs and comments. We use a dataset that includes four sets of ratings - on books, movies, games, and perfumes. Each rating record in the dataset includes a user ID, an item ID, and a rating value between zero (not rated) and ten. The same user ID indicates the same user across the sets of ratings.

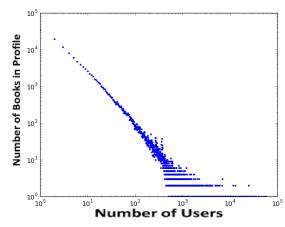
Figure 6 (a) shows the scale of the number of book ratings per user in log-log coordinates and Figure 6 (b) shows the number of ratings for each book. As the figure shows, the plot of number of user raters per book follows the usual power law distribution. But the plot of the number of book ratings per user does not follow a usual pattern. It looks like a combination of two distributions. The same phenomenon happens in the other domains. This peculiar shape is produced by two interfaces for new users that Imhonet offered at different times. One interface asked each new user to rate at least 20 books and movies to receive recommendations. Another interface allowed exploring the system right away adding ratings one by one. To preprocess this dataset we should find the shared users across category pairs, reduce the domain pairs' data to include only the shared users and the rated items by them, separate the category pairs with enough information for the analysis, and separate the test, train, and evaluation data.

4.3 SUPERMARKET DATASET

This dataset includes the purchase history of some customers in a large-scale Supermarket in Australia. The data has been gathered during a health study from the Supermarket employees and offered them a 10% discount on fruit and vegetables as part of a health program. The date range is from January 1, 2014 to 31 December, 2014. It is an anonymized dataset of 1,529,055 records of 1,589 customers purchasing 35,638 items. The number of unique user-item purchase records is 736,416. The number of items in this dataset is much larger than the number of customers and the dataset is very sparse. As a result, the dataset

¹Recently, Imhonet has limited its domains to movies, TV shows, TV series, games, and books. However, we have access to some of its previous domains' data





- (a) Log-log scale of the number of book ratings of users (showing the number of Users having K number of books rated)
- (b) Log-log scale of the number of ratings on books (showing the number of books having K number of users rating them)

Figure 6: Distribution of ratings in the book domain

needs to be cleaned to remove the items with too few purchase records. Additionally, there are return transactions in the data that should be removed from it. The items are categorized into 204 fine-grained categories, such as "salad bar", "sushi", "baby wear", "laundry", and "floral". The number of records in each category, ranges from one to 111,485. Since the categories are fine-grained and, in some cases, overlapping, we should redefine the categories manually. To do this, we categorize the data into 22 main domains. The mapping of this categorization is shown in Appendix A. A summary of basic statistics for the Supermarket domains is shown in Table 5. The purchase history data includes the quantity of purchase and the amount of money spent on the purchase. To convert this data into preference data, we use tf-idf (term frequency-inverse document frequency) statistics on the item purchase frequency. More specifically, we first build user vectors in the item space by counting the number of times each item is bought by each customer. Then, we discount these vectors by the total number of times that each item has been bought. Eventually, we normalize the user vectors such that the values of purchases for each customer is between zero and one.

Table 5: Basic Statistics for Supermarket Dataset

domain name	number of customers	number of items	number of distinct customer-items records	number of records	density
breads	1519	612	25571	59388	0.0275
alcoholic drinks & cigarrettes	217	306	580	1690	0.0087
beauty	1476	3178	33827	48371	0.0072
canned and pickled	1448	929	23920	45699	0.0177
cooking essentials	1506	1748	48094	71646	0.0182
clothing	1026	3757	7518	8459	0.0019
dairy	1535	1150	36190	105287	0.0205
discounts and coupons	1223	504	8479	20504	0.0137
events	913	505	4264	4870	0.0092
fish, meat, poultry and eggs	1536	2080	66848	149008	0.0209
fruit and vegetables	1549	980	95166	309040	0.0626
gifts	1122	573	5308	6316	0.0082
health	1456	1511	20827	31877	0.0094
home indoor	1454	2129	19999	25101	0.0064
home outdoor	1103	518	5596	6821	0.0097
international food	1358	1185	15091	24230	0.0093
leisure	1121	1330	5872	11723	0.0039
pets	1051	1131	12312	31085	0.0103
prepared meals and snacks	1563	5452	140042	269454	0.0164
soft drinks, tea and coffee	1534	1705	37201	85771	0.0142
sweets	1550	2805	84612	151827	0.0194

In summary, preprocessing of this dataset includes cleaning the data, re-defining the categories into domains, aggregating the purchase history in time into unique customer-item purchases, converting the purchase history into tf-idf preference data, finding the shared customers across category pairs, reducing the domain pairs' records to include only the shared customers and the rated items by them, separating the category pairs with enough information for the analysis, and separation of test, train, and evaluation data.

4.4 SUMMARY

In summary, we are using three different datasets with various characteristics in this dissertation: the Supermarket purchase dataset, the Yelp academic dataset, and the Imhonet dataset.

As we have seen in Table 2, these datasets have different sizes: Yelp and Supermarket datasets are average in size and Imhonet is a large-scale dataset. The nature of domains in these datasets is different: in Yelp, we see user preferences on a whole business service. Thus, there is no specific item that users rate in Yelp. For example, users rate a restaurant based on various factors in the restaurant. But, they do not rate each of the foods that have been served in the restaurant. The Supermarket dataset does not include any ratings. Customer purchase histories and their frequencies are represented in this dataset. Thus, we do not see any user preference in the form of rating in this dataset. The feedback we have in this dataset is of an implicit format. Imhonet is the most standard recommender systems dataset among the three: It includes user preference ratings on each of the items. In such a dataset, not only users purchase or consume an item, but also decide to express their preference on that item by rating it. Consequently, the ratings in datasets with explicit ratings are usually more skewed: users tend to rate the items they like more. Although Imhonet is a typical recommender system dataset, working with it is more difficult because of its large size and few number of domains.

To have a more global view of the differences among these datasets, we show some of their characteristics in the following figures.

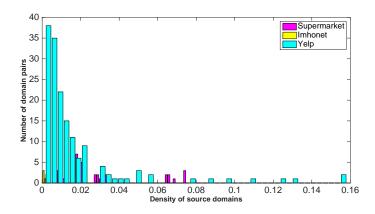


Figure 7: Density of domains in each of the datasets

Figure 7 shows the density of user ratings in different domains in each of the datasets. As we can see in this picture, the Imhonet dataset is very sparse. Also most of the domains have a similar density in this dataset. The Yelp dataset, is also sparse, but less than the Imhonet dataset. In this dataset, most of the domains are very sparse, while there are some domains with much more density. The density of the Supermarket dataset is more than both Yelp and Imhonet datasets. Also, the distribution of densities looks flatter compared to the Yelp dataset.

Figure 8 shows the ratio of number of users to number of items in the domains of each of the datasets. Here, we can see that the number of users compared to number of items can be much larger in the Yelp dataset compared to the other ones. In these cases, the user-item rating matrix, is a tall matrix. However, there are many domains in which the user-item matrix is not very tall in the Yelp dataset. In the Supermarket dataset, we mostly see fat user-item matrices. The ratio of users to items is mostly small in the Supermarket dataset. For the Imhonet dataset, we see both tall and fat user-item matrices for different domains. However, in some of the domains, this ratio is much smaller than the other two datasets.

If we look at the distribution of number of users in the domains, we notice that this distribution is more flat in the Imhonet and Supermarket datasets compared to the Yelp dataset. It means that there are many domains in the Yelp dataset with a few number of

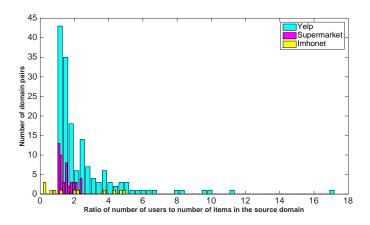


Figure 8: Number of users to number of items ratio in each of the datasets

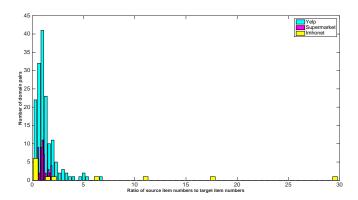


Figure 9: Number of source domain items to number of target domain items in each of the datasets

users and some domains with many users.

Also, looking at Figure 9, we can see that the Imhonet dataset has the maximum ratio of source domain items to target domain items. When this ratio is larger, we have a fatter user-item matrix in the source domain, compared to the target domain. It means that the number of items in domains of Imhonet vary more than the other two datasets. We can see that the Supermarket dataset has the least values for ratio of source domain items to target domain items. As a result, the source domain user-item matrices are not as fat, compared to the target domain user-item matrices.

We expect to see different behaviors in the results for each of these datasets because of their different characteristics. In the following chapters, we analyze how each of the differences can produce different results.

5.0 GENERAL EXPERIMENTS: CD-CCA VS. BASELINE ALGORITHMS

The goal of this chapter of thesis is to answer the research question Q1.1. More specifically, we would like to see if the additional data available to cross-domain recommenders help us to provide better recommendations to users; if the cross-domain recommenders can harm the recommendation performance; if there is a cross-domain recommender system that can perform better than other cross-domain recommender systems; and if the improvement we get from the cross-domain recommendations are because of the additional provided data or the properties of the cross-domain algorithm.

To find an answer to the above questions, we use CD-CCA (and CD-LCAA), as one of the cross-domain algorithms, in addition to other state-of-the-art cross-domain and single-domain algorithms that are mentioned in Section 3.3. We compare the performance of these algorithms using Root Mean Squared Error (RMSE) and Mean Absolute Error (MAE) of the recommended items. To understand the effect of having additional data on the recommendation performance, we apply the single-domain algorithm only on the target domain data and the cross-domain algorithms on both source (auxiliary) and target datasets and compare their results. Additionally, to understand the effect of approach on the recommendation results, we apply the single-domain algorithm on a combination of source and target data to have a fair comparison with cross-domain algorithms. This setting is shown in Figure 10. In the next step, we examine the correlation between these algorithms' performances, on the available domain-pairs in the data, to understand if an increase in the performance of each of the algorithms can lead us to an increase in other algorithms' performance.

Our hypothesis in this part of analyses is:

• It is possible that adding additional domains' data harm the recommendation results;

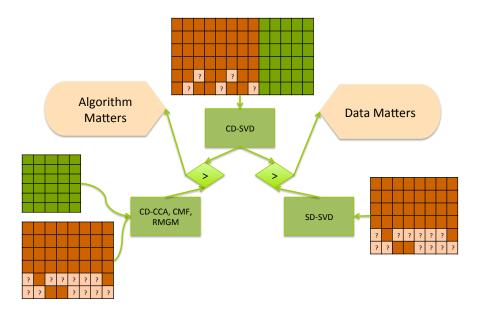


Figure 10: Experiment setup to answer research question Q1.1

- However, using auxiliary material, if selected and applied correctly, should either improve or preserve the performance of recommender systems;
- The performance of single-domain and cross-domain recommenders are correlated with each other due to the data characteristics;
- However, the improvement achieved by using auxiliary data depends also on the applied algorithm.

In the following sections, we present the results of our proposed and baseline algorithms on each of the datasets.

5.1 EXPERIMENT SETUP

To run the experiments on each of the datasets, we implement a user-stratified 5-fold cross-validation setting. The user-stratified setting is used to represent a common situation that happens with recommender systems: we would like to predict the ratings of some (probably

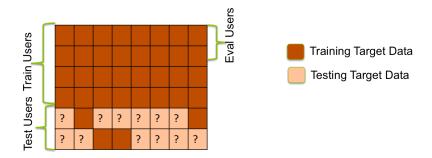


Figure 11: Separating test, train, and evaluation data from the target domain

new) users, given that we have the ratings of other (probably similar) users. As a result, some of the users (20%) are selected as test users and the rest of them (80%) are selected as training users. 80% of the ratings for the test users on the items in target domain is removed randomly from the training dataset. The algorithms approximate this 80% of test user ratings based on the training set. Eventually, the approximated test ratings are compared to the real ones to calculate the error of algorithms.

The reason to remove 80% of test user ratings, and not all of their ratings, is to avoid the extreme cold-start case and to be able to perform a cold-start analysis on the user profile sizes. Thus, we use a random 20% selection of each test user's rating and estimate the rest of test users' ratings (the removed 80%) conditioned on observing this 20% of their ratings and the ratings of users in the training set. Having this setting, if a test user has a large profile in the target domain, we will have more information on this user, compared to another test user with a small target domain profile. Consequently, the distribution of profile sizes among the test users is a factor of the gold-start profile sizes distribution. Thus, the amount of information that we have from the test users is kept in accordance with the amount of information we have from them as the gold-standard. This allows us to perform a cold-start analysis that is similar to the real-world setting: some new users are active and have more ratings in the beginning of using a system, while others have less ratings.

Some of the algorithms have parameters that should be selected by cross-validation. For example, the number of components should be provided as an input to the SVD++

algorithms. To find the best set of parameters for each algorithm, we remove a "validation" set of ratings from the training data. Selection of this validation set is in accordance with selection of the test set; we select 15% of users as validation users and remove 80% of their ratings from the training set. Then, we train the algorithms with different values of parameters on the remaining training ratings and test it over the validation dataset to select the parameters that result in the best performance.

After selecting the best parameters, we add the validation set data to the training set; train the algorithms based on this new training dataset; and test it on the test data of the removed 20% of users. Figure 11 shows a toy example of separating the test, train, and evaluation data in a target domain.

We repeat these experiments 5 times, each time selecting a different set of test users, for the 5-fold cross-validation. Eventually, we average over the performance of algorithms in these 5 times and report it.

For the single-domain algorithm, we use only the target domain dataset. However, for cross-domain algorithms, we have both source and target datasets. To be able to compare single and cross-domain algorithms, we remove the same set of ratings for all of the algorithms. Thus, for each test user in the cross-domain algorithms, we have all of the users' ratings from the source domain, plus 20% of her ratings in the target domain, as training data. The remaining 80% of test user's target domain ratings is what we test the algorithms on.

To measure the performance of algorithms, we use Root Mean Squared Error (RMSE) and Mean Absolute Error (MAE). Although there are other performance measures, such as ranked-based measures like nDCG, precision, and recall, that can be used in the recommender systems field, we choose RMSE and MAE because of the way we formalize our problem. The proposed algorithms are formulated as estimating user ratings over the items. Consequently, the closeness of the estimated rating to the real rating is the measure that is important to us. If R is the set of test ratings, $r_{u,i}$ is the rating of user u on item i, and \hat{r} is the estimated rating by the algorithm, then RMSE and MAE can be calculated as in Equations 5.1 and

5.2.

RMSE =
$$\sqrt{\frac{\sum_{R}(r_{u,i} - \hat{r}_{u,i})^{2}}{|R|}}$$
 (5.1)

$$MAE = \frac{\sum_{R} abs(r_{u,i} - \hat{r}_{u,i})}{|R|}$$
(5.2)

Since we have normalized vectors of purchase frequencies in the Supermarket dataset (instead of user ratings), we cannot use the RMGM algorithm directly on this data. The frequency rates in the Supermarket dataset are normalized and have a value between zero and one. To run RMGM on this dataset, we convert these frequencies to a 10-scale categorical values. To do this, we multiply each of the normalized frequency values by ten and use the ceiling value of it.

5.2 RESULTS OF THE SUPERMARKET PURCHASE DATASET

In this section we compare the result of the proposed cross-domain algorithm (CD-CCA) with the baseline cross-domain and single-domain algorithms. As mentioned in Section 4.3, we use the 22 parent categories as domains for cross-domain recommendation. Considering each domain once as the source domain and once as the target domain, we end up with 462 domain pairs. However, we run the experiments only on the domain pairs that have larger number of users compared to items (in both source and target domains). Consequently, we end up with 50 domain pairs in this dataset. These 50 domain pairs, and some basic statistics are presented in Tables 37 to 39 in Appendix A.2.

As explained in Section 5.1, we use user-stratified 5-fold cross-validation to run each of the algorithms on each of the domain pairs. The results of running algorithms on domain pairs is presented in Table 40 of Appendix A.3.

To have a better global view of these results, we plot the RMSE of these five algorithms on each of the domains in Figure 12 and the MAE of these algorithms in Figure 13. The X-axis shows each of the domain pairs and the Y-axis shows the error reported by the

algorithms. The domain pairs are ordered based on CD-CCA's error on them. The reported errorbars are for p-value < 0.05 based on the 5-fold cross-validation. As we can see in these pictures, RMGM (shown with yellow star marker) and CD-CCA (shown with red circle marker) perform significantly better than other algorithms, in most of the domain pairs. RMGM performs by far better than other algorithms in most of the domain-pairs. While these two cross-domain algorithms perform well, CD-SVD (shown with blue square markers) and CMF (shown with purple cross markers) algorithms have a high error rate in most of the domain pairs. In many cases, the single-domain SD-SVD algorithm (shown with green diamond markers) performs better than these two cross-domain algorithms.

To be more exact, we can look at the number of domain pairs in which each of the two algorithms have a significant difference in their reported error. Table 6 shows this relationship between RMSE of algorithms and Table 7 shows it between MAE of them. The table cell related to i^{th} row and i^{th} column shows the number of domain pairs in which the i^{th} algorithm performed significantly better than the j^{th} algorithm. The last column (row) of the table shows the total number of domain pairs in which the algorithms performed significantly better (worse) than other algorithms. Thus, the higher column-sum and the lower row-sum of an algorithm indicates a generally better performing algorithm in all of the domain-pairs. As we can see in these tables, RMGM is better than other algorithms in 149 comparisons on domain pairs, measured by RMSE, and 159 comparisons, measured by MAE. In 32 and 30 domain pairs RMGM performs significantly worse than other domain pairs measured by RMSE and MAE, respectively. CD-CCA is the next-best algorithm, performing significantly better than other algorithms in 129 and 109 comparisons on RMSE and MAE of domain pairs. CMF is the worst algorithm on this dataset and CD-SVD is the second worst algorithm in terms of the number of domain pairs with significantly higher RMSE and MAEs.

As an interesting observation based on Tables 6 and 7, none of the cross-domain algorithms are always better than the single-domain algorithm. Although the number of domain pairs in which the cross-domain algorithms perform better than SD-SVD varies, there are always some domain-pairs in which SD-SVD performs better than the cross-domain algorithms. Even RMGM, which is the best-performing cross-domain algorithm in this dataset,

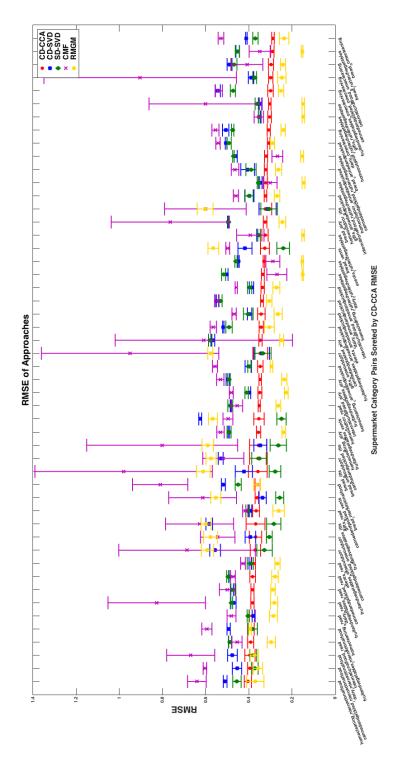


Figure 12: RMSE of algorithms on 50 Supermarket domain pairs ordered by the RMSE of the CD-CCA

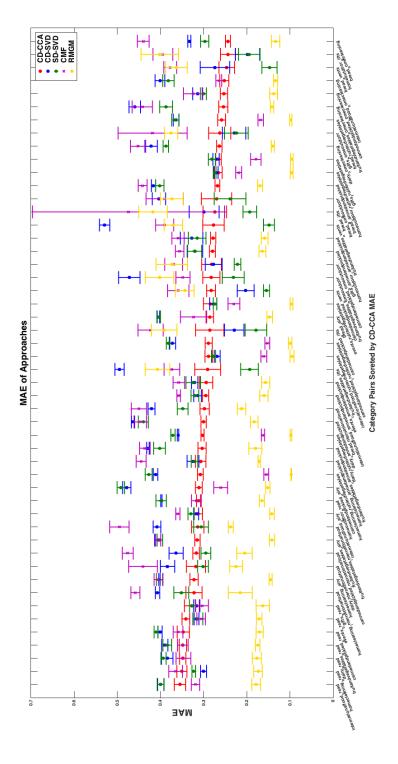


Figure 13: MAE of algorithms on 50 Supermarket domain pairs ordered by the MAE of the CD-CCA

Table 6: Number of domain pairs with significant RMSE difference among algorithms. Each row shows the number of domain pairs in which the algorithm of that row works significantly better than the algorithms mentioned in the columns.

RMSE	CD-CCA	CD-SVD	SD-SVD	CMF	RMGM	SUM
CD-CCA	0	42	35	41	11	129
CD-SVD	0	0	4	27	8	39
SD-SVD	7	20	0	31	11	69
CMF	3	9	7	0	2	21
RMGM	35	40	36	38	0	149
SUM	45	111	82	137	32	

Table 7: Number of domain pairs with significant MAE difference among algorithms. Each row shows the number of domain pairs in which the algorithm of that row works significantly better than the algorithms mentioned in the columns.

MAE	CD-CCA	CD-SVD	SD-SVD	CMF	RMGM	SUM
CD-CCA	0	34	27	30	11	102
CD-SVD	6	0	3	19	7	35
SD-SVD	12	19	0	28	11	70
CMF	11	19	17	0	1	48
RMGM	39	42	39	39	0	159
SUM	68	114	86	116	30	

performs significantly worse than SD-SVD in 11 domain pairs out of the 50 domain pairs.

Another interesting observation is that there is no absolute best algorithm for this dataset. Looking at both of these tables, we can see that there is no row or column with all-zero values. This means that there is no algorithm that always performs significantly better than (or similar to) other algorithms. The only case in which one of the algorithms always performs significantly better or similar to another one is CD-CCA compared to CD-SVD based on RMSE. In none of the domain pairs, CD-SVD performs significantly better than CD-CCA.

Tables 41 and 42 in Appendix A.3 show a detailed view of comparison of algorithms in each of the domains. Each column of these tables ("Alg A > Alg B") shows in which domains the left-hand side algorithm ("Alg A") is performing better than the right-hand side one ("Alg B"). As we can see, there are $1000 = 50 \times 20$ cells in each of the tables, representing the combination of domain pairs with each two of the algorithms. Out of these 1000 combinations, the two tables are different in 103 cells. This means that, in the 897 remaining experiments, the algorithms performed similarly compared to each other, given either RMSE or MAE error measures. Also, we do not see any algorithm that performs better than any other algorithm in all of the domain pairs (otherwise, we would have had the value 50 in the reported tables).

As we can see in these tables, there are 16 domain pairs in which all of the cross-domain algorithms perform either significantly better than, or similar to, SD-SVD based on the RMSE measure. Looking at the MAE measure, there are 20 domain pairs in which adding the source domain information, using all of the cross-domain algorithms, either increases the performance significantly, or does not change it. As example of these domain pairs, we can name "bread \rightarrow 1 dairy", "dairy \rightarrow fruit and vegetables", and "international food \rightarrow home cleaning". There are four domain pairs in which the RMSE and MAE measures are not agreeing on, in terms of having all cross-domain algorithms performing better than SD-SVD. An example of these domain pairs is "canned and pickled \rightarrow home cleaning". While CMF works similar to SD-SVD based on MAE measure in this domain pair, the RMSE of

¹The arrow shows the direction of transferring information from the source domain to the target domain. The left-hand side domain is the source domain; and the right-hand side one is the target domain.

SD-SVD is significantly better than CMF.

Also, there are 6 and 8 domain pairs in which SD-SVD performs significantly better than all of the cross-domain algorithms based on the RMSE and MAE measures respectively. "bread \rightarrow events", "canned and pickled \rightarrow gifts", and "fruit and vegetables \rightarrow gifts" are examples of these domain pairs. The disagreement between RMSE and MAE measures, in SD-SVD performing better than all of the cross-domain algorithms, comes from the "bread \rightarrow gifts" and "fruit and vegetables \rightarrow home outdoor" domain pairs. While SD-SVD performs significantly better than CD-CCA based on RMSE in "fruit and vegetables \rightarrow home outdoor", they do not have a significant difference using MAE measure. For the "bread \rightarrow gifts" domain pair, the disagreement is on comparing SD-SVD and CMF algorithms.

Although there are significant differences between the performances of algorithms, in many cases their errors on domain pairs are correlated with each other. Table 8 shows the correlations between the RMSE of these algorithms. The numbers with star represent a significant correlation with p-value < 0.01. Figure 14 shows the scatter plot of RMSE of these algorithms of all of the domain pairs. The general observation with the correlation between RMSE of algorithms in this dataset suggests that the correlation among cross-domain RMSEs are either significantly positive or non-significant. However, the correlations between SD-SVD and cross-domain algorithms is mostly negative. The exception is the correlation between RMSE of SD-SVD and CD-SVD. Despite other cross-domain algorithms, CD-SVD's RMSE is higher when SD-SVD works worse; and vice versa. A similar pattern can be seen in the correlation of MAE of these algorithms on the Supermarket dataset. Figure 15 shows the scatter plot of MAE of algorithms in all of the domains. We can see that the cross-domain algorithms are positively correlated with each other.

5.3 RESULTS OF THE YELP DATASET

In the Yelp dataset, we have 21 parent categories. We use the star ratings of reviews within each category. For each pair of categories, we find out the common users (the users who have rating reviews in both of the selected domains). To obtain more reliable results, we exclude

Table 8: Correlation between RMSE of algorithms on all domain pairs in the Supermarket dataset

RMSE Correlation	CD-CCA	CD-SVD	SD-SVD	RMGM	CMF
CD-CCA	1	0.199	-0.0537	0.39*	0.1702
CD-SVD	0.199	1	0.4342*	0.0679	-0.045
SD-SVD	-0.0537	0.4342*	1	-0.6734*	-0.2906
RMGM	0.39*	0.0679	-0.6734*	1	0.5049*
CMF	0.1702	-0.045	-0.2906	0.5049*	1

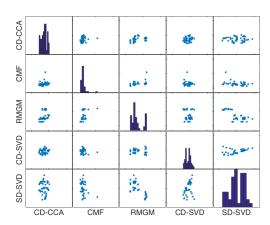


Figure 14: Scatter plot of RMSE of algorithms on 50 Supermarket domain pairs

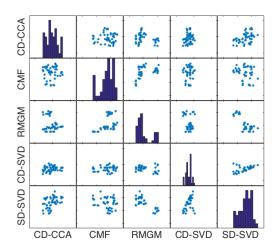


Figure 15: Scatter plot of MAE of algorithms on 50 Supermarket domain pairs

the category pairs, within which the number of common users is smaller than the number of items in any of the two categories. For each pair of categories, we run the experiments twice: once with the first category as the source and the second category as the second domain, and once the other way around. Eventually, we end up with 158 category (domain) pairs. A summary of these data statistics is shown in Table 9.

Table 9: Summary of domain pair statistics in Yelp dataset

	Min	Max	Mean	Median
User Size	9	11013	1064.09	424
Item Size	8	4435	406.89	252.5
Rating Density	0.0017	0.1581	0.017	0.0084

We run CD-CCA, CD-SVD, CMF, and RMGM cross-domain algorithms and SD-SVD single-domain algorithm on the 158 domain pairs in the data. We evaluate the algorithms based on RMSE and MAE. Figure 16 shows the RMSE of all three algorithms on the 158 domain pairs, including the 95% confidence interval; and Figure 17 shows the MAE of the

algorithms on these domain pairs. To better comprehend the difference between algorithms, we order the domain pairs based on RMSE and MAE of CD-CCA algorithm on them. Due to the visualization limitations, we cannot show the name of all domain pairs in the picture.

However, it can be seen that in most of the domain pairs, CD-CCA has a lower RMSE compared to both cross-domain and single-domain algorithms. More specifically, CD-CCA always performs significantly better or similar to SD-SVD and CD-SVD, in terms of RMSE. Compared to RMGM and CMF, CD-CCA has a significantly lower RMSE in 112 and 46 of the domain pairs, respectively. The number of domains in which there is a significant difference (0.05 p-value) between RMSE of algorithms are listed in Table 10. Each cell of the table shows the number of domain-pairs in which the algorithm mentioned in its row performs better that the algorithm mentioned in its column. As we can see in the table, CD-CCA and CD-SVD always perform significantly better than the single-domain algorithm (SD-SVD) in terms of RMSE. However, the RMSE in CMF and RMGM is sometimes (in 18 and 83 domain pairs) significantly higher than the single-domain algorithm. Based on the sum of the number of significant differences in domain-pair RMSEs, we can see that CD-CCA is performing better than all of the baseline algorithms: it has the most sum of significantly better RMSE on domain-pairs, and least sum of significantly worse RMSE. CMF is the next best algorithm based on this measure. However, looking at Figure 16, we can see that CMF has a fluctuating and non-steady behavior, compared to other algorithms. In some of the domain-pairs, CMF performs much better than all other algorithms. While in others, it works much worse than the rest. In other words, when there is a significant difference between RMSE of CMF and other algorithms, this difference is mostly large. Additionally, the errorbars for the results of CMF, when it performs poorly, are very wide. This shows that the results of CMF are not as reliable in these domain pairs. Also, we can see that although RMGM performs significantly better than CD-CCA and CMF in 4 and 11 domain-pairs, it is the worst algorithm in terms of the sum of number of significant relationships between RMSE of algorithms.

Table 47 in Appendix B.2 shows the significant comparison details of algorithms, based on RMSE, in each of the domain pairs. Based on this table, there are 67 domain pairs in which all of the cross-domain algorithms are working significantly better than the single-

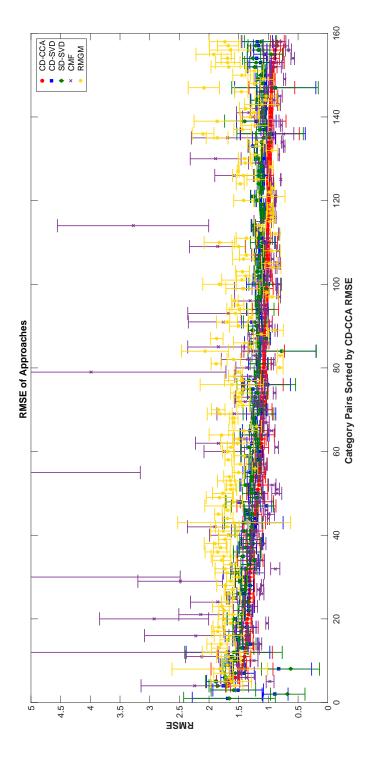


Figure 16: RMSE of algorithms on 158 Yelp domain pairs ordered by the RMSE of the CD-CCA

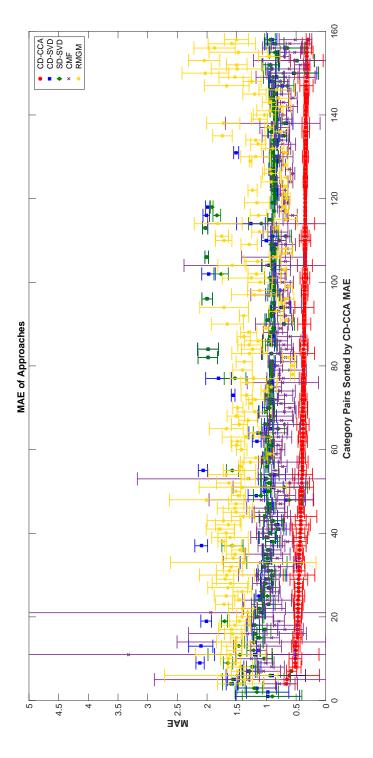


Figure 17: MAE of algorithms on 158 Yelp domain pairs ordered by the MAE of the CD-CCA

Table 10: Number of domain pairs with significant RMSE difference among algorithms for the Yelp dataset. Each row shows the number of domain pairs in which the algorithm of that row works significantly better than the algorithms mentioned in the columns.

Significant RMSE difference	CD-CCA	CD-SVD	SD-SVD	CMF	RMGM	SUM
CD-CCA	0	74	77	33	112	296
CD-SVD	0	0	9	22	87	118
SD-SVD	0	0	0	18	83	101
CMF	46	75	73	0	91	285
RMGM	4	18	19	11	0	52
SUM	50	167	178	84	373	

domain algorithm. As examples of these domain pairs, we can name "Active Life \rightarrow Home Services", "Beauty & Spas \rightarrow Arts & Entertainment", and "Hotels & Travel \rightarrow Nightlife". Since CD-CCA always works significantly better, or similar, to SD-SVD, there is no domain pair in which the single-domain algorithm performs better than all of the cross-domain ones.

Although CD-CCA is generally having a lower RMSE compared to the baselines, there are only 13 domain pairs in which CD-CCA performs significantly better than all of the baseline algorithms. These domain pairs include "Nightlife \rightarrow Food", "Active Life \rightarrow Arts & Entertainment", and "Arts & Entertainment \rightarrow Event Planning & Services".

Looking at the MAE of these algorithms in Figure 17, we can see that CD-CCA is performing by far better than all other algorithms in all domain pairs. CMF is the next best algorithm in terms of MAE and RMGM is the worse one. Looking at the details of number of domain pairs with a significantly different MAE for each two algorithms in Table 11, we can see that CMF and CD-CCA cross-domain algorithms always perform significantly better than, or similar to, the SD-SVD single-domain algorithm. However, in 14 and 86 domain pairs, the single-domain algorithm performs better than RMGM and CD-SVD. In the MAE results, we see less fluctuation for the CMF algorithm, compared to the RMSE

results. However, we can still see the wide errorbars in some of the domain pairs.

Looking at Table 47 in Appendix B.2, we can see that in 63 of the domain pairs, MAE of all cross-domain algorithms is better than MAE of the single-domain algorithm. These domain pairs include "Public Services & Government \rightarrow Mass Media", "Pets \rightarrow Event Planning & Services", and "Health & Medical \rightarrow Active Life". This number is less than the number of domain pairs with the RMSE-based comparison of all cross-domain algorithms versus the single-domain one. This disagreement comes from domain pairs such as "Active Life \rightarrow Arts & Entertainment", "Arts & Entertainment \rightarrow Nightlife", "Automotive \rightarrow Event Planning & Services", "Beauty & Spas \rightarrow Active Life", and "Education \rightarrow Arts & Entertainment". In some of these domain pairs all cross-domain algorithms are significantly better than SD-SVD, measured by RMSE (MAE), while not all of them are significantly better than SD-SVD measured by MAE (RMSE).

In contrast to the low number of domain pairs in which CD-CCA had a significantly better RMSE compared to all other baselines, CD-CCA is having a significantly less MAE in 119 domain pairs. Some of the domain pairs in which CD-CCA performs better measured by MAE, compared to RMSE, are "Active Life \rightarrow Automotive", "Arts & Entertainment \rightarrow Beauty & Spas", and "Nightlife \rightarrow Shopping".

The difference between the MAE and RMSE results can be because of their emphasis on different types of errors. While in the MAE measure the error calculated on all of the datapoints are weighted equally, the RMSE measure puts more weight on the larger errors per datapoint. Based on the above-mentioned results, CD-CCA performs better when using the MAE measure compared to the RMSE measure. On the other hand, CMF works generally better when measured by RMSE compared to MAE. This can mean that there are less large errors happening in the CMF algorithm compared to CD-CCA; However, the total of error made by CD-CCA is smaller than CMF.

We calculate the correlation between error rates of all algorithms in all of the domain pairs (Table 12 and Figure 18). Based on these results, the RMSE of algorithms (except for CMF and RMGM) are significantly correlated. Most notably, the RMSE of SD-SVD and CD-SVD are highly correlated. This correlation is smaller between CD-SVD and SD-SVD with CD-CCA, RMGM, and CMF. We can conclude that if the RMSE of single-domain recommender

Table 11: Number of domain pairs with significant MAE difference among algorithms for the Yelp dataset. Each row shows the number of domain pairs in which the algorithm of that row works significantly better than the algorithms mentioned in the columns.

MAE	CD-CCA	CD-SVD	SD-SVD	CMF	RMGM	SUM
CD-CCA	0	148	148	122	153	571
CD-SVD	0	0	6	0	86	92
SD-SVD	0	14	0	0	86	100
CMF	0	67	25	0	91	183
RMGM	0	30	25	4	0	59
SUM	0	259	204	126	416	

Table 12: Correlation of RMSE of algorithms with each other. *: significant with p-value < 0.01; **: significant with p-value < 0.001; ***: significant with p-value < 0.0001

***: p <0.0001;	CD-CCA	CD-SVD	SD-SVD	RMGM	CMF
**: p <0.001; *:p<0.01		CD S V D		10111 (3111	01/11
CD-CCA	1	0.7896***	0.7779***	0.4384***	0.2925***
CD-SVD	0.7896***	1	0.955***	0.2484*	0.285***
SD-SVD	0.7779***	0.955***	1	0.2729***	0.2536**
RMGM	0.4384***	0.2484*	0.2484***	1	0.1217
CMF	0.2925***	0.285	0.2536***	0.1217	1

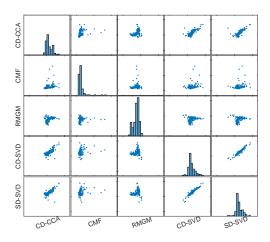


Figure 18: Scatter plot of RMSE of algorithms on 158 Yelp domain pairs

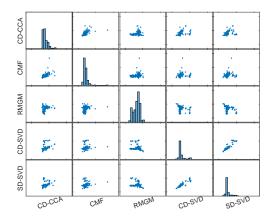


Figure 19: Scatter plot of MAE of algorithms on 158 Yelp domain pairs

is low in the target domain, it is also most likely low for cross-domain recommenders, and vice versa. There is a similar correlation between MAE of these algorithms (Figure 19).

5.4 RESULTS OF THE IMHONET DATASET

We have four domains in the Imhonet dataset: books, movies, perfumes, and games. Users can use a rating scale to rate the items in each of these domains from 0 to 10. For ease of comparison among the algorithms and datasets, we normalize ratings by dividing them by the maximum possible rating (10), so that all of them are between zero and one.

Having only four domains, we can have only 12 domain pairs to study on. Since this is a small number of domain pairs compared to the other two datasets, we do not exclude any domain pairs from our analysis of Imhonet dataset. This means that in these domain pairs, the number of users can be smaller than the number of available source or target items. However, for each of the domain pairs, we select the users that have at least one rating in each of the domains and run the experiments on that set of users. Some of the statistics of domain pairs in the Imhonet dataset are presented in Tables 48 to 51 in Appendix C.1. As we can see, in none of the domain pairs, the number of users are more than both source and target domain items.

Based on this table, the Imhonet dataset is much larger than the other two datasets that we are using in this thesis. Especially, the movies and books domains include many users and items. On the other hand, CD-CCA algorithm requires a large memory for loading the data matrices to compute the canonical correlation between the domains. Consequently, we cannot use the regular CD-CCA algorithm for this dataset and we use CD-LCCA instead of it. For the same reason, it is very difficult to run RMGM and CMF algorithms on this dataset, especially considering the running time of these algorithms. Also, running each of these algorithms require a sparse implementation of them. For these reasons, we omit running CMF and RMGM on Imhonet and only compare the results for CD-LCCA, CD-SVD, and SD-SVD. However, we use the name CD-CCA instead of CD-LCCA in the following sections for simplicity.

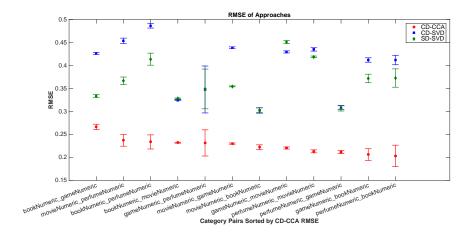


Figure 20: RMSE of algorithms on 12 Imhonet domain pairs ordered by the RMSE of the CD-CCA

Figures 20 and 21 show the RMSE and MAE of algorithms on the 12 domain pairs of Imhonet, sorted by the error of CD-CCA. As explained in previous sections, the reported errorbars represent a 95% confidence interval for the errors.

As we can see in these figures, the single-domain algorithm performs better than, or similar to, CD-SVD in many domains. Only in "book \rightarrow movie" and "game \rightarrow movie" domain pairs, we see that CD-SVD is significantly better than SD-SVD. However, CD-CCA performs significantly better than both CD-SVD and SD-SVD in all of the domain pairs.

Also, we can see that in most of the domain pairs the confidence intervals are small. Except for "game \rightarrow perfume" and "perfume \rightarrow book" domain pairs, the confidence interval for domain pairs are small. Table 13 shows the number of domain pairs in which each of the algorithms (in rows of the table) is working significantly better than other algorithms (in columns of the table). Note that both RMSE and MAE of algorithms in the Imhonet dataset has the same relationship that is represented in this table. So, in general CD-CCA is the best-performing algorithm in this dataset and SD-SVD is the next best one.

As we have seen in the previous sections, the error of these algorithms are correlated with each other. Figures 22 and 23 show the scatter plots of RMSE and MAE of algorithms in the 12 domain pairs.

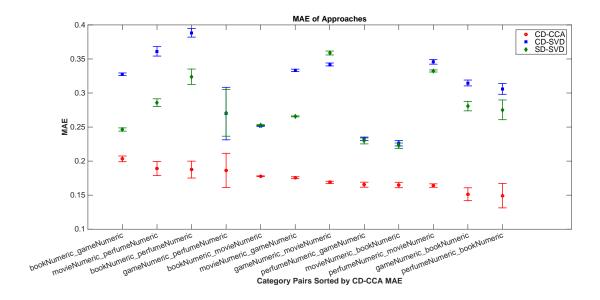


Figure 21: MAE of algorithms on 12 Imhonet domain pairs ordered by the MAE of the CD-CCA

Table 13: Number of domain pairs with significant error difference among algorithms for the Imhonet dataset. Each row shows the number of domain pairs in which the algorithm of that row works significantly better than the algorithms mentioned in the columns.

	CD-CCA	CD-SVD	SD-SVD	SUM
CD-CCA	0	12	12	24
CD-SVD	0	0	2	2
SD-SVD	0	7	0	7
SUM	0	19	14	

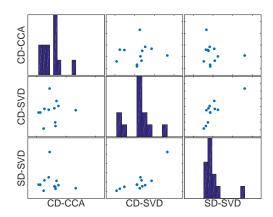


Figure 22: Scatter plot of RMSE of algorithms on 12 Imhonet domain pairs

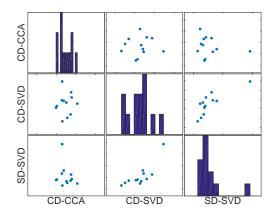


Figure 23: Scatter plot of MAE of algorithms on 12 Imhonet domain pairs

Table 14: Correlation of RMSE of algorithms with each other in the Imhonet dataset. *: significant with p-value < 0.01.

	CD-CCA	CD-SVD	SD-SVD
CD-CCA	1	0.1993	-0.1909
CD-SVD	0.1993	1	0.7416*
SD-SVD	-0.1909	0.7416*	1

Table 14 shows the calculated correlations for Figure 22. It shows the correlation between RMSE of CD-SVD, SD-SVD, and CD-CCA. Here, error of CD-SVD and SD-SVD are highly and positively correlated, while CD-CCA has an insignificant correlation with them.

5.5 PERFORMANCE ANALYSIS OF ALGORITHMS

In this section, we focus on the performance and running time of the proposed and baseline algorithms. Then, we report the running time of each of the algorithms on the Supermarket dataset to compare them in this aspect.

In CD-CCA algorithm, we compute the canonical correlation between two domains, multiply the projection of source domain (canonical variates) with the diagonal correlations matrix, and project it back to the target space by multiplying the results with the discovered components for the target domain. The complexity of calculating CCA using the approach presented in [44] is O(Nk(3n + 5m + 2mn)), in which N is the number of iterations for least squares, k is the number of components (equal to or less than the number of items in the source domain), n is the number of datapoints (users), and m is the number of items in the target domain. The complexity for multiplying the $n \times k$ canonical variate matrix of the source domain, to the diagonal $k \times k$ matrix of canonical correlations is O(nk). Lastly, projecting the target domain canonical variates back to the original target domain space

costs O(nkp), in which p is the number of items in the target domain. Thus, since we have k < m and k < p, the complexity of CD-CCA algorithm is O(Nk(3n + 5m + 2mn) + nkp).

In the large-scale CD-LCCA, the complexity for computing canonical correlations includes iterations of LING least squares algorithm and QR-decomposition of projection of original source and target matrices into their small-scale versions. Ling costs $O(np(N_2+k_{pc}))$ in each iteration, which N_2 is the number of iterations to compute Y_r in large-scale CCA using gradient descent; and k_{pc} is the number of singular values that are used for calculating $U_1U_1^TY$. Each QR-decomposition takes $O(nk^2)$, in which k is the number of components. Eventually, calculating large-scale CCA will cost $O(Nnp(N_2 + k_{pc}) + Nnk^2)$. Since we are using sparse matrices in Matlab the multiplications in CD-LCCA depend on the number of nonzero elements in the matrices. In the worst case of multiplying dense matrices, the multiplications will cost $O(npk + nk^2)$. Thus, as a whole, CD-LCCA will cost $O(Nnp(N_2 + k_{pc}) + Nnk^2 + npk)$.

Among the baseline algorithms, SVD++ is the fastest. Since it is implemented for sparse matrices, its complexity depends on the number of nonzero elements in the matrix. So, if $|R_u|$ shows the number of ratings by user u, the complexity for SVD++ is $O(\Sigma_u |R_u|^2)$.

Figure 24 shows an example of running time of CD-CCA on different domain pairs in the Yelp dataset. The X axis shows the size of domain-pair based on number of items and users. It is in the logarithmic scale and represent the sum of user-item rating matrix sizes in the source and target domains $(\log_{10}(nm + np))$. The Y axis shows the running time of CD-CCA in seconds in logarithmic scale. We can see four examples of domain pairs in the picture. As we can see, as the size of domain-pairs grow, the running time of CD-CCA increases respectively.

To have an analysis of algorithms' performance in practice, we report a sample running time on one of the datasets. We ran all of the algorithms on two similar machines: a MacOS machine with 64GB RAM and two 4-core Intel Xeon, 2.26GHz CPUs and a Linux machine (CentOS) with 64GB RAM and two 4-core Intel Xeon, 2.40GHz CPUs. For CD-CCA, RMGM, and CMF, we use Matlab platform and for CD-SVD and SD-SVD, we use GraphChi software. The average running time of each algorithm on one domain pair of the Supermarket dataset is listed in Table 15. As we can see, CD-CCA has the least running time

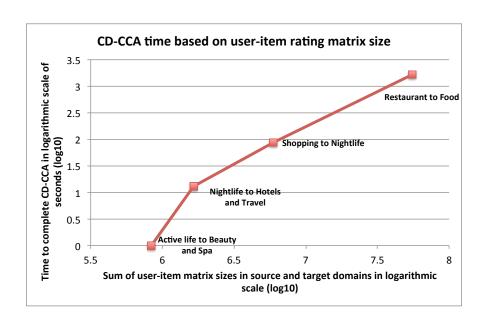


Figure 24: CD-CCA running time in four sample domain-pairs of the Yelp dataset. Numbers are in logarithmic scale.

and RMGM is very slow compared to the other algorithms. One reason for fast running time of CD-CCA is that it can be implemented in full matrices in Matlab and we can avoid loops in its implementation. However, the large-scale implementation of CD-CCA (or CD-LCCA) needs to work with the sparse matrix format in Matlab, and thus, uses less memory and is slow. Running CD-LCCA in Matlab on one domain pair of the Imhonet dataset took 21210 seconds (close to 6 hours) on average. Running CD-SVD with GraphChi on one domain pair of same dataset took almost 4 hours on average.

5.6 SUMMARY

In this chapter of the dissertation, we experimented on different, cross-domain and single-domain, algorithms on three datasets with various characteristics. We studied the feasibility and benefits of cross-domain recommender algorithms, including our proposed algorithms, CD-CCA and CD-LCCA.

Table 15: Average running time of each algorithm on one domain pair in the Supermarket dataset

	CD-CCA	CD-SVD	SD-SVD	RMGM	CMF
Running time (s)	36	252	176.4	11224	295.38

We compared the results of algorithms in each of the datasets and concluded that CD-CCA is the best performing algorithm in the Yelp and Imhonet dataset, and RMGM is the best-performing one in the Supermarket dataset. On the other hand, RMGM is the worst-performing algorithm in the Yelp dataset. One of the reasons that can result in this inconsistency is the characteristics of the datasets. As we have discussed in Section 3.3.2, RMGM algorithm has problems in finding clear clusters of users and items in case there is a high skewness in the ratings of a dataset. If we look at the skewness of ratings in the Yelp dataset, we can see that most of the ratings in the Yelp dataset are on the popular items. The high skewness of the ratings in the Yelp dataset and low skewness of them in the Supermarket dataset can be one of the reasons for this inconsistency. In general, rating-based recommender systems, such as Imhonet and Yelp, are more prone to be naturally skewed; while in the recommender systems based on "implicit feedback" we see more balance in the feedback on items. Also, the nature of Supermarket dataset, in which we have the whole data on the purchased items, is inherently different from the other two datasets. Because, in Yelp and Imhonet datasets, we do not have access to the "consumption" data, e.g. we do not know if a user has gone to a restaurant or not. We only have the rating information of users, if they decide to rate the item that have consumed.

Another reason can be because of the way we processed the Supermarket dataset for RMGM. As mentioned in Section 4.3, we had to convert the frequency of purchases to a categorical rating for RMGM. Although we have lost some of the precision of data because of this pre-processing, the 10-scale categorization in the Supermarket dataset provides more flexibility compared to the 5-Likert scale of the Yelp dataset.

The third likely reason, is the sparsity of the Yelp dataset, compared to the Supermarket dataset. As we have seen in Section 4.4, most of the domains in the Supermarket dataset are denser compared to the Yelp dataset domains. Again, the sparsity problem often happens more in the rating-based datasets compared to the implicit feedback ones. Because, in the explicit rating feedback, the data passes through another cognitive decision of the users, e.g. to decide if they would like to rate the items or not. While, in the implicit feedback datasets, we only see the first cognitive decision of users: to consume (purchase) the item or not. We have mentioned in Section 3.3.2 that RMGM has a poor performance in very sparse datasets.

Also, we have seen that CMF is one of the best-performing algorithms on the Yelp dataset and the worst-performing one in the Supermarket dataset. In both of the datasets, CMF has the most variance of error, and thus widest confidence intervals. We hypothesize that the reason behind CMF's inconsistency of performance is the ratio between number of users and number of (target) items in the two datasets. As we have seen in Section 4.4, in the Yelp dataset most of the domains have a tall user-item matrix. However, the user-item matrices in the Supermarket dataset are usually fat. Since CMF is trying to find a common user factor matrix between the source and target domains, the flexibility of item factor matrices of these domains decreases. Consequently, this leads to better representation of items when there are fewer number of items to fit in the item factor matrix.

Another interesting observation is the correlation among the errors of algorithms. We can see that in all of the datasets, if there is a significant correlation between the error of two cross-domain algorithms, this correlation is positive. However, the correlation between error of SD-SVD and other algorithms varies between the datasets. In the Supermarket dataset SD-SVD's error has a positive correlation with error of CD-SVD; and a negative one with the rest of cross-domain algorithms' errors. In the Imhonet dataset, there is no significant correlation between error of CD-SVD and CD-CCA. In contrast, SD-SVD error's correlation with all of the cross-domain algorithms in the Yelp dataset is positive. This hints us to the effects that the datasets can have on performance of cross-domain algorithms: cross-domain algorithms perform worse where single-domain algorithms perform better in the Supermarket dataset; but, in the Yelp dataset, this relationship is reverse.

We analyzed the time-complexity of the proposed algorithms and compared their running-

time with the baseline algorithms. We concluded that CD-CCA is the fastest algorithm on the average-sized data. SD-SVD and CD-SVD are the next fast ones and CMF is slower than these two algorithms. Among all of the algorithms, RMGM is very slow. On the large-scale dataset, CD-SVD and SD-SVD are faster than CD-LCCA. However, the running time of CD-LCCA is reasonable given the size of the data. On the other hand, CMF and RMGM are very slow on the large-scale dataset. Thus, using these two algorithms in large datasets is not practical. Thus, although RMGM performed better than CD-CCA in terms of estimated error in one of the datasets, it may not be practical to use it in large datasets because of its time performance.

In summary, the goal of this chapter was to answer to the first part of our first research question (Q.1.1); to understand if the benefit gained from cross-domain recommenders is because of the extra data, the better algorithm, or both.

We have seen that cross-domain algorithms mostly perform better than, or similar to the single-domain algorithm. In all of the 158 + 50 + 12 = 220 domain pairs from the three datasets, in only 8 cases SD-SVD performed significantly better than all of the cross-domain algorithms. These 8 domain pairs were all part of the Supermarket purchase dataset. In the rest of the domain pairs, there were at least one cross-domain algorithm that performed significantly better than, or similar to SD-SVD.

Nevertheless, we have seen that cross-domain recommenders do not always increase the quality of recommendation results. In some cases, the cross-domain recommender algorithms did not improve the results, compared to the single-domain algorithm; they just did not have a significantly worse results compared to SD-SVD.

Eventually, we conclude that cross-domain recommender systems are feasible and can be beneficial in some of the domain pairs and datasets.

Also, we have seen that the benefit of these recommender systems, compared to the single-domain recommender, comes from both the additional data available to them and the approach they use to utilize this additional information. CD-SVD algorithm, which uses the cross-domain setup and the single-domain approach, has performed significantly better than SD-SVD in some of the domains of all of the datasets. We attribute this behavior to the extra information that CD-SVD had compared to SD-SVD. However, we have seen

that in many cases that SD-SVD performed significantly better than CD-SVD, the other cross-domain algorithms outperformed SD-SVD. In these cases, the additional information alone is not enough to produce better recommendations. But, having better approaches that efficiently use this extra information, results in less error and better recommendations.

In later chapters, we explore the conditions, which lead to better performance of cross-domain recommender systems, compared to the single-domain ones.

6.0 COLD-START EXPERIMENTS

One of the major problems in the recommender systems literature is the cold-start problem [56]. For example, in collaborative filtering, the cold-start problem happens when a new user joins the system. Since there are no ratings available for this user, there is no way to compare this user to other users and find out their similar tastes. Thus, the recommender system cannot recommend any items to this new user. One of the goals of cross-domain recommendation is to alleviate the cold-start problem by transferring user information from the source domain to the target domain. In this case, if user is new to the target domain, but has an established profile in the source domain, cross-domain recommender can adjust the target user's source profile for using in the target domain. In CD-CCA, we transfer user profiles from the source domain to the target domain using the canonical variates and canonical correlation that are estimated by CCA.

Since tackling the cold-start problem is one of the main goals of cross-domain recommenders, we compare CD-CCA and the baseline algorithms in the cold-start setting for each of the datasets. Another aspect that can affect the performance of algorithms is users' source domain profile size. It is important to understand how much data is needed to be transferred from the source domain to the target domain to have a reasonable increase in recommender system's performance.

This chapter aims to experiment on the cold-start setting to answer the research question Q1.2. The results of our experiments on each of the datasets in the cold-start setting are presented in the following sections.

6.1 EXPERIMENT SETUP

Since we have multiple domain-pairs in each of the datasets, we run the cold-start experiments in two settings: once for each of the domain-pairs separately, and once averaging the errors over all of the domain-pairs.

To understand how each of these algorithms perform in the cold-start setting, we group the test users of each dataset based on the size of their target domain profile. Then, we calculate the error for each group of these users. In the case of analysis of cold-start results for each of the domain pairs separately, we calculate the average user-based error for all of the users with the same target profile size and report that average. For analyzing all of the domain pairs together, we average over user-based error for all of the test users that have the same target profile size, independent of the domain-pair they are coming from.

To study the effect of source profile size on the results, we partition test users based on the size of their source domain profiles and calculate the error for each group separately; once for each of the domain pairs, and once for all of the domain pairs at the same time.

To calculate the user-based error, we calculate the RMSE and MAE of algorithms for each row of the estimated user-rating matrix. So, instead of averaging the error over all of the test ratings, we calculate and average error for each user, based on that specific user's test ratings.

6.2 COLD-START ANALYSIS FOR THE SUPERMARKET PURCHASE DATASET

First, we look at the different profile sizes in the Supermarket dataset. To have a dataset-wide view (instead of a domain-pair specific one), we put all of the test users of all domain-pairs together and plot the size of their target profile sizes. Looking at the scatter plot of number of users versus target profile size in Figure 25, we can see that most of the test users have a small target profile size. The maximum number of items in target profiles of test users is 45.

To understand how each of the algorithms perform in the cold-start setting in all of the

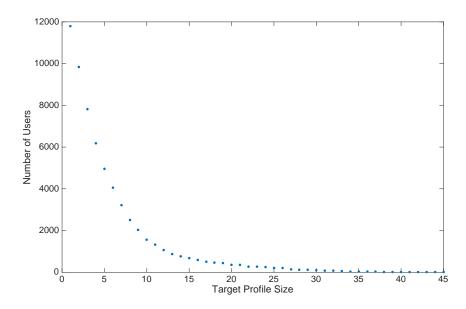


Figure 25: Target profile sizes of users in the Supermarket dataset

domain-pairs, we look at their RMSE and MAE based on users' target profile size. To do so, we calculate the error of each algorithm for each of the test users in each of the domain pairs. Then, we group the test users of all domain pairs based on their target domain profile sizes. For each group of users, we average the error of that group and calculate the 95% confidence interval for that average.

Figures 26 and 27 show the RMSE and MAE of each of the algorithms for test users in all of the domain pairs based on their target domain profile size. As we can see in this figure, the confidence interval for the errors increase as the size of target domain profile grows. This is because there are less number of users with higher target profile sizes in the dataset. Also, we can see that all of the algorithms follow a similar trend of error as users' target domain profile size grows.

Except for RMGM that has a high error when target profile size equals to one, starting from target profile size 1 to around 7, we see an increase in the error rate. Although, the error difference of consequent profile sizes is very small, this difference is significant in many cases, especially for the SD-SVD algorithm. It appears that having more items in the target

domain's profile results in more error in all of the algorithms. Since this trend is happening for SD-SVD more significantly than the cross-domain algorithms, we cannot attribute it to the characteristics of cross-domain recommenders.

After the seventh item in target domain's user profile, we can see a decrease in error of cross-domain algorithms. For SD-SVD the error almost stays the same and then increases after the 25 target profile size. CD-CCA, CMF, and RMGM show a more steady error reduction compared to the single-domain algorithm. This error reduction is most visible in the RMGM algorithm's results. While RMGM works worse than all other algorithms for users with two to seven items in their target profiles, it improves very fast for user profile sizes of around 20. More specifically, for these target domain profile sizes, it has a significantly lower RMSE compared to SD-SVD and CD-SVD and significantly lower MAE compared to CD-SVD, SD-SVD, and CD-CCA. After that, RMGM's error increases again. For CD-CCA and CMF, there is a slight, but significant and steady error reduction by increasing users' target domain profile sizes until the profile size of 35. After that, we can see a small increase in the error rates of all algorithms.

Comparing the confidence intervals of errors in these algorithms, we can see that CD-CCA has smaller confidence intervals and shows a more steady behavior. Except for the error of profile size of one, RMGM also has a relatively steady behavior. CMF and CD-CCA have wider confidence intervals and thus are less reliable, especially with large target profile sizes.

The aforementioned results are for average of test users in all of the domain-pairs. We look at each of the domain-pairs separately to get a closer look at the cold-start setting and how each algorithm handles it. Figure 52 in Appendix A shows the MAE and RMSE of each of the algorithms in each of the 50 domain-pairs for different target domain user profile sizes. As we can see in these pictures, the results of many domain-pairs are similar to the average results over all of the domain-pairs. However, in some of the domain-pairs, we can see different trends. For example, for "home cleaning \rightarrow fruit & vegetables", we can see that CMF has a significantly better RMSE compared to all other algorithms, for users with target profile size of one; and in "home outdoor \rightarrow fruit & vegetables" domain in the same figure, CD-CCA has a similar RMSE compared to SD-SVD and CD-SVD; and SD-SVD performs

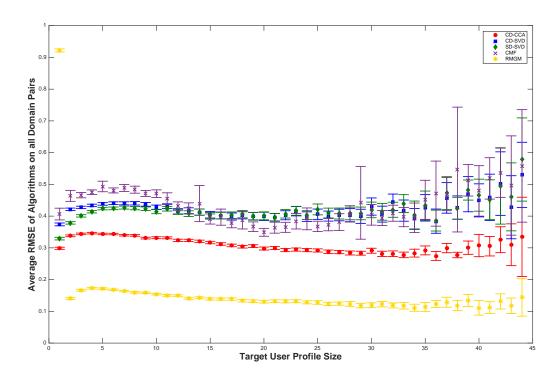


Figure 26: User-based RMSE of algorithms in the Supermarket dataset, averaged on all domain-pairs and sorted based on the users' target domain profile size

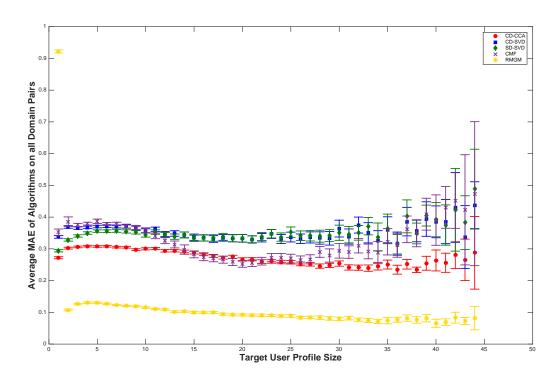


Figure 27: User-based MAE of algorithms in the Supermarket dataset, averaged on all domain-pairs and sorted based on the users' target domain profile size

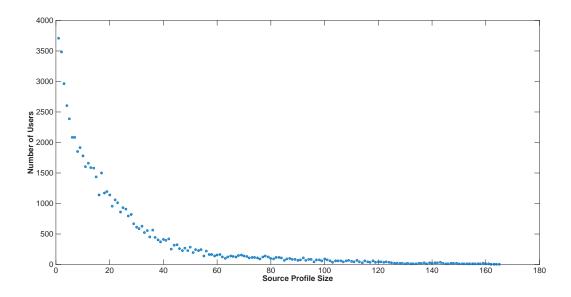


Figure 28: Source profile sizes of users in the Supermarket dataset

mostly better than CD-SVD in "bread \rightarrow home cleaning". However, although these errors appear to be in a different order than the general results, they do not contradict them. This happens because of different distribution of target domain profile sizes in each of the domain pairs.

Another factor that can impact the results is the size of user profile in the source domain. Figure 28 shows the number of users in all domain-pairs with various source domain profile sizes. The number of items bought by users in the source domains ranges between one and 165. It is important to know if transferring just a few items from an auxiliary domain can help or not. Also, we would like to know if transferring more information from the source domain could harm the recommendation results or not. To understand this, we run the same cold-start experiments on users' source domain profile size.

Figures 29 and 30 show the RMSE and MAE of algorithms, grouped by source domain profile size of users, averaged over all domain pairs. Although SD-SVD does not use the information from any source domains, and thus it should not show a change of error based on source user profile size, we still plot the RMSE of this algorithm to show the changes that

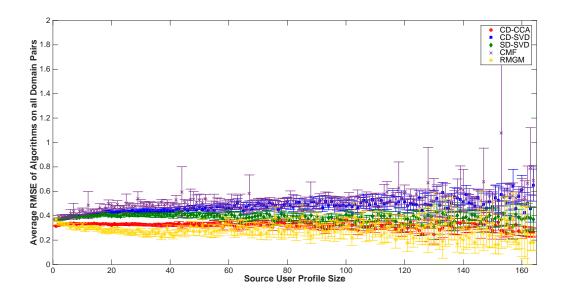


Figure 29: User-based RMSE of algorithms in the Supermarket dataset, averaged on all domain-pairs and sorted based on the users' source domain profile size

happens in other algorithms' errors in correlation with SD-SVD's errors. We can see that the error of SD-SVD, and thus CMF, CD-SVD, and CD-CCA, has a slight increase as the source user profile size grows. This increase is more visible in CMF and CD-SVD compared to CD-CCA and SD-SVD. After having around five items in source profile, CD-CCA's errors start to decrease. For CD-SVD and CMF, the increase will continue by users' source domain profile size. This trend is especially visible in the MAE of algorithms. For SD-SVD, the errors stay more or less the same. For RMGM, we see a steady decrease of error from the beginning until 40 items in users' source domain profile. After having around 40 items in users' source profile, the variance of errors increases and we cannot rely on any increasing or decreasing error trends.

Another interesting observation is that CD-CCA performs better than all of the other algorithms when having a very small source profile size. After having about 5 items in the source domain profile, RMGM has the best error among these algorithms.

To understand the effect of source domain profile size on the errors we can look at Figure

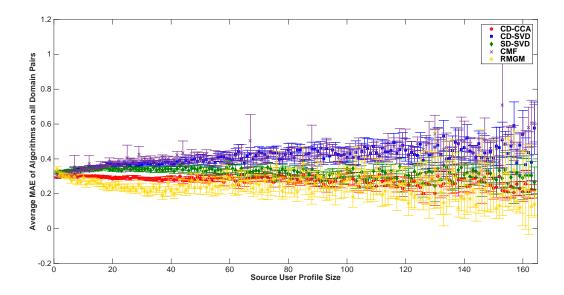


Figure 30: User-based MAE of algorithms in the Supermarket dataset, averaged on all domain-pairs and sorted based on the users' source domain profile size

54 in Appendix A. Looking at these figures, we can see some different error patterns in each of the domain-pairs compared to the average error patterns for all domain pairs. For example, CMF is one of the best-performing algorithms in the "canned & pickled \rightarrow fruit & vegetables" domain pair; RMGM has the most error for the "bread \rightarrow events" domain pair; and MAE of CD-CCA in "home cleaning \rightarrow fruit & vegetables" decreases with a large steep until the biggest source domain profile size.

6.3 COLD-START ANALYSIS FOR THE YELP DATASET

Looking at the target domain profile sizes of users in Figure 31, we can see the rapid drop in user profile sizes. Most of users (92% of them) have only one to three ratings in a domain, and very few of them (8.9219e-07%) have more than 45 item ratings in their target profile. This rapid drop in user profile sizes results in a more severe cold-start problem in the Yelp

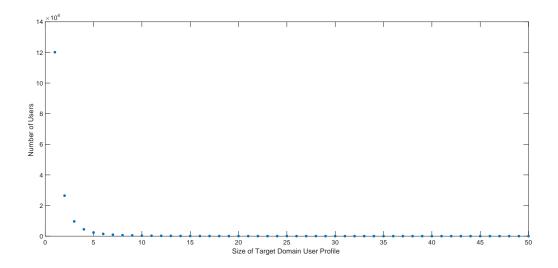


Figure 31: Target profile sizes of users in Yelp dataset

dataset compared to the Supermarket dataset.

We run the cold-start experiments on the Yelp dataset in a similar setup to the Supermarket dataset, as explained in Section 6.2. First, we look at the average performance of algorithms on all 158 domain pairs, based on test user profile sizes in target domains. Figure 32 shows the RMSE of algorithms in the cold-start setting and Figure 33 shows their performance based on MAE.

Based on these figures, averaging over all of the domain pairs, CD-CCA is performing the best in the cold-start setting; and CMF is the next best algorithm. CD-SVD and SD-SVD were unable to return recommendations in the extreme cold-start situation, where we have up to four items in the target user profile. RMGM has a large error when the test users have only one item in their profile. However, after that, its error drops dramatically and continues to decrease as the target profile of user grows in size. For CD-SVD and SD-SVD, there is a slight decrease in the error as the user profile size increases. However, both CMF and CD-CCA experience a small increase in the error until target profile size of three.

As we can see in the pictures, as the user profile size grows, so does the confidence interval of the error. This is because of the small number of users with a larger profile size. Thus,

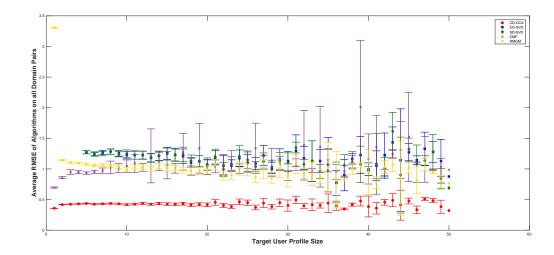


Figure 32: User-based RMSE of algorithms in the Yelp dataset, averaged on all domain-pairs and sorted based on the users' target domain profile size

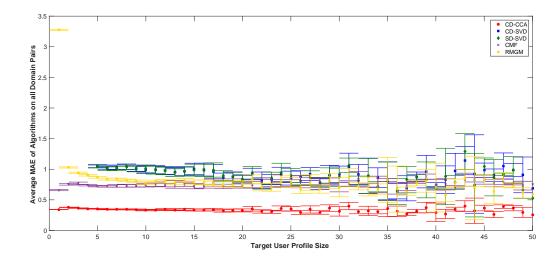


Figure 33: User-based MAE of algorithms in the Yelp dataset, averaged on all domain-pairs and sorted based on the users' target domain profile size

the reliability of results decreases for the errors reported at larger target profile sizes.

We look at the errors reported by each of the algorithms in each of the domain-pairs separately. Figure 74 in Appendix B.3 shows the MAE of algorithms in each of the domain pairs¹.

The first point that is noticed by looking at these pictures is the size of user profiles in various domain pairs. As we can see, in only 26 of the domain pairs the maximum size of user profiles exceeds 10 items and in only 7 of them this size is bigger than 20 items. The domain pairs with largest test user profile sizes are "food \rightarrow restaurants" and "night life \rightarrow restaurants" with largest target profile size of 50. As a result, the results that we see in the tail of plots in Figures 33 and 32 are generated from these domain pairs. In some domain pairs, such as "public services \rightarrow financial services" and "religious organizations \rightarrow education", the target domain user profiles have less than three items. Consequently, since SD-SVD and CD-SVD were not able to generate recommendations in many extreme cold-start situations, we can mostly see the results of CD-CCA. CMF, and RMGM in these domain pairs.

Although there are profile size differences in the domain pairs, most of the algorithms show a similar performance to the one calculated as average of all domain-pair user profile sizes. There are a few cases in which the algorithms show a different behavior compared to the average case. For example, in "professional services \rightarrow financial services", there is no significant differences between CD-CCA, CMF, CD-SVD, and SD-SVD errors; in "night life \rightarrow food" and "arts & entertainment \rightarrow night life", the error rates of SD-SVD and CD-SVD are much higher than CD-CCA, CMF, and RMGM; and in "active life \rightarrow beauty & spas", CD-SVD's MAE is slightly, but constantly, higher than SD-SVD.

In the next step, we perform an analysis on users' source domain profile size. Figure 34 shows the number of test users with various profile sizes in the source domain. The maximum ratings a test user has in the source domain is 145 items. However, more than 92% of users have a source profile size of 10 items or less. To see the effect of source domain profile size on the recommendation results, we look at the RMSE and MAE of all algorithms in Figures 35 and 36. These figures show the error of algorithms, for users of various source domain

¹We have omitted the figures for RMSE of the algorithms because of the large number of domain pairs.

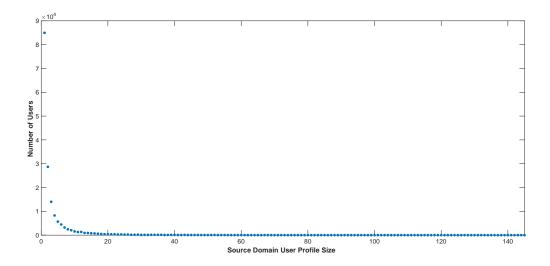


Figure 34: Source profile sizes of users in Yelp dataset

profile sizes, averaged on all domain pairs.

In these figures, we can see that the error of RMGM algorithm decreases as users' source profile size increases. For CD-CCA, SD-SVD, and CD-SVD, the error change is insignificant. However, for CMF, there is a slight increase in the errors as users have more items rated in their source domain profile.

The confidence interval of all errors increases with the increase of user profile size. This increase may be because of the less number of users that we have with larger profile sizes. This increase in confidence interval is more obvious for RMGM and CMF. These two algorithms produce less stable errors compared to CD-CCA, CD-SVD, and SD-SVD.

6.4 COLD-START ANALYSIS FOR THE IMHONET DATASET

To understand how CD-SVD, SD-SVD, and CD-CCA perform in the cold-start setting in the Imhonet dataset, we look at the target domain profile sizes of users. Figure 37 shows the number of test users with each of the target domain profile sizes in all of the domain

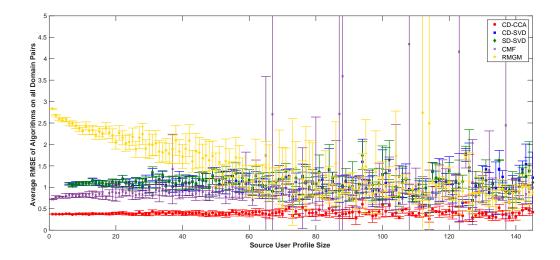


Figure 35: User-based RMSE of algorithms in the Yelp dataset, averaged on all domain-pairs and sorted based on the users' source domain profile size

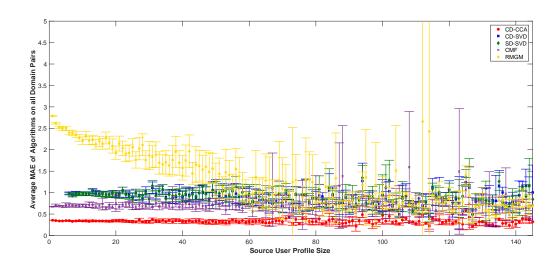


Figure 36: User-based MAE of algorithms in the Yelp dataset, averaged on all domain-pairs and sorted based on the users' source domain profile size

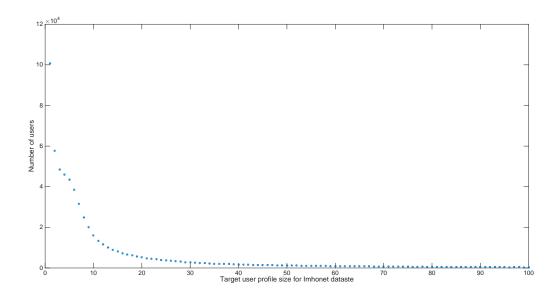


Figure 37: Target profile sizes of users in Imhonet dataset

pairs. We can see that most of the test users have a small profile size (less than 10 items) in the target domain. There are a few users with 100 and more items in their target profile. However, to have a better plot, we skipped showing these users. Also, we can see a concave shape at the small (less than 10) target domain profile sizes. This happens due to the data collection procedure in Imhonet. To collect more data from users, Imhonet has asked some of the users to rate at least 20 items, so that Imhonet can provide recommendations to them. Since we only use 20% of test user ratings in their target profiles, this increase in the profile size happens for the profiles that have less than 10 items.

For the cold-start experiments in the Imhonet dataset, we follow the same instructions as for the other two datasets. We calculate user-based errors in each of the domain pairs. Then, we average over the error of users with the same profile size in all of the domain pairs. Figures 38 and 39 show the RMSE and MAE of algorithms in the cold-start setting based on target user profile size.

As we can see in the pictures, for all of the algorithms, we see an increase of error as the target profile size grows, until a maximum point of error happens. After that, we can

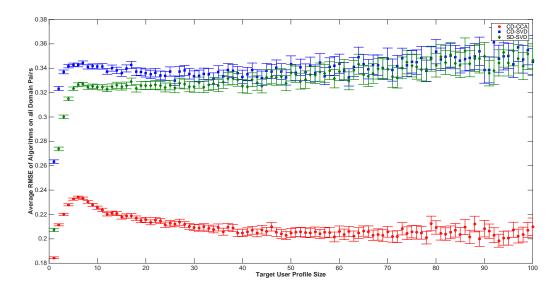


Figure 38: User-based RMSE of algorithms in the Imhonet dataset, averaged on all domainpairs and sorted based on the users' target domain profile size

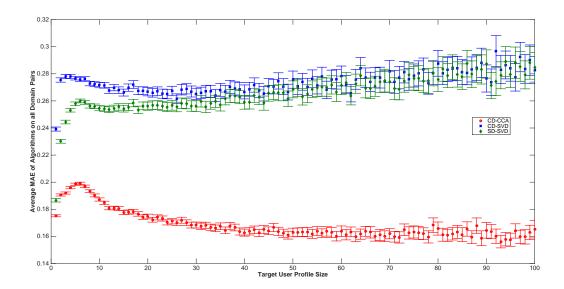


Figure 39: User-based MAE of algorithms in the Imhonet dataset, averaged on all domainpairs and sorted based on the users' target domain profile size

see a drop in the error rates by increasing target profile sizes. For SD-SVD and CD-SVD, we can see an insignificant increase (or steadiness) of error after a while. However, the error of CD-CCA continues to decrease by increasing size of target domain user profiles. Also, as the target user profile sizes increase, and we have less number of users with larger profile sizes, the confidence interval of error gets wider. CD-CCA has a significantly lower error compared to SD-SVD and CD-SVD for all user profile sizes. SD-SVD has a significantly better performance compared to CD-SVD, up to target profile size of 40. After 40 items, SD-SVD and CD-SVD become comparable in error.

Figures 97 and 98 in Appendix C.3 show the cold-start results of each of the algorithms in each of the domain pairs. As we can see in these figures, CD-CCA is generally performing better than the other two algorithms. But, we have different results, especially for CD-SVD and SD-SVD, in some of the domain pairs. For example, in "book \rightarrow game", CD-CCA and the other two algorithms get to perform similar to each other after users have enough items in their target profile (around 45 items); in "book \rightarrow perfume", the error is mostly increasing as the target profile sizes grow; in "movie \rightarrow game", SD-SVD performs much better than CD-SVD from the beginning, but in "game \rightarrow movie", CD-SVD is sometimes significantly better than SD-SVD; and in "movie \rightarrow book" the error of all three algorithms continue to decrease after a certain point in user profile size.

Also, we can see the difference in confidence of algorithms in different domain pairs. For example, in "book \rightarrow movie" the errorbars are much tighter than in "game \rightarrow perfume".

Studying the same setup for the source domain profile sizes, we look at source domain profile sizes of users in Figure 40. We can see that there is a break in the picture for source domain profile size of 20; the number of users with 20 items in their profile is suddenly higher than the neighboring profile sizes. The reason is the same as for the concave shape of target profile sizes: the data collection procedure in Imhonet. Other than this exception, we can see that the graph has a familiar trend: more users with a few ratings in their profiles and less users with more ratings. There are a few users that have more than 500 item ratings in their profile that we are not showing in this picture.

Experimenting on the source domain profile sizes, results in Figures 41 and 42 for RMSE and MAE of algorithms. We can see that there is a sharp increase of error for all of the

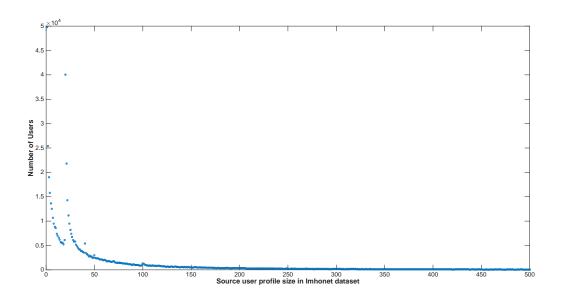


Figure 40: Source profile sizes of users in Imhonet dataset

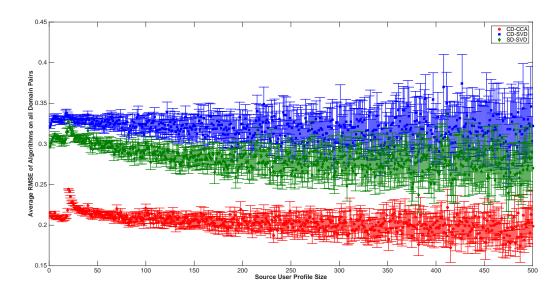


Figure 41: User-based RMSE of algorithms in the Imhonet dataset, averaged on all domain-pairs and sorted based on the users' source domain profile size

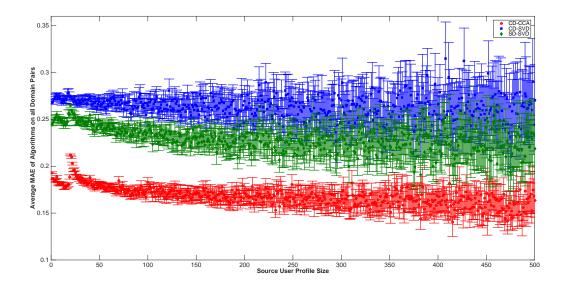


Figure 42: User-based MAE of algorithms in the Imhonet dataset, averaged on all domainpairs and sorted based on the users' source domain profile size

algorithms at the 20 profile size. This can be because of the number of source profile sizes with 20 items in them. Also, we can see that the error of all algorithms decreases after this point by increase in the source profile size of users. For SD-SVD, this decrease is unexpected, because this algorithm is not using source domain information. However, we speculate that the decrease may be because of correlation of source domain profile sizes with another factor that results in less error for SD-SVD.

Looking at the effect of source profile size on the error of algorithms in Figures 99 and 100 in Appendix C.3, we can see some differences in the cold-start results of different domain pairs. For example, we can see that the algorithms perform more similar to each other in "perfume \rightarrow game" versus "perfume \rightarrow book"; CD-SVD is the worst algorithm in "book \rightarrow game", but better than SD-SVD for smaller profile sizes in "book \rightarrow movie"; and the confidence of error in "book \rightarrow perfume" is much more than "game \rightarrow perfume".

6.5 SUMMARY

In this chapter, we experimented on the cold-start setting for different, cross-domain and single-domain, algorithms on three datasets. We looked at the cold-start setting in the target domain profile of users to research on the possible answers for research question Q1.2. We also looked at the source domain profile sizes to see the effect of amount of data that is transferred from the source domain on the recommendation results.

An interesting observation in the cold-start profile is that the average domain errors of almost all of the algorithms in all of the datasets increases at the beginning by the increase of target profile size (despite the fact that we expect a decrease in error because of the increase of information for users). This increase is more visible in the Supermarket and Imhonet datasets and SD-SVD, CMF, and CD-SVD algorithms. For CD-CCA, it only happens briefly, and then the error decreases. We hypothesize that this increase is because there are many domain pairs with a few number of users and very small profile sizes in the datasets. In other words, the maximum profile size of users in these domains are very low. In general, the errors for recommendations in these domain pairs can be high because of the lack of enough overall information, e.g. due to sparsity, to provide good recommendation. This phenomenon results in increasing the average error in the beginning for the target profile sizes. As we have seen in the figures related to each of the domain pairs, this increase does not happen in the domain pairs with larger target profile sizes and more data.

An exception to this reasoning is the CMF algorithm. As the target profile grows, the error of this algorithm grows even in the domain pairs with larger target profile sizes. This is more visible in the Supermarket dataset with denser domains. This can be because of the design of this algorithm: it tries to find a common set of factors between the users in the source and target domains; while having a small item factor matrix for each of the two domains. As the number of items grow, it will be more difficult for this algorithm to fit all of the item features in a small item factor matrix, especially in dense domains with more information about items.

The exception to the initial growth of average error on all domains is the RMGM algorithm on the Yelp dataset. It has a monotonic decreasing trend as the target profile of

users grow. As we have mentioned in Section 3.3.2, RMGM has problems to find the shared user-item clusters in skewed and sparse datasets. As the profile size of users grow, the sparsity of the dataset and its skewness decrease and thus results in better recommendations for RMGM. Since RMGM is performing very poorly for users with a very small profile size, no matter how big is the largest profile size of the domain pair, the reasoning that applies to the initial increase of average error in the other algorithms does not apply to it.

After the initial increase of error, we see different trends of errors based on user target profile sizes in different datasets. For the Yelp and Supermarket datasets, we mostly see a decrease of average error on all domain pairs when the target profile sizes exceed a specific size. But, for the Imhonet dataset, the error of SD-SVD and CD-SVD algorithms has an insignificant increase. We hypothesize that this happens because of the extreme sparsity of Imhonet as we have seen in Section 4.4.

As a summary of error changes over the source profile size, we can see that, while there should not be any changes in the error of SD-SVD based on the source profile size, its average error has a small increase or decrease as the source profile size increases in all of the datasets. This relationship can be because of some other variables that change with the source profile size. For example, if users with larger source profile size also have a larger target profile size, the error of SD-SVD will be correlated with the source profile size through its correlation with the target profile size. The average error of CMF and CD-SVD increases as the source profile size grows in the Yelp and Supermarket datasets. This increase means that these two algorithms cannot handle extra (unrelated) information about the users and more source domain information will add more noise and thus harm their performances in average. CD-CCA has a relatively small decrease of error at the beginning and then has a steady or decreasing error as the source domain profile size of users grow. This hints that CD-CCA can use the extra source domain information at the beginning and then, handles the noise that comes with adding too much source domain information. However, RMGM is the best algorithm in handling extra source domain information. Starting with a very high error at the beginning, it seems that RMGM cannot use a small amount of information from the source domain efficiently (especially in the Supermarket dataset). However, as the source domain profile sizes grow, the error of RMGM decreases constantly and with a fast pace.

In summary, we conclude that CD-CCA is the best algorithm in handling the cold-start situation in general. It has a low error in the extreme cold-start setting for target domain; it can use the moderate amount of source domain data to reduce the error; and it can handle the extra source domain information without harming the recommendations.

RMGM is the second best algorithm for the cold-start situation because even though it performs better than other algorithms in some of the datasets and even though it has a decreasing trend of error on having more and more information, it has a very bad performance in the extreme cold-start case of having one or very few ratings in user profiles.

Finally, to answer to Q1.2, we can conclude that cross-domain recommender systems, especially CD-CCA, can be beneficial in the cold-start setting.

7.0 FINDING THE APPROPRIATE AUXILIARY DOMAIN

In this chapter of the dissertation, the goal is to find the data characteristics that lead us to a better cross-domain recommendation and a higher improvement in cross-domain recommendations versus single-domain recommendations. Discovering these characteristics can lead us to select the best source domain for a specific target domain before performing the cross-domain recommendation task.

Here, we use CCA, in addition to other data characteristics, as key factors to find the best auxiliary domain for a specific target domain. We use this tool to answer the research questions Q2.1, Q2.2, and Q2.3. We hypothesize that the more canonical correlation the two domains have, the better the performance of cross-domain recommender system will be. To test this hypothesis, we analyze the correlation of the error of cross-domain recommendations with the CCA results, each domain data characteristics, and domain-pair data characteristics.

The second hypothesis in this chapter is on the improvement of cross-domain recommendations, compared to the single-domain recommendations. Since, based on our results in Chapter 5, the cross-domain algorithms' error is correlated with the single-domain algorithm's error, we would like to study if CCA can be a major factor in defining the amount of improvement that can be achieved by cross-domain algorithms over single-domain algorithms.

Eventually, to have a global view of effect of all of the data characteristics, at the same time, on cross-domain recommender results, we perform a regression analysis in the next section.

In the following sections, we first introduce the data characteristics that we use from the datasets. Then, we perform a correlation analysis between these data characteristics and the error of each of the algorithms. After that, we run a regression analysis with these data characteristics as dependent variables and the error of each algorithm as the dependent variable. Finally, we look at the domain pairs to find out if the good domain pair can make sense intuitively.

7.1 DATA CHARACTERISTICS

To have a global view of each of the domain pairs, we select four sets of features to build our analysis on: CCA-related features, general dataset characteristics, descriptive statistics, and divergence features. The goal of our analysis is to understand the importance and effect scale each of these factors on cross-domain recommendations. In other words, we would like to investigate the reason behind different results that we get for each of the approaches. Is there a data characteristic that can significantly predict the results?

For the CCA-related features, we look at the number of components than can be found in the CCA analysis of the two domains. Each of these components, include an r-value and p-value that indicate the strength and significance of the canonical correlations. So, we look at the number of significant correlations between the components (with 95% confidence) and the number of components with r-value that is bigger than a threshold. To be more exact, we picked 0.8, 0.9, and 0.95 thresholds for r-values based on CCA guidelines [24]. In addition to the above, we look at the r-value for the first component (with strongest correlation), average correlations of the first five components, and average correlations of all of the discovered components.

For the single-domain and domain pair characteristics, we look at both general dataset statistics and descriptive statistics. For general dataset statistics, we look at number of users, number of items in each of the domains, density of ratings in each of the domains, and their ratios with respect to each other. For example, we look at the ratio between rating densities for domain pairs, the ratio of user numbers to source item numbers, and target item numbers to source item numbers.

For descriptive statistics of the domain pairs, we look at the rating values. As measures

of central tendency, we choose average, median, and mode of rating values for both source and target domains. For dispersion measures, we look at the variance, kurtosis, and skewness of all ratings in both source and target domains.

Eventually, since we would like to measure the relationship between the rating values in source and target domains, we use divergence features. To be more specific, we look at the KL-divergence between all of the ratings in the source domain and all of the ratings in the target domain. However, since recommender systems rely on the similarity among users, we also look at the KL-divergence of ratings in the user level. To do this, we calculate the KL-divergence between each user's ratings in source and target domains. Then, we use average, median, and variance of these user-based KL-divergences to calculate the global user-based KL-divergence features for each domain pair.

Eventually, we end up with 33 different features for each domain pair. These data characteristics and their values are listed in Sections A.2, B.1, and C.1 in the Appendix sections for each of the datasets.

7.2 CORRELATION ANALYSIS

In this section, we seek to answer research questions Q2.1 and Q2.2. We analyze the correlation between each of the mentioned data characteristics in Section 7.1 and the error of single and cross-domain recommendations to figure out the features that lead to a fit domain pair. More specifically, we look at the correlation of single-domain data characteristics with the error of single-domain recommenders and the correlation of both single and cross-domain features with the error of cross-domain recommenders.

Additionally, since we have discovered a correlation between the single-domain and cross-domain error results in the previous chapter, we look at the relative improvement that we achieve in cross-domain recommendations, compared to the single-domain one. Thus, we define an "Improvement Ratio" factor as a dependent variable. Then, we run bivariate correlation analysis on data characteristics defined in Section 7.1 as independent variables.

The improvement ratio of algorithm a_1 over algorithm a_2 with the source domain s_i and

target domain d_j (IR_{a_1,a_2}(s_i,d_j)) is equivalent to the improvement of error of algorithm a_1 over algorithm a_2 , normalized by error of algorithm a_2 in the source domain s_i and target domain d_j (Equation 7.1).

$$IR_{a_1,a_2}(s_i, d_j) = \frac{Error_{a_1}(s_i, d_j) - Error_{a_2}(s_i, d_j)}{Error_{a_2}(s_i, d_j)}$$
(7.1)

In the following sections, the correlations with p-value < 0.05 are shown with one star, the ones with p-value < 0.01 are shown with two stars, and the ones with p-value < 0.001 are shown with three stars. Also, we count all of the correlations with p-value < 0.05 as significant correlations.

7.2.1 Correlation Analysis for the Supermarket Purchase Dataset

7.2.1.1 Correlation Analysis of Errors In this section, we look at the bivariate Pearson correlation of each of the data statistics with the error of each of the algorithms. Table 17 shows these correlations with the RMSE of algorithms and Table 16 shows them with the MAE of algorithms.

As we can see, the total KL-divergence of ratings in the source and target domains, the mode of source domain rating values and the average CCA correlations between the source and target domains do not have any significant correlations with the RMSE and MAE of any of the algorithms. Also, the average and median of user-based KL-divergences of source and target domains do not have any significant correlations with the RMSE of algorithms. However, they have a negative correlation with MAE of CD-CCA. The significant correlation of these two factors with the SD-SVD error is meaningless, because in SD-SVD, we only use the target domain data.

Except for the average CCA correlations between the source and target domains, the rest of CCA-related features have at least one significant correlation with the error of algorithms. For example, the number of significant CCA correlations, is significantly correlated with RMSE of CD-CCA, RMGM, CD-SVD, and SD-SVD; the average of first five components' CCA is significantly correlated with RMSE of CMF, RMGM, CD-SVD, and SD-SVD; and the value of first component's CCA is significantly correlated with RMSE of CMF, RMGM, and SD-SVD.

Table 16: Correlations of data characteristics with MAE of algorithms on the Supermaket dataset; *: significant with p-value < 0.05; **: significant with p-value < 0.01; ***: significant with p-value < 0.001

variables	CD-CCA MAE	CMF MAE	RMGM MAE	CD-SVD MAE	SD-SVD MAI
user size	0.3262*	-0.0441	-0.5925***	0.4777***	0.7593***
source item size	0.4702***	0.0043	-0.2012	0.3167*	0.2956*
target item size	-0.1585	0.0074	-0.5761***	0.2363	0.3918**
source density	-0.0326	0.3506*	0.3546*	0.5849***	-0.1233
target density	0.039	-0.8624***	-0.6611***	-0.1777	0.2763
total KL-divergence	-0.1717	-0.1384	0.0191	-0.1786	-0.1868
mean user KL-divergence	-0.3032*	-0.0836	0.2179	0.0352	-0.3761**
median user KL-divergence	-0.2994*	-0.0645	0.2231	0.1402	-0.3543*
variance user KL-divergence	-0.1676	0.3838**	0.8286***	-0.0679	-0.6455***
source mean rating	0.0049	0.3421*	0.247	0.6268***	0.0283
target mean rating	0.2885*	-0.7415***	-0.7859***	-0.016	0.5452***
source median rating	-0.0215	0.3475*	0.2726	0.6211***	0.0025
target median rating	0.3113*	-0.7554***	-0.8048***	-0.0283	0.5476***
source mode rating	0.09	0.189	-0.0884	0.2697	0.2319
target mode rating	-0.0446	-0.6463***	-0.3259*	0.0486	0.2391
source var rating	0.005	0.3111*	0.1997	0.5877***	0.0417
target var rating	0.2404	-0.6977***	-0.6131***	-0.0371	0.4268**
source kurtosis rating	-0.1073	-0.1338	-0.0356	-0.2982*	-0.1064
target kurtosis rating	-0.1827	0.2162	0.6107***	-0.1987	-0.4793***
source skewness rating	-0.1281	-0.1418	-0.0408	-0.3318*	-0.1144
target skewness rating	-0.1801	0.2392	0.6676***	-0.204	-0.5167***
user to source item ratio	-0.3496*	-0.0536	-0.1673	-0.0662	0.1397
user to target item ratio	0.431**	0.0189	0.3157*	0.0514	0.0189
source to target item ratio	0.5161***	0.024	0.3378*	0.0893	-0.0923
source to target density ratio	-0.1478	0.4109**	0.644***	0.4444**	-0.4935***
CCA correlation ≥ 0.80	0.0129	-0.1914	-0.4423**	0.1974	0.2572
CCA correlation ≥ 0.90	0.0492	-0.2208	-0.5352***	0.2183	0.3403*
CCA correlation ≥ 0.95	0.0256	-0.2492	-0.5717***	0.204	0.3873**
average correlation	-0.0914	-0.1572	-0.247	0.1455	0.114
first component correlation	0.1104	-0.1576	-0.5075***	0.317*	0.3793**
first 5 components correlation	0.1145	-0.2227	-0.5938***	0.2587	0.4096**
# components	0.1424	0.0196	-0.4671***	0.3329*	0.4781***
# significant correlations	-0.0863	-0.016	-0.5925***	0.3483*	0.525***

Table 17: Correlations of data characteristics with RMSE of algorithms on the Supermaket dataset; *: significant with p-value < 0.05; **: significant with p-value < 0.01; ***: significant with p-value < 0.001

variables	CD-CCA RMSE	CMF RMSE	RMGM RMSE	CD-SVD RMSE	SD-SVD RMSE
user size	-0.0598	-0.1703	-0.5693***	0.4108**	0.7439***
source item size	0.3265*	-0.2235	-0.1831	0.2758	0.2827*
target item size	-0.3395*	-0.2111	-0.5343***	0.1757	0.363**
source density	0.1617	0.1172	0.3587*	0.6299***	-0.0981
target density	-0.3796**	-0.4313**	-0.7199***	-0.2782	0.2448
total KL-divergence	-0.1587	0.0509	-0.0003	-0.2103	-0.2006
mean user KL-divergence	-0.1694	0.1084	0.1890	0.0332	-0.3874**
median user KL-divergence	-0.1741	0.1612	0.1862	0.1332	-0.359*
variance user KL-divergence	0.3158*	0.4961***	0.831***	0.0814	-0.6189***
source mean rating	0.1384	0.1345	0.2583	0.6772***	0.0516
target mean rating	-0.2404	-0.4377**	-0.8317***	-0.1303	0.5145***
source median rating	0.1270	0.1470	0.2847*	0.6779***	0.0267
target median rating	-0.2247	-0.4583***	-0.8498***	-0.1496	0.5135***
source mode rating	-0.0173	-0.0247	-0.0738	0.2701	0.2444
target mode rating	-0.2688	-0.3138*	-0.3695**	0.0373	0.2477
source var rating	0.1122	0.1261	0.2051	0.6202***	0.0639
target var rating	-0.2073	-0.3184*	-0.669***	-0.1167	0.4091**
source kurtosis rating	-0.1199	0.0726	-0.0480	-0.3341*	-0.1106
target kurtosis rating	0.0959	0.5192***	0.5725***	-0.1194	-0.4642***
source skewness rating	-0.1420	0.0780	-0.0549	-0.3681**	-0.1178
target skewness rating	0.1299	0.529***	0.6307***	-0.1139	-0.4961***
user to source item ratio	-0.4389**	0.1225	-0.1738	-0.0686	0.1429
user to target item ratio	0.437**	0.1710	0.2876*	0.0810	0.0421
source to target item ratio	0.5717***	0.0210	0.3191*	0.1046	-0.0818
source to target density ratio	0.2573	0.2166	0.647***	0.5296***	-0.4641***
CCA correlation ≥ 0.80	-0.2278	-0.3547*	-0.4285**	0.1043	0.2127
CCA correlation ≥ 0.90	-0.2289	-0.3867**	-0.5187***	0.1224	0.2982*
CCA correlation ≥ 0.95	-0.2576	-0.342*	-0.5585***	0.1185	0.3557*
average correlation	-0.2428	-0.2628	-0.2417	0.0763	0.0798
first component correlation	-0.0936	-0.3517*	-0.4814***	0.2479	0.361**
first 5 components correlation	-0.1678	-0.3901**	-0.5733***	0.1678	0.3747**
# components	-0.0752	-0.2096	-0.4355**	0.2862*	0.4628***
# significant correlations	-0.3511*	-0.2179	-0.5587***	0.2846*	0.5005***

As we expected to have better cross-domain recommendations when having a high canon-

ical correlation between the domain pairs, these CCA-related features have negative correlations with RMSE of CD-CCA, RMGM, and CMF. It means that the RMSE of these algorithms are lower when there is a high canonical correlation between the source and target domains. However, as it is shown in the table, although CD-SVD is also a cross-domain recommender, these correlations are always positive for its error. It means that the error of CD-SVD grows more with the higher CCA between the source and target domains. Also, we can see that although SD-SVD is a single-domain algorithm (thus there should not be any meaningful correlations between its error and CCA-based features), there is a significant positive correlation between the error of SD-SVD and most of the CCA-related features. As we have seen in section 5.2, the error of algorithms, especially for CD-SVD and SD-SVD, are highly correlated in the Supermarket dataset. Consequently, we hypothesize that the positive correlation between the error of CD-SVD and the CCA-related features is because of the same factors that create a positive correlation between the error of SD-SVD and these features. Especially, because the magnitude and significance of this positive correlation is higher for RMSE and MAE of SD-SVD, compared to CD-SVD.

Among the general dataset characteristics, the density of target domain has a significant negative correlation with RMSE of CD-CCA, RMGM, and CMF and MAE of RMGM and CMF. Thus, we will have a lower error rate when there is more user rating information available in the target domain. The denser the source domain is, the higher error we will have in CD-SVD and RMGM algorithms. It means that more information in the source domain can harm more than help in these two cross-domain recommenders. One interesting observation is the correlation between number of users and RMSE of CD-SVD and SD-SVD (and MAE of CD-CCA, CD-SVD, and SD-SVD). As the number of users grow, we expect to have a better understanding of various user tastes, and thus better recommendations. However, for these two algorithms in the Supermarket dataset, this relationship works in reverse. Also, we see that as the number of users grow compared to the number of source domain items (when the user-item source domain matrix gets taller), we achieve significantly less error from CD-CCA. However, as the target domain's user-item matrix gets taller, we see an increase in error of CD-CCA and RMGM. Another general factor with a large correlation with the errors is the density ratio of source to target domains. Having a higher density

source domain, compared to target domain, results in worse recommendations from RMGM, CD-SVD, and CMF; and (meaninglessly) better recommendations in SD-SVD.

Among the descriptive statistics features, most of them have a significant relationship with CMF. While the source domain's central tendency measures have a positive correlation with MAE of CMF, these features from the target domain are negatively correlated with CMF's error. The target domain central tendency features are also negatively correlated with RMGM's errors and positively correlated with SD-SVD's. For the dispersion statistics, we can see that SD-SVD performs worse when there is more variance in the target domain ratings; but the cross-domain recommenders work better in this case. This relationship is the reverse for target ratings' kurtosis and skewness. More specifically, the RMSE of RMGM and MAE of RMGM and CMF increases significantly when the target data ratings are skewed and have more kurtosis.

In general, we can see that RMGM and SD-SVD have the largest number of significant correlations with the data features. For SD-SVD, many of these correlations do not impose any meaningful relationship, because it only uses the target domains data and many of the features are calculated based on domain pairs. We can get a better understanding of these correlations by looking at the scatter plot of these features against the error of algorithms. These scatter plots can be found in Appendix A.5.

7.2.1.2 Correlation Analysis of Improvement Ratio In this section, we look at the correlation of data features with the improvement that can be achieved in the recommendation results by using cross-domain recommenders, instead of the single-domain recommender. Tables 19 and 18 show the improvement ratio (IR) of each of the cross-domain algorithms over SD-SVD for RMSE and MAE of the results.

Table 18: Correlations of data characteristics with MAE-based improvement ratio of cross-domain algorithms, over SD-SVD, on the Supermarket dataset; *: significant with p-value < 0.05; **: significant with p-value < 0.01; ***: significant with p-value < 0.001

variables	IR for CD-CCA over SD-SVD for all the pairs			IR for CD-SVD over SD-SVD for all the pairs
user size	0.6803***	0.5659***	0.6556***	0.3639**
source item size	0.121	0.2002	0.2251	0.0111
target item size	0.4528***	0.3081*	0.5077***	0.2047
source density	-0.215	-0.3327*	-0.3177*	-0.6189***
target density	0.3528*	0.7081***	0.535***	0.3865**
total KL-divergence	-0.0982	-0.017	-0.0588	-0.0517
mean user KL-divergence	-0.3103*	-0.2168	-0.2866*	-0.4413**
median user KL-divergence	-0.2831*	-0.2176	-0.2859*	-0.522***
variance user KL-divergence	-0.7482***	-0.7879***	-0.8332***	-0.5933***
source mean rating	-0.0832	-0.2316	-0.2007	-0.4955***
target mean rating	0.5283***	0.8181***	0.7054***	0.5032***
source median rating	-0.1058	-0.258	-0.2296	-0.5165***
target median rating	0.5376***	0.8387***	0.7278***	0.5208***
source mode rating	0.1709	0.0541	0.118	0.013
target mode rating	0.2383	0.439**	0.2402	0.1518
source var rating	-0.043	-0.1812	-0.1501	-0.4492**
target var rating	0.3833**	0.6712***	0.5252***	0.3928**
source kurtosis rating	0.0038	0.0595	0.0318	0.1437
target kurtosis rating	-0.484***	-0.5313***	-0.6041***	-0.2927*
source skewness rating	0.0105	0.063	0.036	0.1657
target skewness rating	-0.5314***	-0.5777***	-0.6583***	-0.3288*
user to source item ratio	0.302*	0.1475	0.1754	0.218
user to target item ratio	-0.0984	-0.018	-0.1744	-0.0164
source to target item ratio	-0.2726	-0.099	-0.2426	-0.1756
source to target density ratio	-0.5963***	-0.6616***	-0.6594***	-0.9057***
CCA correlation ≥ 0.80	0.2497	0.324*	0.3699**	0.0698
CCA correlation ≥ 0.90	0.3196*	0.3911**	0.4523***	0.1325
CCA correlation ≥ 0.95	0.3827**	0.4325**	0.4914***	0.1998
average correlation	0.1421	0.2046	0.202	-0.0193
first component correlation	0.3683**	0.4052**	0.4787***	0.1259
first 5 components correlation	0.3779**	0.4424**	0.5208***	0.1759
# components	0.4109**	0.3187*	0.4474**	0.1934
# significant correlations	0.536***	0.383**	0.5435***	0.2307

Table 19: Correlations of data characteristics with RMSE-based improvement ratio of cross-domain algorithms, over SD-SVD, on the Supermarket dataset; *: significant with p-value < 0.05; **: significant with p-value < 0.01; ***: significant with p-value < 0.001

variables	IR for CD-CCA over SD-SVD for all the pairs			IR for CD-SVD over SD-SVD for all the pairs
user size	0.6831***	0.3683**	0.643***	0.3944**
source item size	0.1191	0.2644	0.2109	0.0383
target item size	0.4528***	0.3163*	0.5048***	0.226
source density	-0.2177	-0.1307	-0.3227*	-0.617***
target density	0.4098**	0.4021**	0.5955***	0.4435**
total KL-divergence	-0.0935	-0.0932	-0.0487	-0.0337
mean user KL-divergence	-0.303*	-0.2128	-0.2708	-0.4325**
median user KL-divergence	-0.2719	-0.2554	-0.2602	-0.4964***
variance user KL-divergence	-0.7727***	-0.6405***	-0.8541***	-0.6848***
source mean rating	-0.0875	-0.0993	-0.2099	-0.5058***
target mean rating	0.5881***	0.5019***	0.7579***	0.5738***
source median rating	-0.1096	-0.1202	-0.2395	-0.5312***
target median rating	0.5926***	0.5187***	0.7777***	0.5925***
source mode rating	0.197	0.0901	0.1177	0.0236
target mode rating	0.2921*	0.2629	0.289*	0.1763
source var rating	-0.0466	-0.0782	-0.1543	-0.4456**
target var rating	0.4506**	0.3617**	0.5849***	0.4497**
source kurtosis rating	0.0033	-0.0682	0.0375	0.1682
target kurtosis rating	-0.5066***	-0.6336***	-0.6036***	-0.3583*
source skewness rating	0.0105	-0.0738	0.0435	0.1904
target skewness rating	-0.5515***	-0.6488***	-0.6574***	-0.3959**
user to source item ratio	0.308*	-0.0476	0.1849	0.2117
user to target item ratio	-0.1169	-0.1525	-0.1889	-0.0277
source to target item ratio	-0.2905*	-0.0587	-0.2606	-0.1778
source to target density ratio	-0.5986***	-0.3255*	-0.6601***	-0.915***
CCA correlation ≥ 0.80	0.2691	0.3901**	0.3682**	0.1109
CCA correlation ≥ 0.90	0.3447*	0.4288**	0.4564***	0.179
CCA correlation ≥ 0.95	0.4095**	0.3914**	0.5029***	0.2453
average correlation	0.1557	0.2835*	0.1968	0.0093
first component correlation	0.3721**	0.4353**	0.4743***	0.1675
first 5 components correlation	0.3978**	0.454***	0.5256***	0.2233
# components	0.4188**	0.3029*	0.4439**	0.2178
# significant correlations	0.5518***	0.3387*	0.5442***	0.2594

As shown in the tables, number of shared users, target domain's density, and average, median, and variance of user ratings in the target domain are the factors that are positively correlated with the improvement ratios of all cross-domain recommenders versus SD-SVD, calculated on either RMSE or MAE. Variance in KL-divergence of user ratings between source and target domains, kurtosis and skewness of target domain ratings, and the density ratio of source domain to target domain, all have a negative correlation with the improvement ratios of all algorithms.

Also, we can see that the number of items in the source domain, the KL-divergence of all ratings in the source and target domains, mode, kurtosis, and skewness of rating values in the source domain, the ratio of number of common users to number of target domain items, and the ratio between number of items in the source and target domains do not have any significant correlations with the IRs.

Among the CCA-related features, almost all of them (except average canonical correlation) are positively and significantly correlated with IR of CD-CCA, RMGM, and CMF. Interestingly, the improvement of CD-SVD over SD-SVD does not follow a similar rule: the correlations are weak and not significant.

The scatter plot of these features against the improvement ratio of algorithms can be found in Appendix A.5.

7.2.2 Correlation Analysis for Yelp Dataset

7.2.2.1 Correlation Analysis of Errors Tables 21 and 20 show the bivariate Pearson correlation between the RMSE and MAE of algorithms and the dataset characteristics for the Yelp dataset.

Table 20: Correlations of data characteristics with MAE of algorithms on the Yelp dataset; *: significant with p-value < 0.05; **: significant with p-value < 0.01; ***: significant with p-value < 0.001

variables	CD-CCA MAE	CMF MAE	RMGM MAE	CD-SVD MAE	SD-SVD MAE
user size	-0.1747*	-0.1206	-0.4416***	0.0506	0.0806
source item size	-0.1374	-0.135	-0.2912***	0.0178	0.0176
target item size	-0.1466	-0.096	-0.545***	0.0232	0.0228
source density	0.16*	0.3345***	0.3647***	-0.0974	-0.0949
target density	0.0822	0.2441**	0.2735***	-0.1189	-0.0884
total KL-divergence	0.2823***	0.5248***	0.1583*	-0.0224	0.051
mean user KL-divergence	-0.1564	0.0286	-0.2179**	-0.0089	-0.0217
median user KL-divergence	-0.1174	-0.0106	-0.2637***	-0.0159	-0.0035
variance user KL-divergence	0.1848*	0.2528**	0.5671***	-0.0207	-0.0797
source mean rating	-0.2491**	0.01	0.0737	-0.2444**	-0.243**
target mean rating	-0.3789***	-0.1638*	0.4904***	-0.3583***	-0.457***
source median rating	0.0036	0.0862	0.0291	-0.1302	-0.097
target median rating	0.0339	0.0495	0.4978***	-0.2154**	-0.2944***
source mode rating	0.0754	0.1185	0.0139	-0.0616	-0.0168
target mode rating	0.4441***	0.2908***	0.7259***	0.0229	-0.0184
source var rating	0.364***	0.2485**	-0.044	0.1227	0.2128**
target var rating	0.9222***	0.4855***	0.4326***	0.301***	0.33***
source kurtosis rating	-0.2328**	-0.0632	0.0959	-0.2103**	-0.2414**
target kurtosis rating	-0.5195***	-0.2627***	0.2639***	-0.3639***	-0.4431***
source skewness rating	0.1836*	-0.0448	-0.0551	0.2233**	0.219**
target skewness rating	0.2057*	0.0704	-0.5734***	0.3029***	0.3966***
user to source item ratio	-0.222**	-0.1113	-0.4632***	0.0507	0.0868
user to target item ratio	-0.2191**	-0.2359**	-0.126	0.0498	0.0815
source to target item ratio	-0.1125	-0.2127**	0.1437	-0.043	-0.0586
source to target density ratio	0.3044***	0.1737*	0.3143***	0.1294	0.0595
CCA correlation ≥ 0.80	-0.0154	-0.082	-0.2807***	-0.0238	-0.01
CCA correlation ≥ 0.90	-0.0873	-0.1467	-0.332***	-0.0243	-0.0212
CCA correlation ≥ 0.95	-0.0637	-0.0761	-0.1228	-0.1103	-0.0856
average correlation	-0.0236	-0.1022	-0.3981***	0.0594	0.0884
first component correlation	-0.0927	-0.1681*	-0.4294***	0.1428	0.1151
first 5 components correlation	-0.1884*	-0.4392***	-0.5319***	0.1718*	0.1313
# components	-0.1727*	-0.1412	-0.5009***	0.0548	0.0736
# significant correlations	-0.1748*	-0.1282	-0.5285***	0.0487	0.0659

Table 21: Correlations of data characteristics with RMSE of algorithms on the Yelp dataset; *: significant with p-value < 0.05; **: significant with p-value < 0.01; ***: significant with p-value < 0.001

:	CD CCA PMCD	OME DMCD	DMCM DMCD	CD CVD DACE	CD CUD DMCD
variables .				CD-SVD RMSE	
user size	-0.1782*	0.0039	-0.4475***	-0.1745*	-0.1455
source item size	-0.1239	0.0087	-0.2754***	-0.1274	-0.0953
target item size	-0.125	-0.0537	-0.5613***	-0.1445	-0.1225
source density	0.0515	0.0407	0.3396***	-0.1161	-0.1201
target density	-0.0502	-0.0098	0.2513**	-0.1346	-0.1525
total KL-divergence	0.194*	0.1772*	0.1376	-0.0669	-0.2068**
mean user KL-divergence	-0.1597*	-0.0001	-0.2284**	-0.0532	-0.1093
median user KL-divergence	-0.1532	-0.0104	-0.2754***	-0.0821	-0.142
variance user KL-divergence	0.2526**	0.1367	0.5741***	0.1234	0.0944
source mean rating	-0.2173**	-0.0224	0.0719	-0.0759	-0.1682*
target mean rating	-0.2679***	-0.2141**	0.5041***	-0.4038***	-0.33***
source median rating	-0.0075	-0.0409	0.0233	0.0789	0.0078
target median rating	0.1271	-0.0604	0.4941***	-0.1213	-0.0491
source mode rating	0.0346	-0.0233	0.0045	0.0972	0.0156
target mode rating	0.495***	0.0652	0.7302***	0.3559***	0.3973***
source var rating	0.2939***	0.0614	-0.0519	0.1339	0.1176
target var rating	0.876***	0.2667***	0.4259***	0.6789***	0.6415***
source kurtosis rating	-0.2009*	-0.0512	0.0958	-0.1039	-0.1651*
target kurtosis rating	-0.4062***	-0.2154**	0.2753***	-0.5027***	-0.4313***
source skewness rating	0.1637*	0.0239	-0.0514	0.0912	0.174*
target skewness rating	0.0742	0.1252	-0.5846***	0.2747***	0.2027*
user to source item ratio	-0.2427**	-0.0581	-0.4812***	-0.2047**	-0.1831*
user to target item ratio	-0.2532**	0.0121	-0.1159	-0.1595*	-0.1282
source to target item ratio	-0.1308	-0.0265	0.1572	-0.0406	-0.0225
source to target density ratio	0.3824***	0.0793	0.3196***	0.2477**	0.2871***
CCA correlation ≥ 0.80	-0.0765	-0.0945	-0.296***	-0.1704*	-0.1401
CCA correlation ≥ 0.90	-0.127	-0.1269	-0.3452***	-0.2301**	-0.207**
CCA correlation ≥ 0.95	-0.102	-0.0678	-0.1409	-0.2932***	-0.3426***
average correlation	-0.095	-0.0967	-0.4118***	-0.0909	-0.0798
first component correlation	-0.072	-0.099	-0.4246***	-0.1498	-0.1036
first 5 components correlation		-0.133	-0.5075***	0.045	0.1213
# components	-0.1536	-0.0353	-0.4974***	-0.1514	-0.1205
# significant correlations	-0.1601*	-0.0375	-0.5343***	-0.1606*	-0.1335
// 5-Similarit correlations	0.1001	5.0516	0.0010	0.1000	0.1000

As we can see in these tables, median and mode of source domain ratings do not have

any significant correlations with any of the errors of the algorithms. Average of ratings in the target domain, kurtosis of target domain ratings, and variance in target domain ratings, all have significant correlations with the error of all algorithms. The more variance we see in the target ratings, the more the RMSE and MAE of all algorithms will be. However average of ratings in the target domain and kurtosis of target domain ratings have a tricky correlation with error of algorithms. While they are both negatively correlated with RMSE and MAE of CD-CCA, CD-SVD, CMF, and SD-SVD, their correlation with RMGM's MAE and RMSE is positive.

Also, source domain's density, KL-divergence between all ratings of the two domains, variance in user-based KL-divergences between the domains, mode of the rating values in the target domain, and density ratio between source and target domains are all positively and significantly correlated with either MAE or RMSE of CD-CCA, CMF, and RMGM algorithms.

The number of users has a significant negative correlation with RMSE of all cross-domain algorithms except CMF, and with MAE of CD-CCA and RMGM. This means that as the number of common users between the domains grow, we achieve better cross-domain recommendations in these algorithms. The same relationship exists between the ratio of user numbers to number of items in the source domain. In this case, we have a significant negative relationship between this factor and RMSE of CD-CCA, CD-SVD, and RMGM and with MAE of CD-CCA and RMGM.

Among the CCA-related features, they mostly have a negative correlation with the error of algorithms. But, we can see more significant correlations with MAE of algorithms. For example, number of significantly correlated components, maximum number of components, average correlation of first five components all have a negative significant correlation with MAE of CD-CCA and RMGM. But, only number of significantly correlated components is correlated with RMSE of CD-CCA. Also, only MAE of CMF is significantly correlated with the value of first component's correlation and average correlation of first five components. For CD-SVD, the correlations are confusing: while the RMSE of this algorithm has a negative significant correlation with the number of significantly correlated components, its MAE is positively correlated with the average correlation of first five components. Again, this

phenomenon can be because of the high correlation of error in SD-SVD and CD-SVD, and the fact that SD-SVD has a positive (although non-significant) correlation with the average correlation of first five components.

Again, we can see that RMGM has the most number of significant correlations with the data features.

We can look at the scatter plot of these features against the error of algorithms in Appendix B.4 to get a better understanding of these correlations. The blue circles show the non-significant improvement ratios and the red crosses show the significant ones. In these pictures, you can see the improvement ratio of all of the algorithms compared to each other (not only the improvement ratio of cross-domain algorithms over SD-SVD).

7.2.2.2 Correlation Analysis of Improvement Ratio If we look at the IR of cross-domain algorithms vs SD-SVD in Tables 23 (for their RMSE) and 22 (for their MAE), we can see that most of the CCA-related features have a positive correlation with the IRs. More specifically, the average correlation of the first component is positively and significantly correlated with the improvement of all cross-domain RMSEs, over the single-domain one; and is positively and significantly correlated with the IR of CD-CCA, CMF, and RMGM, calculated over MAEs. Also, the maximum number of components, and number of components with significant correlations are positively correlated with IR of CD-CCA, CMF, and RMGM, calculated over MAEs. The complicated case here is the negative significant correlation of the number of components with more than 0.95 CCA, with MAE-based IR of CD-CCA, and RMSE-based IR of CD-CCA and CD-SVD. One of the possible reasons for this relationship can be the few number of cases in which there exists a CCA more than 0.95 between the components. In other words, since very few of the discovered components, in a few of domain pairs, have such a high correlation, this result can be less reliable.

Table 22: Correlations of data characteristics with MAE-based improvement ratio of cross-domain algorithms, over SD-SVD, on the Yelp dataset; *: significant with p-value < 0.05; **: significant with p-value < 0.01; ***: significant with p-value < 0.001

variables	IR for CD-CCA over SD-SVD for all the pairs			IR for CD-SVD over SD-SVD for all the pairs
user size	0.1945*	0.1661*	0.3324***	0.0601
source item size	0.1296	0.1556	0.2238**	0.0034
target item size	0.1401	0.1168	0.3949***	-0.0094
source density	-0.3325***	-0.4406***	-0.3669***	-0.0095
target density	-0.3123***	-0.3833***	-0.3357***	0.0706
total KL-divergence	-0.189*	-0.4209***	-0.0924	0.159*
mean user KL-divergence	0.1309	-0.0198	0.2031*	-0.0284
median user KL-divergence	0.1055	0.0086	0.2119**	0.0371
variance user KL-divergence	-0.2122**	-0.2822***	-0.3666***	-0.119
source mean rating	-0.1373	-0.1682*	-0.2336**	0.1113
target mean rating	-0.4017***	-0.2806***	-0.7135***	-0.129
source median rating	-0.1324	-0.112	-0.1177	0.1138
target median rating	-0.5065***	-0.375***	-0.6256***	-0.1723*
source mode rating	-0.0997	-0.1452	-0.0552	0.1232
target mode rating	-0.36***	-0.3053***	-0.5133***	-0.1034
source var rating	-0.0528	-0.1068	0.1	0.1327
target var rating	-0.2239**	-0.1909*	-0.0559	-0.0217
source kurtosis rating	-0.1481	-0.1134	-0.2662***	0.0278
target kurtosis rating	-0.317***	-0.1854*	-0.6055***	-0.0963
source skewness rating	0.1776*	0.1997*	0.2403**	-0.1069
target skewness rating	0.4771***	0.3291***	0.7602***	0.1421
user to source item ratio	0.2423**	0.1617*	0.3449***	0.0689
user to target item ratio	0.239**	0.2863***	0.1233	0.0709
source to target item ratio	0.0394	0.1883*	-0.1107	-0.0257
source to target density ratio	-0.1227	-0.1094	-0.1391	-0.1999*
CCA correlation ≥ 0.80	-0.0671	0.032	0.0993	0.0172
CCA correlation ≥ 0.90	-0.0367	0.0632	0.1282	-0.0098
CCA correlation ≥ 0.95	-0.241**	-0.1169	-0.1367	0.0851
average correlation	0.1189	0.161*	0.3063***	0.0266
first component correlation	0.1327	0.1989*	0.2896***	-0.1191
first 5 components correlation	0.381***	0.5376***	0.498***	-0.126
# components	0.2096**	0.1952*	0.3896***	0.0428
# significant correlations	0.1978*	0.1739*	0.399***	0.0346

Table 23: Correlations of data characteristics with RMSE-based improvement ratio of cross-domain algorithms, over SD-SVD, on the Yelp dataset; *: significant with p-value < 0.05; **: significant with p-value < 0.01; ***: significant with p-value < 0.001

variables	IR for CD-CCA over SD-SVD for all the pairs			IR for CD-SVD over SD-SVD for all the pairs
user size	0.0595	-0.0385	0.311***	0.1016
source item size	0.0631	-0.0319	0.2036*	0.1186
target item size	0.0354	0.0369	0.424***	0.0863
source density	-0.3493***	-0.0915	-0.4647***	-0.1772*
target density	-0.3357***	-0.0592	-0.4544***	-0.217**
total KL-divergence	-0.5609***	-0.2323**	-0.3149***	-0.6312***
mean user KL-divergence	-0.0185	-0.0238	0.1232	-0.2226**
median user KL-divergence	-0.0554	-0.023	0.1279	-0.2665***
variance user KL-divergence	-0.1671*	-0.1221	-0.3997***	-0.1324
source mean rating	-0.0053	-0.0076	-0.184*	-0.22**
target mean rating	-0.005	0.1641*	-0.574***	0.2133**
source median rating	-0.0048	0.0563	-0.0455	-0.1801*
target median rating	-0.1881*	0.0427	-0.463***	0.1949*
source mode rating	-0.1121	0.0147	-0.072	-0.2354**
target mode rating	-0.0403	0.0381	-0.362***	0.1306
source var rating	-0.1785*	-0.0305	0.068	-0.1209
target var rating	-0.2936***	-0.1553	-0.0563	-0.1369
source kurtosis rating	-0.0046	0.0175	-0.2067**	-0.1269
target kurtosis rating	0.0205	0.1409	-0.4507***	0.224**
source skewness rating	0.0617	0.006	0.1857*	0.2014*
target skewness rating	0.0889	-0.0938	0.5841***	-0.2213**
user to source item ratio	0.0878	0.0267	0.3163***	0.0779
user to target item ratio	0.1547	-0.0508	0.0483	0.1126
source to target item ratio	0.1217	0.0111	-0.1276	0.0652
source to target density ratio	-0.0688	-0.022	-0.0774	0.1345
CCA correlation ≥ 0.80	-0.0941	0.0607	0.1172	0.055
CCA correlation ≥ 0.90	-0.0096	0.0974	0.1758*	0.013
CCA correlation ≥ 0.95	-0.1933*	0.0035	-0.1139	-0.2738***
average correlation	-0.0096	0.078	0.2718***	0.0044
first component correlation	0.1087	0.1094	0.3601***	0.1494
first 5 components correlation	0.422***	0.1877*	0.6293***	0.3814***
# components	0.0739	0.0157	0.3776***	0.1192
# significant correlations	0.0618	0.0148	0.3966***	0.1035

Other important factors are the KL-divergence of all ratings between the source and target domains and the median ratings in the target domain. The first one is significantly and negatively correlated with the RMSE-based IR of all algorithms and the second one is significantly and negatively correlated with the MAE-based IR of all of them. This means that as the median of ratings in the target domain and the divergence between the source and target ratings grow, we will achieve less improvement when using cross-domain recommender systems.

Source domain's density, target domain's density, average, median, and variance of user-based KL-Divergence between the domains, average, median, mode, variance, and kurtosis of ratings in the source and target domains, all have a mostly negative correlation with the improvement ratio of algorithms. So, the higher they are, the less improvement we achieve in the cross-domain algorithms.

On the other hand, skewness of rating in the source and target domains, the ratio of number of users to source items, and number of users to target items have a generally positive effect on the IR of cross-domain algorithms in the Yelp dataset.

The scatter plot of these features against the improvement ratio of algorithms can be found in Appendix B.4.

7.2.3 Correlation Analysis for Imhonet Dataset

7.2.3.1 Correlation Analysis of Errors This section analyzes correlations between the Imhonet dataset features and error of algorithms. Table 25 shows these correlations for the RMSE of CD-CCA, SD-SVD, and CD-SVD; and Table 24 shows these correlations for the MAE of these algorithms. Note that we do not see any results for the number of components (# components) or number of significant correlations (# significant correlations) in these two tables. For the number of components, the reason is that the best number of discovered components for all of the domain pairs in this dataset is the same (5 components for all) and there is no variance in this feature. So, we cannot examine its correlation with the error of algorithms.

Table 24: Correlations of data characteristics with MAE of algorithms on the Imhonet dataset; *: significant with p-value < 0.05; **: significant with p-value < 0.01; ***: significant with p-value < 0.001

variables	CD-CCA MAE	CD-SVD MAE	SD-SVD MAE
user size	-0.0632	-0.5345	-0.403
source item size	0.604*	0.0116	-0.309
target item size	-0.7093**	-0.3742	-0.0922
source density	-0.3402	0.0543	0.0789
target density	0.4529	0.4491	0.5155
total KL-divergence	0.5608	0.7411**	0.1675
mean user KL-divergence	-0.057	-0.6151*	-0.4542
median user KL-divergence	-0.0134	-0.5658	-0.3986
variance user KL-divergence	-0.0932	-0.6299*	-0.4812
source mean rating	0.5755	0.2336	0.1661
target mean rating	-0.5898*	-0.3778	-0.5119
source mode rating	-0.0946	0.2031	0.6077*
target mode rating	0.0394	0.1512	-0.0998
source var rating	-0.8311***	-0.3703	0.0785
target var rating	0.8367***	0.2114	-0.0575
source kurtosis rating	0.7129**	0.3331	0.0619
target kurtosis rating	-0.7564**	-0.292	-0.2778
source skewness rating	-0.5813*	-0.2654	-0.1477
target skewness rating	0.6097*	0.3471	0.4562
user to source item ratio	-0.8191**	-0.033	0.399
user to target item ratio	0.7995**	0.4653	-0.0494
source to target item ratio	0.6352*	0.642*	0.2179
source to target density ratio	-0.7088**	-0.3823	-0.3747
CCA correlation ≥ 0.80	0.2312	0.0329	-0.1487
CCA correlation ≥ 0.90	-0.0181	0.1138	0.1365
CCA correlation ≥ 0.95	-0.1191	0.1593	0.1647
average correlation	0.0332	0.1133	0.0519
first component correlation	0.0755	0.1857	0.1183
first 5 components correlation	0.0332	0.1133	0.0519

Table 25: Correlations of data characteristics with RMSE of algorithms on the Imhonet dataset; *: significant with p-value < 0.05; **: significant with p-value < 0.01; ***: significant with p-value < 0.001

variables	CD-CCA RMSE	CD-SVD RMSE	SD-SVD RMSE
user size	0.0885	-0.5475	-0.4316
source item size	0.7073*	-0.0013	-0.3277
target item size	-0.532	-0.3435	-0.057
source density	-0.4844	0.0707	0.0819
target density	0.1955	0.366	0.4448
total KL-divergence	0.5748	0.7663**	0.2021
mean user KL-divergence	0.0451	-0.6396*	-0.4979
median user KL-divergence	0.0736	-0.5957*	-0.4485
variance user KL-divergence	0.0174	-0.6483*	-0.5174
source mean rating	0.5961*	0.1956	0.147
target mean rating	-0.3715	-0.2714	-0.4159
source mode rating	-0.095	0.1622	0.6*
target mode rating	0.0825	0.2101	-0.0658
source var rating	-0.831***	-0.3596	0.0908
target var rating	0.7*	0.1671	-0.1159
source kurtosis rating	0.7233**	0.3059	0.0542
target kurtosis rating	-0.567	-0.19	-0.178
source skewness rating	-0.5825*	-0.2287	-0.135
target skewness rating	0.4049	0.2307	0.351
user to source item ratio	-0.7606**	-0.0134	0.4371
user to target item ratio	0.7385**	0.4508	-0.0675
source to target item ratio	0.5286	0.6142*	0.2114
source to target density ratio	-0.5769*	-0.3018	-0.3047
CCA correlation ≥ 0.80	0.1209	0.0193	-0.161
CCA correlation ≥ 0.90	-0.2526	0.0954	0.1204
CCA correlation ≥ 0.95	-0.3158	0.1562	0.1647
average correlation	-0.1695	0.0967	0.0372
first component correlation	-0.1128	0.153	0.0912
first 5 components correlation	-0.1695	0.0967	0.0372

For the number of significant components, the reason is that we did not have any significant canonical correlation in any of the 5 components in any of the domains. In other words, the significance of the correlations between domain pairs, although high in value in some pairs, did not pass our threshold for the significance test.

As we can see in the tables, the significant factors that effect the error of each of these algorithms are different with each other. In CD-CCA, we can see that the number of items in the source domain, variance of ratings in the target domain, kurtosis of ratings in the source domain, and the ratio of number of users to the number of items in the target domain have a positive correlation with the errors. On the other hand, the variance in the source domain ratings, kurtosis of target domain ratings, skewness of ratings in the source domain, the ratio of number of users to number of items in the source domain, and the density ratio between source and target domains, all have a significantly negative relationship with CD-CCA's errors.

For CD-SVD, the ratio of number of users to number of items in the source domain and the KL-divergence between all ratings in the source and target domains are associated with higher errors. While more average and variance in user-based KL-divergence results in less errors.

In SD-SVD, the only significant factor is mode of ratings in the source domain, which has a positive correlation with RMSE and MAE.

Interestingly, none of the CCA-related features are significantly correlated with the error of cross-domain algorithms in this dataset. The scatter plot of these features against the error of algorithms can be found in Appendix C.4.

7.2.3.2 Correlation Analysis of Improvement Ratio Tables 27 and 26 show the correlation analysis between the data features and the improvement ratios of errors for CD-CCA and CD-SVD versus SD-SVD. For the reason explained in the previous section, we do not have the # components and # significant correlations features in these tables.

As we can see in these tables, the only factor that is significantly and positively correlated with the IR of CD-CCA vs. SD-SVD, is the ratio between number of users and number of items in the source domain. This means that the taller the user-item matrix of source domain, the more improvement we achieve in CD-CCA compared to SD-SVD. Also, the MAE-based improvement ratio of CD-CCA is negatively correlated with the number of items in the source domain.

Table 26: Correlations of data characteristics with MAE-based improvement ratio of cross-domain algorithms, over SD-SVD, on the Imhonet dataset; *: significant with p-value < 0.05; **: significant with p-value < 0.01; ***: significant with p-value < 0.001

variables	IR for CD-CCA over SD-SVD for all the pairs	IR for CD-SVD over SD-SVD for all the pairs
user size	-0.331	0.303
source item size	-0.5731	-0.3944
target item size	0.274	0.4436
source density	0.2783	0.034
target density	0.188	-0.0132
total KL-divergence	-0.1248	-0.9132***
mean user KL-divergence	-0.3669	0.3802
median user KL-divergence	-0.3343	0.374
variance user KL-divergence	-0.3768	0.3688
source mean rating	-0.1653	-0.1562
target mean rating	-0.1171	-0.0925
source mode rating	0.4748	0.3861
target mode rating	-0.0746	-0.3676
source var rating	0.4622	0.6446*
target var rating	-0.4506	-0.3652
source kurtosis rating	-0.3204	-0.4196
target kurtosis rating	0.1794	0.0752
source skewness rating	0.1896	0.2176
target skewness rating	0.0422	0.0703
user to source item ratio	0.7264**	0.5199
user to target item ratio	-0.4214	-0.7369**
source to target item ratio	-0.1182	-0.6415*
source to target density ratio	0.0792	0.1243
CCA correlation ≥ 0.80	-0.2109	-0.1882
CCA correlation ≥ 0.90	0.169	0.0658
CCA correlation ≥ 0.95	0.2491	0.0253
average correlation	0.0741	-0.039
first component correlation	0.099	-0.0593
first 5 components correlation	0.0741	-0.039

Table 27: Correlations of data characteristics with RMSE-based improvement ratio of cross-domain algorithms, over SD-SVD, on the Imhonet dataset; *: significant with p-value < 0.05; **: significant with p-value < 0.01; ***: significant with p-value < 0.001

variables	IR for CD-CCA over SD-SVD for all the pairs	s IR for CD-SVD over SD-SVD for all the pairs
user size	-0.4189	0.3242
source item size	-0.6069*	-0.3661
target item size	0.1848	0.4466
source density	0.3337	-0.0023
target density	0.2625	-0.0251
total KL-divergence	-0.0878	-0.9198***
mean user KL-divergence	-0.4437	0.4006
median user KL-divergence	-0.4108	0.3908
variance user KL-divergence	-0.4505	0.3912
source mean rating	-0.1765	-0.131
target mean rating	-0.1495	-0.084
source mode rating	0.4579	0.3911
target mode rating	-0.0641	-0.3997
source var rating	0.4437	0.6337*
target var rating	-0.4008	-0.3669
source kurtosis rating	-0.3068	-0.3889
target kurtosis rating	0.1419	0.071
source skewness rating	0.1828	0.1864
target skewness rating	0.0684	0.0706
user to source item ratio	0.6851*	0.5026
user to target item ratio	-0.3778	-0.7345**
source to target item ratio	-0.0623	-0.6355*
source to target density ratio	0.0469	0.1156
CCA correlation ≥ 0.80	-0.1567	-0.1763
CCA correlation ≥ 0.90	0.2551	0.0469
CCA correlation ≥ 0.95	0.323	0.0014
average correlation	0.1514	-0.0504
first component correlation	0.1579	-0.0688
first 5 components correlation	0.1514	-0.0504

For CD-SVD, the total KL-divergence between source and target domain ratings, the ratio between source and target domain densities, and the ratio of number of users to number of target domain items have significantly negative correlations with improvement ratio. The only significantly positive correlation is for the variance of source domain ratings.

Again, none of the CCA-related features have a significant correlation with the amount of improvement we get in the cross-domain recommender systems, compared to the single-domain one. The scatter plot of these features against the improvement ratio of algorithms can be found in Appendix C.4.

7.2.4 Summary

In this section, we studied the correlation of various data characteristics with RMSE, MAE, RMSE-based improvement ratio, and MAE-based improvement ratio of algorithms. In summary, we have seen that some of the data features are consistently correlated with the results in different datasets and some other are inconsistent.

For example, the total KL-divergence between the source and target domains, if significant, mostly has a negative correlation with the improvement ratio of algorithms. This means that the distribution of ratings in the source and target domains should be similar to each other to have a better result in cross-domain recommendations.

Also, the CCA-related features, if significant, have a positive correlation with the improvement ratio of algorithms. It means that stronger canonical correlation between the source and target domains is associated with better cross-domain recommendations. The only exception is the number of correlations > 0.95 in the Yelp dataset that can be ignored because of very few domain pairs that actually have a canonical correlation of > 0.95.

Some of the features had different behaviors in different datasets. For example, the correlation of number of users and average ratings of target users with MAE of CD-CCA is negative in the Yelp dataset, but positive in the Supermarket dataset; skewness of source domain ratings has a positive correlation with MAE of CD-SVD in Yelp dataset, but a negative one in the Supermarket dataset; Source density and variance in user-based KL-divergence between the source and target domains has a positive correlation with IR in the Supermarket dataset and a negative one in the Yelp dataset; and Kurtosis of target domain ratings is negatively correlated with RMGM's IR in the Yelp dataset and positively correlated with it in the Supermarket dataset.

For the Imhonet dataset, we see very different results. None of the CCA-related features

have a significant correlation with the error of algorithms. Also, there are fewer significant correlations between the errors and the data features. Additionally, there is no shared factor that significantly correlates with the error of any two algorithms. We attribute these results to having unreliable CCA correlations for the Imhonet dataset. As we have mentioned in Section 4.2, the number of users is always smaller than the number of source or target domain items in the Imhonet dataset. This, results in less significance in the canonical correlations. As we have seen in this chapter and in Table 51 in Appendix C.1, the canonical correlations between domain pairs are high, but insignificant. Consequently, although we achieve better recommendations using CD-CCA, we cannot discover any significant correlations between the error of algorithms and the CCA-related features in Imhonet.

Another reason for such a different result in the Imhonet dataset is the few number of domain pairs. Compared to the 50 studied domain pairs in the Supermarket dataset, and the 158 domain pairs of Yelp dataset, the 12 domain pairs of Imhonet dataset are too few. The few number of domain pairs results in a few number of datapoints for the correlation analysis and leads to unreliable results for that.

Finally, we have only studied the Pearson correlation between the dataset characteristics and performance of algorithms. In case there is a non-monotonic relationship between the dependent and independent variables, Pearson correlation cannot capture that. As we have seen in the scatter plots presented in Appendix A.5, B.4, and C.4, some of the variables do not follow a monotonic association with the performance of algorithms. For example, in Figure 73, the scatter plot for average rating of target domain and error of SD-SVD, has an upside down U shape.

7.3 REGRESSION ANALYSIS

Although correlation analysis can show us the general trend of relationship between two variables, it cannot determine how much each independent variable has a role in prediction of the dependent variable compared to other factors. To understand the relative importance of each of the cross and single-domain data features, explained in Section 7.1, we use multi-

variable regression analysis. In the following sections, we explain our setup for the regression analysis and report its results on each of the datasets.

7.3.1 Experiment Setup

We run multi-variable regression on the dataset features, presented in Section 7.1, as independent variables. For the dependent variable, we choose RMSE and RMSE-based improvement ratio of each of the algorithms on each of the datasets.

Because of having so many features (33), we start with the features that show significant correlations with the algorithms in Section 7.2 for each dataset¹.

Since many of the aforementioned data features can be correlated to each other, we perform a multicollinearity analysis [5] and select a subset of presented features, as the independent variables. To do this, we sort the variables based on their correlations that are reported in Section 7.2. We normalize these variables and look at their condition index and variance inflation factors (VIFs). We remove the feature that causes the maximum condition index and/or has the maximum VIF and repeat the process for the rest of the variables. We continue this process until we reach an acceptable condition index (less than 30). Consequently, we end up with a different set of variables for each of the datasets.

We run the regression analysis on these sets of variables once with the RMSE of each algorithm as the dependent variable, and once with each algorithm's improvement ratio over SD-SVD as the dependent variable, in each of the datasets. The results are reported in the following sections.

7.3.2 Regression Analysis for the Supermarket Dataset

In this dataset, we end up with 10 variables after performing the multicollinearity analysis. These variables and the results of regression on the RMSE of algorithms are listed in Table 28. This table shows the coefficients of each of the variables, with stars representing their significance, the RMSE, R^2 , and p-value for R^2 of the model.

¹We tried starting the multicollinearity analysis with all of the variables. The results were similar to, or worse than starting with the significant set of variables.

Table 28: RMSE regression analysis results for the Supermaket dataset; *: significant with p-value < 0.05; **: significant with p-value < 0.01; ***: significant with p-value < 0.001

	CD-CCA	CD-SVD	RMGM	$_{\mathrm{CMF}}$	$\operatorname{SD-SVD}$
intercept	0.4244***	0.3917***	0.4287***	0.1095	0.4319***
target mode rating	0.0018	0.0412	0.0811*	-0.2233	0.0256
mean user KL-divergence	-0.0129	0.0249	-0.0349	0.1211	-0.0143
user to source item ratio	-0.1115***	-0.0158	-0.0111	0.2977	-0.0099
CCA correlation ≥ 0.95	-0.1316***	-0.0268	-0.0419	0.1632	-0.0266
target density	0.0028	-0.0566	-0.2134***	-0.138	-0.0583
target item size	0.0149	-0.0168	-0.0661	0.005	-0.025
target skewness rating	-0.0135	-0.0543	0.0794*	0.4595**	-0.0567
source to target density ratio	0.0154	0.2252***	0.1584***	-0.2605	-0.0787
user size	0.0401**	0.1261***	-0.1154***	0.1354	0.1512***
variance user KL-divergence	-0.0156	-0.0439	0.1452**	0.5374*	-0.1199*
RMSE	0.0202	0.0514	0.0441	0.23	0.0474
P value	1.55E-06	1.12E-05	1.73E-19	1.66E-03	1.79E-08
R2	0.572	0.52	0.913	0.351	0.666

Based on the reported R^2 s, we can see that all p-values are significant. Also, we can see that although all p-values for the R^2 s are significant, the p-values of all variables are not. For CD-CCA, we see negative significant relationships between the RMSE with the number of components with CCA correlation more that 0.95 and the ratio between number of users and number of source domain items. This means that as the CCA correlation increases, the error of CD-CCA decreases. Also, as we have a taller source domain rating matrix, we have less error in CD-CCA. However, an increase in the number of users by itself increases the error. For CD-SVD, the density ratio and number of users both increase the RMSE. This means that having a denser source domain, compared to target domain, we get more error in CD-SVD.

For SD-SVD, we see a positive relationship for the number of users and a negative one for the variance in user-based KL-divergences between the source and target domains. The latter relationship is meaningless since the source domain information is not used in SD-SVD algorithm.

In RMGM, we can see that the more skewed the target domain is, we will have more error. Also, the user-based KL-divergence variance, ratio between source and target domain densities, and mode of ratings in the target domain all have a positive relationship with the error. However, the denser the target domain is and the more the number of users is, the less error we have in RMGM.

The user-based KL-divergence variance and the target domain skewness have a positive relationship with CMF's error also.

The maximum significant coefficient variable belongs to the number of canonical correlations >= 0.95 for CD-CCA, source to target domain density rations for CD-SVD, number of users for SD-SVD, target domain density for RMGM, and the variance in user-based KL-divergence of domains for CMF.

In general, we can see that the variance of user-based KL-divergence and the target domain skewness are both positively related to CMF and RMGM errors; the number of users can have a positive or negative relationship with the RMSE of algorithms; and the density ratio between source and target domains have a positive relationship with the error of both RMGM and CD-SVD.

The relationships get more clear if we look at the improvement ratios in Table 29. Here, we see that variance in user-based KL-divergence is associated with less improvement in all of the cross-domain recommenders, compared to SD-SVD. This means that as the KL-divergences of each users' ratings between source and target domains varies more, using the source domain information helps less in cross-domain recommendations. The next important factor is the density ratio between source and target domains, which is significant for IR of RMGM, CD-SVD, and CD-CCA. The denser the source domain is, compared to the target domain, the less improvement we will have in the RMSE of these algorithms compared to SD-SVD. Skewness of ratings in the target domain has a negative effect on the IR of RMGM and CMF, in accordance with its relationship with the error of these algorithms. The number of users have a contradictory effect in CD-CCA, but its relationship with RMGM is consistent. Although it has a positive relationship with the RMSE of CD-CCA, it has a positive relationship with its IR too. In other words, although the more users we have, the more the error of CD-CCA will be, we will also see more improvement over SD-SVD with

Table 29: Improvement ratio regression analysis results for the Supermaket dataset; *: significant with p-value < 0.05; **: significant with p-value < 0.01; ***: significant with p-value < 0.001

	CD-CCA	CD-SVD	RMGM	CMF
intercept	0.0685	0.1671	0.06	1.2936
target mode rating	0.0063	-0.0795	-0.3454*	0.4984
mean user KL-divergence	-0.0118	-0.161*	0.0601	-0.4848
user to source item ratio	0.2434*	0.0464	-0.0177	-0.9167
CCA correlation ≥ 0.95	0.2415	0.0163	0.0094	-0.5688
target density	-0.1324	-0.0589	0.4745**	0.0809
target item size	-0.1064	-0.0295	0.1086	-0.1517
target skewness rating	-0.1239	-0.0147	-0.4594**	-1.9305**
source to target density ratio	-0.2716**	-1.0848***	-0.7398***	0.6203
user size	0.2434***	0.1104	0.6934***	0.0982
variance user KL-divergence	-0.3685**	-0.3047**	-0.9634***	-2.5057**
RMSE	0.1023	0.0972	0.1911	0.7658
P value	2.62E-12	4.74E-18	4.59E-19	1.84E-05
R2	0.793	0.897	0.909	0.506

Table 30: RMSE regression analysis results for the Yelp dataset; *: significant with p-value < 0.05; **: significant with p-value < 0.01; ***: significant with p-value < 0.001

	CD-CCA	CD-SVD	RMGM	CMF	SD-SVD
intercept	0.4889***	0.5221***	1.9023***	0.2964	0.5979***
source kurtosis rating	-0.0022	0.1295	-0.0134	0.1188	0.0287
first component correlation	-0.0099	-0.105*	-0.4184***	-0.4066	-0.0746
target mode rating	0.2317***	0.2401***	0.2979***	0.2769	0.2486***
target density	-0.2123**	-0.3217***	0.1057	-0.3196	-0.3424***
target median rating	0.1951***	0.1286**	0.078	0.2482	0.1379**
target skewness rating	0.8091***	0.9822***	-0.4937**	1.7259	0.9036***
RMSE	0.1213	0.1317	0.1673	0.9004	0.1381
P value	2.33E-18	2.81E-19	1.06E-35	2.86E-01	6.50E-18
R2	0.449	0.459	0.682	0.00949	0.435

larger number of users. This is because the error of SD-SVD is also positively correlated with the number of users.

In addition to these relationships, IR of CD-CCA improves as we have a taller source domain rating matrix, and IR of CD-SVD improves as the average user-based KL-divergence of the two domains decreases, and thus there is more similarity between average user rating distributions. Also, as the mode of target domain ratings increases, which can be an indicator of skewness of ratings, the IR of RMGM decreases.

7.3.3 Regression Analysis for the Yelp Dataset

Table 30 shows the results of regression analysis on the Yelp dataset. As we can see here, the RMSE of the models are more than in the Supermarket dataset and the p-value of R^2 for CMF is insignificant.

Also, none of the factors are significant in the CMF model. However, skewness of ratings in the target domain and mode of ratings in the target domain both have significant relationships with the error of RMGM, CD-CCA, CD-SVD, and SD-SVD. Mode of ratings in the target domain has a positive relationship with all of the RMSEs and skewness of

Table 31: Improvement ratio regression analysis results for the Yelp dataset; *: significant with p-value < 0.05; **: significant with p-value < 0.01; ***: significant with p-value < 0.001

	CD-CCA	CD-SVD	RMGM	CMF
intercept	0.1249	0.0654	-1.1226***	0.1734
source kurtosis rating	0.0126	-0.0633*	-0.015	-0.0409
first component correlation	0.0355	0.0242	0.3663***	0.3551
target mode rating	0.0207	0.0075	0.0077	0.0296
target density	-0.2836***	-0.0669**	-0.7502***	-0.1731
target median rating	-0.0762	0.0064	0.0171	-0.1305
target skewness rating	-0.0521	-0.0762	1.1694***	-0.6705
RMSE	0.1266	0.05	0.2111	0.6657
P value	1.10E-03	4.74E-04	6.66E-24	6.79E-01
R2	0.103	0.113	0.539	-0.0133

ratings in the target domain has a positive relationship with all RMSEs, but RMGM's. Target domain's density has a negative relationship with the errors of CD-CCA, CD-SVD, and SD-SVD and the median of target domain ratings has a positive relationship with them.

Looking at the regression results for improvement ratios in Table 31, we see no significant coefficients for CMF. The density of target domain has a negative effect on the improvement of RMGM, CD-CCA, and CD-SVD, over SD-SVD; the kurtosis of ratings in the source domain has a negative relationship with CD-SVD's IR; the skewness of ratings in the target domains has a positive relationship with RMGM's IR; and the canonical correlation of the first discovered component has a positive effect on RMGM's IR.

7.3.4 Regression Analysis for the Imhonet Dataset

Table 32 shows the results of regression analysis in Imhonet dataset. We can see that although RMSEs of models are low, the p-value of R^2 in CD-CCA is insignificant and none of the coefficients are significant in this model.

For SD-SVD and CD-SVD, we see a positive relationship between their RMSEs and kurtosis of ratings in the source domain, the ratio of users to source domain items, and

Table 32: RMSE regression analysis results for the Imhonet dataset; *: significant with p-value < 0.05; **: significant with p-value < 0.01; ***: significant with p-value < 0.001

	CD-CCA	$\operatorname{CD-SVD}$	$\operatorname{SD-SVD}$
intercept	0.2182***	0.1618**	0.1794**
source to target density ratio	-0.0091	0.006	-0.0224
target var rating	0.0071	-0.0141	0.0626
source item size	0.0134	-0.0783**	-0.0433
source kurtosis rating	0.0096	0.1116**	0.0815*
user to target item ratio	0.0049	0.3044***	0.1286**
user to source item ratio	-0.0073	0.2614***	0.2398**
RMSE	0.0129	0.0121	0.017
P value	1.83E-01	3.22E-04	7.31E-03
R2	0.425	0.961	0.86

the ratio of users to the target domain items. For SD-SVD, the first two relationships are meaningless because it does not use source domain information. Also, as the number of items in the source domain increases, the error of CD-SVD decreases.

For regression on the improvement ratios, we report the results in Table 33. Here, non of the p-values of R^2 s are significant. But, we see a significant positive relationship between the ratio of users to source domain items and CD-CCA's IR; and a negative relationship between the ratio of users to the target domain items and CD-SVD's IR. This means that the taller the source domain rating matrix is, the more improvement we have in CD-CCA over SD-SVD; and the fatter the rating matrix in the target domain is, the less improvement we have in CD-SVD over SD-SVD.

7.3.5 Summary

As we can see in the regression results, there are many different factors that are important in each of the algorithms and each of the datasets. For example, the number of users is an important factor only in the Supermarket dataset, or the first component's CCA correlation is only important in the Yelp dataset.

Table 33: Improvement ratio regression analysis results for the Imhonet dataset; *: significant with p-value < 0.05; **: significant with p-value < 0.01; ***: significant with p-value < 0.001

	CD-CCA	$\operatorname{CD-SVD}$
intercept	0.0774	0.0252
source to target density ratio	-0.003	-0.0677
target var rating	0.0883	0.2254
source item size	-0.1218	0.0904
source kurtosis rating	0.1118	-0.0714
user to target item ratio	0.2152	-0.4745*
user to source item ratio	0.4171*	-0.0414
RMSE	0.0582	0.0774
P value	6.84E-02	1.17E-01
R2	0.636	0.535

There are some common important factors between the datasets also. For example, the density ratio of source and target domains appears in both Supermarket and Imhonet regression models and the source domain kurtosis appears in both Yelp and Imhonet dataset models.

However, there are two contradictory results between the datasets. The first one is related to the density of target domain. It has a positive relationship with RMGM's improvement ratio in the Supermarket dataset and a negative relationship with it in the Yelp dataset. It means that in the Supermarket dataset, the denser the target domain is, the more improvement RMGM has over SD-SVD. But, in the Yelp dataset, the denser target domain contributes to less improvement of RMGM's results.

The second one is the skewness of ratings in the target domain. In the Supermarket dataset, it has a positive relationship with RMGM's error and a negative relationship with its improvement ratio. However, this relationship works in the reverse direction in the Yelp dataset. This can be one of the reasons that leads to the good performance of RMGM in the Yelp dataset compared to the Supermarket dataset. Also, we can see that the mode of ratings in training data has a positive relationship with RMGM's RMSE. We know that in highly skewed datasets, the mode of ratings moves in the direction of skewness. So, if

the ratings are skewed towards higher ratings (which is the case for most explicit feedback recommender systems' datasets), the mode is also going to be higher. Although there is no direct correlation and collinearity between the mode and skewness of Yelp, we think that this general rule can explain some of the contradiction that we see in the regression analysis of the Yelp dataset. Basically, we hypothesize that some of the "positivity" of the relationship between skewness and RMSE of RMGM in the Yelp dataset, is absorbed by the positive relationship between the mode of target ratings and RMGM's RMSE. The same can be true for the median of target domain ratings, that appears in the Yelp dataset's regression analysis.

As for the CCA-related features, we see the number of correlations that are > 0.95 in the Supermarket dataset's regression analysis and the canonical correlation of first component in the Yelp regression analysis. We can see that the direction of their relationship, when significant, is as expected: to lower the cross-domain recommenders' error and to increase their improvement ratios. However, they are not present in the Imhonet dataset's regression analysis.

Also, we should note the number of data points in the analysis. Each domain pair is one datapoint in this regression analysis. So, we have 12 data points for the Imhonet dataset, 50 in the Supermarket dataset, and 158 in the Yelp dataset. These number of datapoints, especially for Imhonet, are not nearly enough for having a powerful regression analysis.

Eventually, we only looked at the possible linear relationships among the dependent and independent variables. Thus, we cannot find other kinds of possible relationships, such as polynomial or exponential ones. Looking at the scatter plots of independent variables and error of algorithms in appendices, we can see that most of the independent variables do not have a strict linear relationship with the dependent variables.

7.4 NATURE OF GOOD DOMAIN-PAIRS

In this part of our analysis, we look at the specific samples of domain pairs to get a deeper understanding of the results of previous analyses and answer our research question Q2.3.

More specifically, we look at the domain pairs with a high CCA to see if they can obtain a higher improvement in cross-domain recommenders versus the single-domain recommender. We examine the domain-pairs with a high CCA and low improvement in a closer look to understand the reason behind this behavior. As a reverse look at these results, we look at the domain pairs with a high improvement ratio and their characteristics. More specifically, we look at the domain-pairs with a high improvement in cross-domain recommenders versus the single-domain recommender, and a low CCA, to understand the other factors that affect this result.

First, we look at the domain pairs that have a high canonical correlation between the domain pairs and are having good results in cross-domain recommenders. In the Supermarket dataset, we see very good results in cross-domain recommendation versus single-domain recommendation in domains such as "international food \rightarrow fruit and vegetables" and "dairy \rightarrow bread". In these domain pairs, all of the cross-domain recommender systems perform significantly better than SD-SVD. Also the canonical correlation of them (calculated by the average of CCA for the first five components) is in the first 10 and 25 percentile of all domain pairs in the dataset, respectively. In the Yelp dataset, examples include "active life \rightarrow food", "food \rightarrow restaurants", and "home services \rightarrow local services". In the same way, all of the cross domain recommenders perform significantly better than SD-SVD in these domain pairs and their canonical correlation is in the first 5, 1, and 33 percentile of all canonical correlations in the Yelp dataset.

Next, we look at the domain pairs with low CCA results that have high errors in cross-domain recommendations. In the supermarket dataset, examples of these domain pairs are "bread \rightarrow events", "canned and pickled \rightarrow home outdoor", and "fruit and vegetables \rightarrow events". In these domain pairs, the single-domain algorithm has significantly less MAE and RMSE compared to all of the cross-domain algorithms. Accordingly, the canonical correlation between the domains are in the last 6, 30, and 25 percentile of all canonical correlations of this dataset. To illustrate such relationship in the Yelp dataset, we can name "active life \rightarrow hotels and travel" and "arts and entertainment \rightarrow pets" domain pairs. The canonical correlation between these domain pairs are in the last 40 percentiles of the Yelp dataset's canonical correlations. Similarly, SD-SVD performs better than all of the cross-

domain algorithms in these domain pairs.

After looking at the domain pairs with expected results in CCA and performance of algorithms, we examine the ones that act in a reverse order. Thus, we look for the domain pairs with a relatively low canonical correlation between the domains, but good cross-domain results. For example, in the Supermarket dataset, "events \rightarrow fruit and vegetables" has a very good cross-domain results: all of the cross-domain algorithms perform significantly better than SD-SVD in this domain pair. However, this domain pair's CCA in in the last 40 percentile of all CCA's in the dataset. Looking at other characteristics of this domain pair, we can see that the density ratio of source to target domain is the minimum for this domain pair in the dataset. This is associated with a high improvement ratio and thus better performance of cross-domain recommenders. Also, the number of users and items in the target domain are very close to each other in this domain pair. This, can result in unreliable CCA results. Looking at the number of components with a significant CCA in this domain pair, we can see that less than 41% of the component correlations are significant. As examples of this phenomenon in the Yelp dataset, we can name "mass media \rightarrow local flavor" and "professional services \rightarrow religious organizations". In both of these domain pairs, the cross-domain algorithms all perform significantly better than SD-SVD, but the canonical correlations are in the last 4 percentile in the dataset. In "mass media \rightarrow local flavor", the density ratio of source to target domain is high which is associated with less RMSE in the Yelp dataset. Also, we have less skewness in the "local flavor" domain (least 8 percentile) that is associated with a better result in cross-domain recommendations. Again, the number of users and target items is very close to each other and makes the CCA results unreliable. Less than half of the discovered components have a significant canonical correlation. In "professional services \rightarrow religious organizations" the target domain's density is very high (high 2 percentile) that is associated with less error for the cross-domain algorithms. Also, there are only 9 users, 9 source items, and 8 target items in this domain pair that causes less reliability in CCA results. Only one of the six canonical components have a significant correlation in this domain pair. In Imhonet, "book \rightarrow movie" has a relatively low CCA. But both cross-domain algorithms work significantly better than SD-SVD in this domain pair. Generally, we believe that we cannot trust the CCA results in this dataset because of the very high sparsity of the data. As we have seen, none of the correlations for discovered components in any of the domain pairs are significant.

In some of the domain pairs of some of the datasets, we can see a high canonical correlation, but high error of cross-domain recommenders, compared to the single-domain one. For example in the Yelp dataset, "food \rightarrow hotels and travel" has a high CCA (high 20 percentile), but SD-SVD works better than two of the four cross-domain algorithms in this pair. One reason can be the high skewness of ratings in the "hotels and travel" domain compared to other domains (high 20 percentile). Also the density of target domain is in the lower side (low 30 percentile) and the variance of user-based KL-divergence in the source and domain pairs are high that can result in more RMSE and less improvement of cross-domain recommenders. In the imhonet dataset, the canonical correlation in "perfume \rightarrow game" is high, but CD-SVD is not significantly better than SD-SVD for this domain. Also, the variance of error is very high in this domain pair. Again, for the Imhonet dataset, we cannot rely on CCA results, or correlation and regression analyses, because of the sparsity of this dataset and the few number of domain pairs in it.

Another interesting observation is that the relationship between the domain pairs is not always reciprocal. For example, in the Supermarket dataset, the "gifts" domain helps in improving the results for the "bread" domain, but adding the "bread" domain information to the "gift" domain does not help. Also, the "home outdoor" domain helps the "fruit and vegetable" domain, but the reverse is not true. In the Yelp dataset, the "nightlife" domain information improves the recommendations in the "restaurants" domain. But, the "restaurants" domain information does not add much to the "nightlife" recommendation results. On the other hand, the "health and medical" domain information helps the recommendations in the "nightlife" domain, but, the "nightlife" domain does not help the recommendations in the "health and medical" domain.

Finally, there are some domain pairs that work surprisingly well together. For example, one may not intuitively think that there is any semantic relationships between the "international food" and "home cleaning" domains in the Supermarket dataset. However, the canonical correlation of "international food \rightarrow home cleaning" is relatively high and the cross-domain algorithms have significantly less errors compared to SD-SVD in this domain

pair. The same happens for the "automotive \rightarrow nightlife" and "health and medical \rightarrow arts and entertainment" domain pairs. One may not see any relationship between user tastes in arts and their reviews on hospitals, or user reviews on night clubs and where they repair their car. But, we can see that both the canonical correlation and improvement ratios of cross-domain algorithms are high in these two domain pairs. This means that CCA can capture some unexpected, however existing, relationships between the domains.

On the other hands, there are some domain pairs that intuitively seem to be similar, but cross-domain recommenders do not work better than single-domain ones in them. For example, one may think that user preferences in the "active life" domain is related to their preference in the "hotels and travel" domain. However, the "active life \rightarrow hotels and travel" domain pair has a low canonical correlation and adding the user ratings of "active life" domain to the "hotels and travel" domain worsens the recommendations on "hotels and travel". Thus, we cannot only rely only on the "intuitive similarity" of domains in choosing them for cross-domain recommendations.

7.5 SUMMARY

In this chapter we researched on the data characteristics that can lead us towards selection of better domain pairs for cross-domain recommendations. Our goal was to answer research question Q.2, to find the factors that distinguish between a beneficial domain pair and a non-helpful one, and determine the amount of improvement in cross-domain recommenders. Also, we aimed to find out more about the nature of good domain pairs and study if they match our expectations based on intuitively similar domain pairs.

We first defined the data features in Section 7.1, based on dataset general statistics, central tendency and dispersion descriptive statistics of ratings in each of the domain pairs, divergence of rating distributions in domain pairs, and CCA-related features.

Then, we performed a correlation analysis to understand the general trend between the performance of algorithms and these data features. For measures of performance, we studied the RMSE and MAE of algorithms. For measures of improvement, we analyzed the ratio of improvement of cross-domain algorithms compared to the single-domain algorithm, calculated based on RMSE and MAE (IRs). We found out that the correlation values and their significance varies among different datasets. For example, in the Supermarket dataset, the denser the target domain is, the more improvement we will have in cross-domain recommendations. But, this correlation works in reverse in the Yelp dataset. Even in the same dataset, some of the data characteristics had a different effect on different algorithms' results. For example, in the Yelp dataset, the improvement ratio of RMGM algorithm decreases by more skewness in the target domain's ratings. However, more skewness is associated with more improvement ratio in the CMF algorithm.

Among all of the data characteristics, the CCA-related features and the divergencerelated features performed most consistently among the datasets. Mostly, the CCA-related features had a positive correlation with improvement ratio of algorithms and a negative one with the error of algorithms. Also, the KL-divergence between all ratings in the source and target domains mostly have a negative correlation with the improvement ratio of crossdomain algorithms.

To uncover the relative linear relationship of these data characteristics with error and improvement ratios of algorithms, we performed regression analysis in Section 7.3. Before that, we looked at the multicollinearities among the variables and removed the problematic features. We ended up with different variables in each of the datasets. Then, we modeled the RMSE and RMSE-based improvement ratio of algorithms with these features in a linear model. In summary, the regression model usually did not explain all of the variability in the data; which is expected. Because each of the algorithms have a complicated approach to estimate user ratings and this complicated task cannot be completely modeled with a linear regression analysis. Based on the regression results, we encountered with some contradictory relationships between the features and our dependent variables. On the other hand, we discovered that CCA-related features, in both Yelp and Supermarket datasets, work as we expect: if they have a significant relationship, they work towards less error and more improvement ratio. Although the size of the effect is very small in these factors.

Finally, we studied the domain pairs that had unexpected behaviors: the ones with high CCA and low cross-domain performance, the ones with low CCA and good cross-domain

performance, the ones which are intuitively close to each other but had a bad cross-domain performance, and the ones that had a good cross-domain performance but were not intuitively close to each other. In the cases with low CCA and high performance, or vice versa, we have seen that other features of domain pairs are working towards getting these surprising results. Also, in most of them, CCA results were not as reliable as we would have expected.

As a whole, we conclude that different variables are effective for each of the algorithms in each of the datasets and we achieve different results in each setting. Some of the differences are because of the different nature of each of the datasets. For example, the Supermarket dataset is denser than the other two datasets and is less skewed. It does not reveal the "rating" of users on the items, but their purchase history. On the other hand, the Imhonet dataset is very sparse. As a result, the canonical correlations in this dataset are not significant. However, the canonical correlation between all domain pairs are very high in this dataset. To illustrate, the least value for average of canonical correlation in the first five components in Imhonet is more than 0.8; while for Yelp, the minimum value for this factor is less than 0.5 and for the Supermarket dataset, it is less than 0.3.

Also, we conclude that CCA-related features, although not always significant, and although having a small effect size, work mostly similar in different datasets and algorithms. Additionally, based on the surprising domain pairs that we studied in Section 7.4, we decide that CCA can capture some relationships that may not be intuitively meaningful to us, but lead to better cross-domain recommendations. Yet, CCA alone may not be sufficient in finding the best matches for some domains. Other, dataset-dependent variables, can change the way two domains work together in cross-domain recommendations.

8.0 AUXILIARY DOMAIN CLASSIFIER

This chapter of dissertation aims to find answers to research question Q3, defined in Section 1.2. More specifically, we would like to examine if we can classify the domain pairs based on the data characteristics defined in Section 7.1. The dependent variable for this classification is if a domain pair is an appropriate pair for cross-domain recommendation or not. In other words, if it is beneficial, in terms of the error of recommendation results, to use cross-domain recommenders in each domain pair; or having the single-domain recommendation on the target domain is good enough.

Having such classifier in hand, one can decide on the usefulness of an auxiliary domain, for a specific target domain, before performing the cross-domain and single-domain recommender algorithms. In the next sections, we first explain the setup under which we run the experiments, then we present the results of experiments, and summarize them.

8.1 EXPERIMENT SETUP

As we have concluded in the previous chapters, and we can see in the figures in Appendix A.5, B.4, and C.4, the more improvement ratio of cross-domain algorithms does not always mean that there is a significant improvement of cross-domain algorithm over the single-domain one. Thus, we do not select error or improvement ratio as our dependent variables in this chapter. Since we would like to discover the domain-pairs that have better results in cross-domain recommender systems, compared to the single-domain ones, the dependent variable in this classifier should represent such characteristic. The choice of dependent variable for such classifier is based on our goals to study the feasibility of detecting beneficial domain

pairs. A domain pair is beneficial, using a specific cross-domain algorithm, if adding the information of the source domain to the target domain and applying such algorithm provides us with better results compared to using the single-domain recommender algorithm only on the target domain data. As a result, we choose a binary variable (SigIndx) that indicates if a cross-domain recommender has performed significantly better than the single-domain recommender. To be more clear, if \ll represents the "significantly less" relation between error of algorithms¹, and a_i represents one of the cross-domain algorithms, then Equation 8.1 explains the dependent binary variable calculated over SD-SVD algorithm. We use the RMSE of algorithms as the measure of error.

$$SigIndx_{a_i,SD-SVD} = \begin{cases} 1, & \text{if } Error_{a_i} \ll Error_{SD-SVD} \\ 0, & \text{otherwise} \end{cases}$$
(8.1)

Note that this is one possible definition of gold-standard for class labels and the classifier that we can use. It is possible to have other definitions for SigIndx. For example, the domain pairs that work significantly better than SD-SVD in all cross-domain algorithms. However, we do not experiment on this definition because of the diverse results that we are getting from different cross-domain algorithms. In other words, each of the cross-domain algorithms have their own strength and weaknesses that relate to domain-pair characteristics. Thus, the number of domain-pairs in which all of these algorithms work significantly better than SD-SVD is very limited.

Also, it is possible to have a multi-class classifier instead of a binary classifier. For example, we can train the classifier based on the set (or number) of algorithms in which a domain pair performs significantly better than SD-SVD. However, since the focus in this dissertation is to study the feasibility of distinguishing between beneficial and non-beneficial domain pairs, we focus on the simple case of a binary classifier for each of the algorithms.

Since we have four different cross-domain algorithms, we train the classifier four times, every time based on the performance of one of them versus SD-SVD performance.

To test the generalizability of the trained classifiers, we explore three general setups: a) having the test and train domain pairs from the same dataset to see how accurate the

 $^{^{1}}$ p-value < 0.05

classifier is within a specific domain nature or system; b) having the train domain pairs from one dataset and the test domain pairs from another dataset to see how much this classifier can be accurate on other domains with a different nature and how much does this meta-knowledge transfers between the domains with various nature; and c) mixing the domain pairs of two datasets with different natures and training a classifier on this mix to see the effect of a this merge on their results.

We use 5-fold cross-validation and repeat the experiments for five times. So, in general, we run the experiments 25 times on each dataset.

For the independent variables, we remove the central tendency features because they had less variability and added to the error of classifiers. We use all of the rest of features as dependent variables. However, to better understand the role of CCA-based features in classifying the good domain pairs, we run the experiments with three different sets of independent variables: a) using all of the data features; b) using all of the data features except the CCA-related features; and c) using only the CCA-related features. By this setup, we want to understand if the CCA-related features play an important role in the classification of good domain pairs or not. We compare these setups with a random classifier as baseline. To be more specific, we calculate the probability of misclassification, if we assign each domain pair to a class in random. We use the dataset priors for this random classification. For example, if the positive class happens in 70% of the times in the dataset, we calculate the probability of misclassification based on a random classifier that returns a positive label in 70% of the times.

Eventually, we use linear Support Vector Machine (SVM) classifier to run the experiments².

To evaluate the classifier, we use classifier error as our loss function. In other words, we count the number of misclassified domain pairs as the loss of SVM.

In the following sections, we present our results in each of the experiment settings for all of the datasets.

²We tried the RBF and polynomial kernels, but the results of linear classifier were better. Also we use the "fitsym" function in Matlab as the implementation of SVM.

Table 34: Percentage of positive class labels in each dataset

	Supermarket	Yelp	Imhonet
CD-CCA	70	48.73	100
CMF	14	46.2	N/A
RMGM	72	12.03	N/A
CD-SVD	8	5.7	16.67

8.2 WITHIN DATASET CLASSIFICATION

In this section, we experiment on the classification of beneficial and non-beneficial domain pairs in each of the datasets. We run 5-fold cross validation over the 158 domain pairs in the Yelp dataset, 50 domain pairs in the Supermarket dataset, and 12 domain pairs in the Imhonet dataset.

Table 34 shows the percentage of these domain pairs that have a significantly less RMSE compared to SD-SVD, and thus, have a positive class label.

We run SVM on each of these datasets with three independent variable sets and a random baseline. The results of this classification on the Supermarket dataset is shown in Figure 43.

As we can see in this picture, the SVM classifier performs better than the random labeling in almost all of the algorithms with most of the variable sets. In predicting the classification labels for CD-SVD, the CCA-related set of features performs better than the random class label assignment. However, using all of the variables or all, except CCA-related ones perform similar to random assignment of class labels. Although relying on only CCA-related features have the best performance for CD-SVD, for the rest of the algorithms, adding or removing the CCA-related features in the set of independent variables, does not change the loss of classifier significantly.

Figure 44 shows the results of running SVM on the Yelp dataset. In this dataset, the SVM classifier always performs better than random class assignment. Both CCA-related

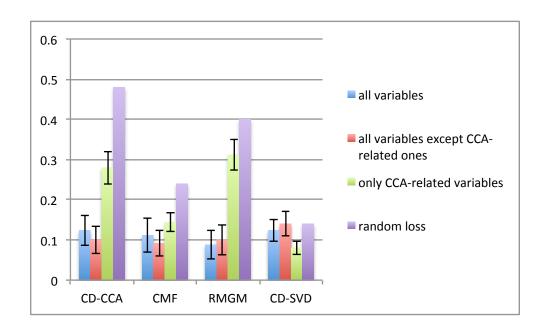


Figure 43: Classification loss in the Supermarket dataset

features and data features except the CCA-related ones, build the best classifier for CD-SVD. However, in classification of the other algorithms' results, although classifying the domain pairs based on only CCA-related features performs better than random assignment, adding CCA-related features does not significantly change the classification loss. So, in these cases, we can predict if a domain-pair will be beneficial in the cross-domain setting, by looking at the rest of the data features.

Figure 45 shows the classifier loss on the significance of error on domain pairs in CD-SVD algorithm in the Imhonet dataset. Since we always have a significantly better results in CD-CCA, compared to SD-SVD, in this dataset, all the losses for this algorithm is going to be zero. So, we do not show it here. In this picture, we can see that the SVM built on only CCA-related features and all features are doing better than the random classifier. However, having all of the features except for CCA-related ones does not perform significantly better than the random classifier.

In summary, we see that in all of the datasets, we can predict if a domain pair is suitable for cross-domain recommendation or not using the data features. Our prediction works

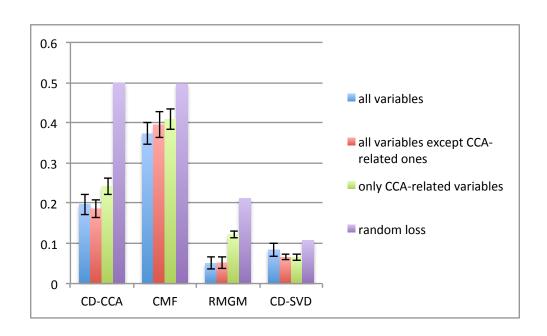


Figure 44: Classification loss in the Yelp dataset

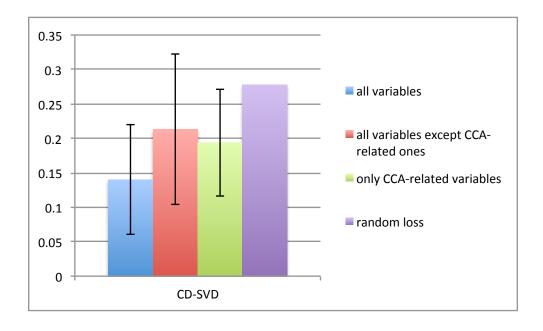


Figure 45: Classification loss in the Imhonet dataset

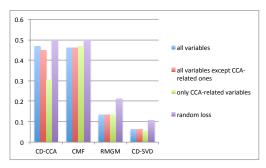
better than a random prediction that is based on the dataset priors. Also, we have seen that CCA-related features are important to classify domain pairs for the CD-SVD algorithm. However, for the rest of the algorithms, adding these features does not significantly change the results of a classifier that is built upon the rest of the features. But, it does not harm the results either.

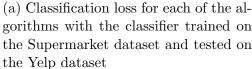
8.3 CROSS DATASET CLASSIFICATION

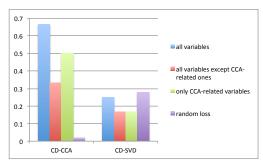
In this section, we test the generalizability of the classifier for domain pairs, by training it on one dataset and testing it on another dataset. Again, we use three sets of independent variables and compare the classifier's results with a random classifier.

Figures 46a and 46b show the results of classifiers trained on the Supermarket dataset and tested on the Yelp and Imhonet datasets. As shown in these figures, except for CD-CCA in Figure 46b, the cross-dataset classifier performs better than the random classifier, that is based on the target dataset priors. The reason that SVM performs bad in comparison with the random classifier for CD-CCA in Imhonet is that there is no negative class labels for CD-CCA in that dataset. This happen because CD-CCA always performs significantly better than SD-SVD in the Imhonet dataset. In the rest of the experiments, we can see that the classifiers trained on CCA-related features only perform better, or similar to the classifiers trained on the rest of the dataset features, or all of the dataset features. Especially in the classifier for CD-CCA in Yelp and for CD-SVD in Imhonet, we can see that the classifier trained on CCA-related features of the supermarket dataset performs much better than the other classifiers.

Figures 47a and 47b show the loss of the classifiers trained on the results of algorithms in the Yelp dataset and tested on the Supermarket and Imhonet datasets. Again, we can see that the cross-dataset classifier that is trained on CCA-related features only performs the best and better than the random classifier in all of the settings (The CD-CCA data in the Imhonet dataset does not have a negative class label, and thus is not reliable). For the classifiers trained on all of the variables, we mostly see better results, compared to the







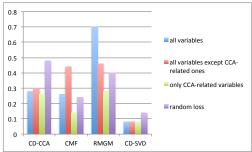
(b) Classification loss for each of the algorithms with the classifier trained on the Supermarket dataset and tested on the Imhonet dataset

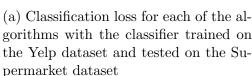
Figure 46: Classification loss for cross-dataset experiments; trained on the Supermarket data

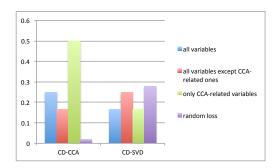
random baseline. Also this classifier is mostly better than the one trained on all, except CCA-related, features. Only in RMGM results tested on the Supermarket dataset, the all-variables classifier performs very poor, and even worse than the random baseline.

In figures 48a and 48b we see the loss of the classifiers trained on the results of algorithms in the Imhonet dataset and tested on the Supermarket and Yelp datasets. As for the previous experiments, we cannot trust the CD-CCA results, because the classifier trained on the results of this algorithm in the Imhonet dataset always returns the positive label. For CD-SVD, we can see that the SVM trained on CCA-related features performs better than all other classifiers. The other two classifiers even perform worse than the random baseline.

Eventually, these experiments show that the classifiers trained on the domain pairs in one dataset can mostly be transferable to the domain pairs of other datasets. However, the classifiers trained only on the CCA-related features are the ones that perform the best in this transfer.







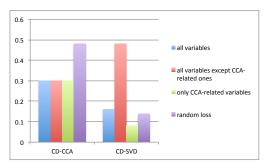
(b) Classification loss for each of the algorithms with the classifier trained on the Yelp dataset and tested on the Imhonet dataset

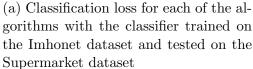
Figure 47: Classification loss for cross-dataset experiments; trained on Yelp data

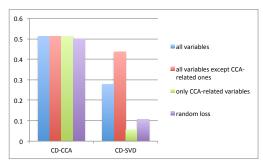
8.4 MIXED DATASET CLASSIFICATION

In this section, we experiment on transferability of domain pair classifiers by training them on a set of domain pairs coming from mixed datasets. To be more specific, we select each two datasets, merge the domain pairs features and the results of algorithms on them together, and run the classification experiments with 5 fold cross-validation on this mixed dataset. Consequently, the test and train domain pairs come from both of these datasets. As a result of this mixing, the percentage of positive labels in the new merged datasets are going to be different with the original ones, and thus, the performance of random baseline will change with that. Table 35 shows the percentage of positive class labels for each of the algorithms in each of the datasets.

Figure 50 shows the loss of SVM classifiers for the mix of Imhonet and Supermarket datasets. As we can see here, the classifiers trained on CCA-related features are all performing significantly better than the random baseline and better than the other classifiers. In most of the cases, the classifiers trained on all data features, and the ones trained on all, but CCA-related, features are also performing better than the random baseline. The only







(b) Classification loss for each of the algorithms with the classifier trained on the Imhonet dataset and tested on the Yelp dataset

Figure 48: Classification loss for cross-dataset experiments; trained on Imhonet data

case in which a classifier performs worse than the random baseline is the SVM trained on all features, for the CD-CCA algorithm.

Figure 50 shows the loss of classifiers on the mix of Supermarket and Imhonet datasets. Here, since because of the merge of the datasets, the label for CD-CCA algorithm is not always positive, we can actually test the classifiers' performance for this algorithm. As shown in the figure, in the classifiers trained on CCA-related features perform significantly better than all other classifiers and the random baseline, in both CD-CCA and CD-SVD algorithms.

Table 35: Percentage of positive class labels in each mixed dataset

	Supermarket + Yelp	Yelp + Imhonet	Supermarket + Imhonet
CD-CCA	53.84	52.35	75.81
CMF	38.46	N/A	N/A
RMGM	26.45	N/A	N/A
CD-SVD	6.25	6.47	9.68

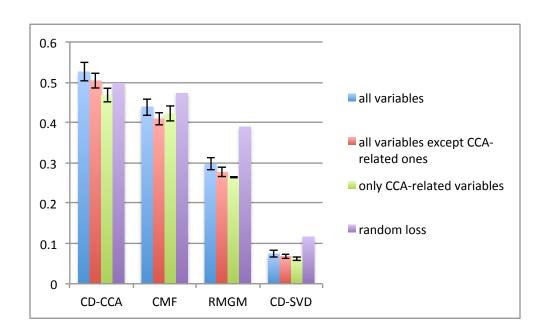


Figure 49: Classification loss in the mix of Supermarket and Yelp datasets

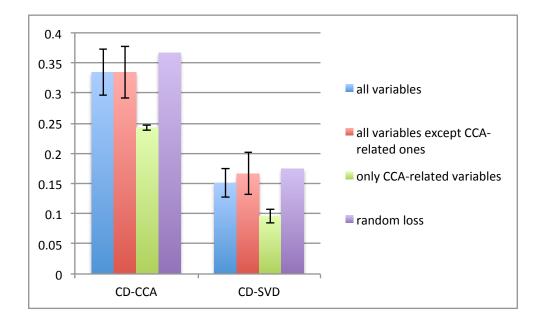


Figure 50: Classification loss in the mix of Supermarket and Imhonet dataset

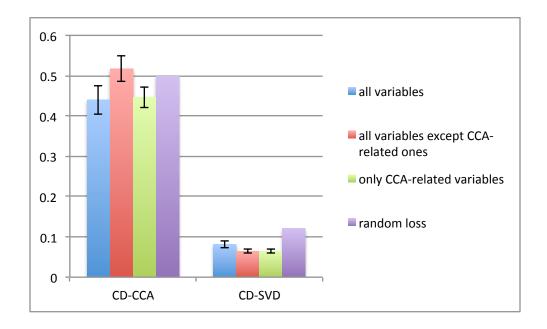


Figure 51: Classification loss in the mix of Yelp and Imhonet dataset

The results of the other two classifiers are comparable with the random baseline.

In Figure 51, we can see similar results for the mix of Yelp and Imhonet datasets. Again the classifier trained on CCA-related features is performing significantly better than the random baseline and better than the other two classifiers.

To summarize, we can see that the classifiers that are trained on the CCA-related features perform better in finding out the suitable domain pairs for cross-domain algorithms in the mixed datasets.

8.5 SUMMARY

In this chapter of the dissertation, we experimented on feasibility and generalizability of a domain-pair classifier, that can distinguish between suitable and non-suitable domain pairs for cross-domain recommendation. We have seen that the trained classifiers in general perform better than random baselines. We experimented on three different setups to research on within dataset, cross dataset, and mixed dataset classifiers. The results show that the trained classifiers can transfer the knowledge between datasets with very different natures and characteristics.

Also, we used three different sets of independent variables to examine the importance of CCA-related features in the classifiers. We noticed that in the within dataset experiments, adding CCA-related features does not boost the performance of domain pair classifiers. Using other dataset features can be as good as using the CCA-related features while working with one dataset. However, the classifiers trained on CCA-related features performed very well in mixed and cross dataset experiments. Thus, for the results to be generalizable beyond one dataset, we should rely on the CCA-related features.

Comparing the results of within dataset and cross dataset classifiers in the Supermarket and Yelp datasets, when trained on all features or all except CCA-related features, we can see that the loss of algorithms in the within dataset classifiers is less than the ones in the cross dataset classifiers. However, for the Imhonet dataset, the loss of within and cross datasets are very close to each other. This means that, if available, using domain pairs from the same dataset to train the classifier, provides us with a more accurate domain pair classifier. Also, for the classifiers trained on CCA-related features, the results of within and cross dataset classifiers are similar to each other. This leads us to using CCA-related features for training a classifier if the domain pair data from the same dataset is not available.

Eventually, since CCA-related features do not harm the within dataset classification results, and improve the mixed and cross dataset results, it would be better to keep them in the classifier.

Finally, to answer research question Q3, we conclude that having a domain pair classifier, although not perfect, is feasible and beneficial for cross-domain recommendation.

9.0 CONCLUSIONS AND DISCUSSION

In this chapter, we discuss the contributions of the proposed thesis, its limitations and delimitations, and the possible future work.

9.1 CONCLUSIONS

Our goals in this dissertation were to explore the added value of cross-domain recommendations in comparison with traditional within-domain recommendations, and to achieve some progress in uncovering the main mystery of cross-domain recommendation: how can we determine whether a pair of domains is a good candidate for applying cross-domain recommendation techniques?

To explore the cross-domain recommender systems' value, we proposed a cross-domain collaborative filtering approach, and its large-scale version, based on canonical correlation analysis in Chapter 3. To achieve the goals of this dissertation, we also designed the research questions Q1 to Q3 in Section 1.2.

The first question studies the feasibility and benefit of cross-domain recommender systems. The first part of this question (Q1.1) focuses on the reasons behind getting better results in cross-domain recommendations: if the better results are because of the additional data, better algorithms, or both of them. To answer this question, we performed a study as explained in Chapter 5. We examined the success and failure of our proposed approach, three other cross-domain collaborative filtering baselines, and a single-domain recommender system. We used three different datasets, introduced in Chapter 4, with various characteristics in the number of domains, nature of domains, and size of data to run the experiments.

We noticed different behavior of the algorithms in different datasets and discussed the potential reasons for these irregularities and their relationships to the design of cross-domain algorithms. For example, a potential reason for RMGM algorithm to perform very well in the Supermarket dataset and very poorly in the Yelp dataset is skewness of the Yelp dataset, compared to the Supermarket dataset. From these experiments, we concluded that both extra information and the approach that uses this extra information are important in achieving better results in cross-domain recommender systems. We have seen that CD-SVD algorithm sometimes perform better than SD-SVD algorithm, only because it has access to more information about the users from the source domain. Also, in many domain pairs in all of the datasets other cross-domain algorithms including our proposed CD-CCA has performed better than CD-SVD. All of these algorithms had both domains' data as their input, but they had different approaches to use this data.

Additionally, we observed that not all of the domain pairs in all of the datasets are suitable for cross-domain recommendations. For some of the domain pairs, especially in the Supermarket dataset, the single-domain recommendations can work better than the cross-domain ones.

We analyzed the time performance of algorithms and concluded that one of the strong points for the proposed CD-CCA is its time performance; it is the fastest cross-domain algorithm in average-sized datasets. In large-scale datasets CD-LCCA has a reasonably good time-performance.

The second part of first question (Q1.2) concentrate on the cross-domain collaborative filtering in the cold-start setting. Since one of the major contributions of the cross-domain collaborative filtering is assumed to be in the cases where there is too little information (ratings) available by users, we would like to understand how each of the cross-domain approaches perform in this setting, compared to the single-domain algorithm. The study designed in Chapter 6 aims to answer this question. In this chapter, we studied the trend of errors of algorithms based on the user profile sizes in both target and source domains. We examined this trend both by looking at the average errors over all of the domain pairs, and the error trend in each of the domain pairs of the three datasets. In some cases of the extreme cold-start situation CD-SVD and SD-SVD were not able to recommend any

items to users. But, other cross-domain algorithms could recommend items with reasonable errors in these cases. We noticed an initial increase on average error, by target profile size increase in the cold-start setting that was attributed to the large number of domain pairs that had very small user profiles. Also, we have seen a decrease of error with larger target profile sizes in most of the cross-domain recommenders that was attributed to having more information about users and thus better recommendation results. We notices that RMGM algorithm performs very poorly in the extreme cold-start setting, when users have only one item in their target profile. We noticed that error of SD-SVD is surprisingly associated with source domain profile sizes and hypothesized that this phenomenon is because of a third factor correlated with both source domain profile size and error of SD-SVD. Also, we have seen that CD-CCA can use the external source information while avoiding the noise that comes with it. Based on these trends we concluded that CD-CCA can handle the cold-start problem better than the baseline cross-domain recommenders. Additionally, we inferred that the cross-domain algorithms can especially help the results in the cold-start setting.

Having answered the first research question, we studied the reasons behind the observed performance of cross-domain approaches by designing the experiments in Chapter 7. In this chapter we examined the three parts of our second research question: we studied canonical correlations between the domains, in addition to various dataset and domain-pair characteristics, as possible predictors of successful domain pairs. We concluded that, for each of the algorithms in each of the datasets, a different set of variables can have significant relationships with the performance of the algorithms. The size and direction of these relationships varied among the datasets and algorithms. The most consistent associations among the datasets and algorithms were CCA-related features and features related to KL-divergence. We discussed potential reasons for having such inconsistent or insignificant results, including few number of datapoints (domain pairs), only checking the linear associations or monotonic correlations, and different nature of datasets. We looked at domain-pairs with surprising and unexpected behaviors to understand if empirical behavior of domain pairs matches our intuitive expectations from them. We noticed some domain-pairs with high CCA and poor cross-domain performance, low CCA and good cross-domain results, and high CCA with good results that did not seem to have any intuitive relationship. We concluded that CCA, as a tool in detecting beneficial domain-pairs, can discover some counter-intuitive but useful relationships that lead to good cross-domain performance. However, it is better to rely on a combination of dataset characteristics and CCA of domain pairs to select the best-performing domains.

Finally, in Chapter 8.3, we answered the third research question (Q3): if we can classify the domain pairs into beneficial and non-beneficial ones for performing cross-domain recommendation. We designed a study that uses a SVM classifier to distinguish between the domain pairs with significantly better cross-domain recommendations, compared to the single-domain ones. We used three different sets of features (independent variables) to study the effect of CCA-related features in the classifiers. Also, we designed three setups for within dataset, cross dataset, and mixed dataset classification of domain pairs. In brief, we discovered that it is possible to classify the domain pairs into appropriate and inappropriate ones for cross-domain recommendations, with some error. We noticed that in most cases, adding the CCA-related features does not change the classification results within one dataset significantly. However, for having a transferable classifier among the datasets or a classifier on a mixed dataset, the CCA-related features work the best. Thus, we concluded that they play an important role in general for classifying the appropriate domain pairs for cross-domain collaborative filtering.

On the whole, we have concluded that: a) cross-domain collaborative filtering is useful in some domain pairs if the appropriate approach is selected to handle the extra information of the source domain; b) it helps to alleviate the cold-start problem (especially the proposed CD-CCA approach); c) some dataset-dependent data characteristics can define if a domain pair is a good selection for cross-domain recommendation or not; d) the CCA-related data characteristics are the most consistent ones across multiple datasets; e) however, it is better to rely on a mix of dataset features and CCA-related ones in figuring out the best domain pairs using correlation and regression analyses; and f) we can classify domain pairs into beneficial and non-beneficial domain pairs before performing the cross-domain recommendations a1) relying on dataset descriptor data features for within dataset classifications; and a2) relying on CCA-related features for generalizable cross and mixed dataset classifications.

¹with some classification loss that is less than random loss.

9.2 CONTRIBUTIONS

Although cross-domain recommender systems have been the focus of some researches recently, the past studies mostly focus on the feasibility of cross-domain recommenders and its benefits. In this thesis, we discovered that there are more complexities involved in performance and benefits of cross-domain recommenders: it may depend on the dataset, algorithm, and specifically choice of domain pairs.

To discover these complexities and the factors behind them, we proposed a cross-domain recommendation method based on canonical correlation analysis (CD-CCA) and its large-scale version (CD-LCCA) that can take into account the relatedness of domains while transferring the knowledge from one domain to the another. We tested the performance of this method with three baseline cross-domain and one single-domain recommenders on three different datasets. We explored the feasibility and benefit of cross-domain recommenders in the general, and cold-start settings. We performed correlation analysis and regression analysis on various dataset features to understand the cues that lead us in selecting the best domain pairs. We proposed CCA as the main data feature to distinguish between domain pairs. Finally, we proposed a domain pair classifier to distinguish between appropriate and not appropriate domain pairs, and studied the domain pairs with unexpected behaviors.

In summary, our contribution in this thesis are be as follows:

- To the best of our knowledge, we presented the first large scale study that examines the value of cross-domain recommendation approaches in a broad and diverse set of domain pairs.
- We designed a new cross-domain recommendation approach based on Canonical Correlation Analysis (CD-CCA) as well as the large-scale version of it (CD-LCCA).
- We conducted a study on the performance of this approach and baseline approaches to find out:
 - if the cross-domain recommendation results only improve because of added information, or if the recommendation algorithm also matters; and
 - if the cross-domain recommenders alleviate the cold-start problem.

- We designed a detailed set of experiments by correlation and regression analysis of dataset characteristics with the error and improvement of cross-domain approaches to find out:
 - the single-domain and domain-pair data characteristics that affect the prediction error of approaches;
 - the single-domain and cross-domain data characteristics that affect the amount of recommendation improvements; and
 - the nature of suitable domain pairs.
- We built a domain pair classifier that can distinguish between helpful and unhelpful domain pairs for each recommender algorithm.

Our contributions in this thesis will be useful in finding if a domain pair are suitable for cross-domain recommendations before performing the recommendations, finding the best auxiliary domains when alleviating the cold-start problem in a target domain, finding more reliable information about users of a domain, and performing cross-domain recommendations in datasets having shared users.

9.3 LIMITATIONS AND DELIMITATIONS

The limitations and delimitations of the proposed thesis are derived from both the data used for the studies, and the proposed approaches.

This study utilizes data from three resources, imposing several limitations to this research:

- All three datasets are sparse. Although it is natural in the domain of recommender systems to have sparse dataset, this sparsity might affect the results and our confidence in them.
- There are few domains in the Imhonet dataset compared to the other datasets. This results in less confident analysis for the relationship between data characteristics and recommendation results and less accurate predictions in the classifier.

- Although this dissertation is on cross-domain collaborative filtering recommender systems, two of the datasets are not based on classic ratings ("tastes") in the items they purchases. The Yelp dataset has user ratings, but is on business services rather then for individual products and services. The Supermarket dataset includes implicit "taste" of customers in their purchases, but it does not have an explicit preference feedback, nor the decision of user to rate an item or not. Only in the Imhonet dataset, we have an explicit rating of users on items, based on their taste.
- The Imhonet data was collected while there was a recommender system active in the system. Also, some of the users are guided to provide at least 20 ratings in the movies and books domains. This might cause a bias in the preference ratings of users and affect the analysis and recommendation results.
- The Supermarket dataset is gathered from purchases of people with special discounts in some domains (more specifically, healthy foods). This might cause a bias in the purchasing pattern of customers that can affect the analysis and recommendation results.

In addition, the following limitations and delimitations exist with regards to the approaches proposed in this thesis:

- While the data in recommender systems are sparse, CD-CCA assumes that it has access to all of the training records. To alleviate this problem, we use a common rule of thumb in recommender systems and fill in each of the unknown training records with an average rating calculated by average user rating, average item rating, and the global average of the data.
- CD-CCA is only able to capture the linear relationship between the domains. While there might be some non-linear relationship between the domains, CD-CCA is unable to capture it because of the linear nature of CCA. Kernel-CCA methods can capture the non-linear relationship between the domains. However, using kernel-CCA for recommendation requires a mapping from the source space to the kernel space and from the kernel space back to the target space, and performing the latter is not feasible in the extent of this thesis.
- The proposed approaches require shared user sets between the source and target domains.

- Because of the large size of Imhonet dataset and slow performance of RMGM and CMF algorithms we were not able to report their results in the dissertation.
- We only have four baseline approaches in the thesis. The results may not be generalizable to all recommendation approaches.
- The regression and Pearson correlation analyses of Chapter 7 rely on linear and monotonous associations among dependent and independent variables. As a result, we cannot find other possible associations in the data, including non-monotonic, polynomial, or exponential relationships.
- The analyses we performed in Chapter 7 lack enough power to make strong conclusions.
- Even after removing multicollinearity from the variables in Chapter 7, some of the regression models were not significant. This can be because of the few number of datapoints, the complicated nature of the dependent variables, or the hidden relationships between the dependent variables.
- Our approaches are not discovering any causal relationships between the dataset features and the recommender system results by performing the analyses.
- While other settings can be defined to classify between beneficial and non-beneficial domain pairs, the classifier presented in this thesis is a binary linear classifier distinguishing between significantly better performing cross-domain algorithms compared to SD-SVD. Thus, it does not capture possible non-linear relationships that may exist in the data.
- All of the experiments are on offline datasets and may have different results in the wild.
- This thesis is focused on empirical aspects of cross-domain collaborative filtering and does not analyze the effects of adding external source domain data theoretically. While having empirical evidence for the benefits and disadvantages of cross-domain recommender systems is valuable and needed, it is important to support this evidence with theoretical definitions and proofs. It can provide a strong foundation for the empirical results that we have seen in this dissertation and explain them.

9.4 FUTURE WORK

Popularity of cross-domain recommender systems is increasing because of their promises for alleviating problems such as cold-start and sparsity. However, there are many aspects of these type of recommender systems, such as domain pair selection, intelligent transfer of information from the source domain to the target domain, domain definition, and large-scale algorithms, that need more research. Although we have done an extensive study on domain pair selection in this thesis, the definition of domains are coming from predefined, manual, categorization of items. One of the research questions that can be addressed in continuation of this thesis is what makes a domain definition to be good. Especially in datasets similar to the Supermarket dataset, the item domains can be very similar to each other. Defining metrics to define a good domain and automatic ways to separate the domains based on these metrics can be an interesting extension of this work.

In this thesis, our focus was on finding out the data characteristics that can lead to a good domain pair and the feasibility of domain pair classification for the cross-domain recommendation. Study on different classifier approaches in different setups or nonlinear association analysis may provide a better idea on finding the best domain pairs for a dataset.

In addition to the empirical studies reported in this thesis, a future direction can take a theoretical view to the problem to analyze the effect of adding extra source domain information, with different dataset characteristics, to the recommendation results. As we have discussed in the limitations section, a theoretical analysis can strengthen the empirical results and explain the irregularities in them. Given the limited literature on this aspect of cross-domain recommenders, such work can be very valuable.

Our proposed approaches (CD-CCA and CD-LCCA) work on a complete matrix of ratings. As another possible future work in this thesis, a sparse version of these algorithms that relies on the observed user ratings only, and thus an approximation of CCA, can be developed. Similarly, an online version of these algorithms can be developed to be deployed in a real world setting. In this case, one can experiment on the real-time recommender system and extend the evaluations with A/B testing. Another possible extension for the proposed algorithms is adopting them for the implicit feedback data. Here, we transformed

the implicit feedback in the Supermarket dataset to a similar rating scale. However, we can design an algorithm that models the implicit feedback directly.

Another focus of this dissertation was on pairs of domains. An interesting research direction can be studying the effect of multiple auxiliary domains on the target domain recommendations, either having a CCA-based algorithm or other transfer learning approaches. On of the challenges for this research would be designing an evaluation framework for it. Since the number of different combinations for a set of source domains is exponential, evaluating the best selection of domains need some heuristics to reduce the search space for this problem.

Finally, we have only researched on collaborative filtering cross-domain approaches. However, there are many other possible resources, such as texts, tags, and context, that can be used in cross-domain recommendations. Including these resources in the cross-domain recommender systems may both boost their performance and increase their interpretability. For example, we may find out some domain similarities by analyzing the texts associated with two domains. In a related note, we have used the word "semantics" for two heuristically similar domains. Using the text associated with domains we can check if there are any semantics that can be discovered between such domains.

APPENDIX A

SUPERMARKET DATA FIGURES AND TABLES

A.1 SUPERMARKET DATA DOMAIN MAPPING

Table 36: Mapping of supermarket item categories to domains

alcoholic drinks & cigarrettes	spirits	28
alcoholic drinks & cigarrettes	beer	34
alcoholic drinks & cigarrettes	wine	110
alcoholic drinks & cigarrettes	cigarettes/tobacco	1502
beauty	soaps & body wash	8580
beauty	skin care	5800
beauty	mens toiletries	5042
beauty	health & beauty gift	78
beauty	hair care	10213
beauty	hair accessories	15
beauty	facial tissues	7368
beauty	deodorants	6988
beauty	$\operatorname{cosmetics/toiletries}$	2009
beauty	beauty/trial travel	2278
bread	instore bread	24174
bread	bread rolls & fbread	8586
bread	bh bought in easter	29
bread	bakery bought in	26599
canned & pickled	pickled vegetables	3332
canned & pickled	meal bases	14939
canned & pickled	canned veg	16026
canned & pickled	canned meals	4961

parent category (domain)	subcategory	number of records in subcategory
canned & pickled	$\rm antip/olive/dip/pate$	6441
clothing	seasonal apparel	358
clothing	mix womenswear	2489
clothing	mix menswear	288
clothing	mix girlswear 2-6	463
clothing	mix boyswear 2-6	293
clothing	mix babywear	414
clothing	menswear	1
clothing	ladieswear	2
clothing	hosiery	1708
clothing	girlswear	1
clothing	family underwear	731
clothing	family socks	1324
clothing	boyswear	1
clothing	babywear	386
cooking essentials	vinegar	1499
cooking essentials	sugar/sweeteners	5759
cooking essentials	spices/herbs	8086
cooking essentials	sauces/relish	10527
cooking essentials	salad dressings	4278
cooking essentials	rice	6409
cooking essentials	pasta	12226
cooking essentials	oils	4683
cooking essentials	flour	3820
cooking essentials	cooking	14359
dairy	spec/fresh cheese	3416
dairy	grocery milk	9335
dairy	gourmet cheese	8353
dairy	dy milk	46107
dairy	chilled spreads	13225
dairy	cheese dairy	24851
discounts & coupons	select ctomr discnt	48
discounts & coupons	dummy do not touch	23
discounts & coupons	Supermarket mcard disc	41
discounts & coupons	Supermarket insurance disc	170
discounts & coupons	Supermarket finsvc \$10 off	9293
discounts & coupons	ancil services	10929
events	seasonal events	1479
events	party goods	1637
events	events	1479

parent category (domain)	subcategory	number of records in subcategory
events	easter	3222
events	christmas gen merch	11
fish, meat, poultry & eggs	smallgoods dairy	12177
fish, meat, poultry & eggs	smallgoods	5880
fish, meat, poultry & eggs	sliced meats	14091
fish, meat, poultry & eggs	seafood (mt)	2134
fish, meat, poultry & eggs	seafood (dl)	4896
fish, meat, poultry & eggs	sausages	9980
fish, meat, poultry & eggs	poultry-frozen	53
fish, meat, poultry & eggs	poultry (mt)	18592
fish, meat, poultry & eggs	poultry (dl)	4575
fish, meat, poultry & eggs	pork	4983
fish, meat, poultry & eggs	lamb	6927
fish, meat, poultry & eggs	hams/bacon	771
fish, meat, poultry & eggs	game	462
fish, meat, poultry & eggs	frozen meat	4
fish, meat, poultry & eggs	fish - dairy	2212
fish, meat, poultry & eggs	eggs	13810
fish, meat, poultry & eggs	continental	5438
fish, meat, poultry & eggs	canned fish	15551
fish, meat, poultry & eggs	beef	20583
fish, meat, poultry & eggs	bbq	5889
fruit & vegetables	soft vegetables	111485
fruit & vegetables	organic fruit & veg	1013
fruit & vegetables	hard veg & mushroom	62138
fruit & vegetables	garden greens	1
fruit & vegetables	fruit-shelf stable	6110
fruit & vegetables	fruit snacks	43198
fruit & vegetables	fruit desserts	70676
fruit & vegetables	frozen vegetables	14419
gifts	gift cards	518
gifts	floral	1487
gifts	christmas gr non fd	576
gifts	cards/wraps	3108
gifts	3rd party giftcard	627
health	vitamins	2165
health	sanitary protection	5837
health	medicinal products	8036
health	infant personal	3172
health	infant nappies	2839

parent category (domain)	subcategory	number of records in subcategory
health	first aid	48
health	dental health	9780
home cleaning	toilet paper	8736
home cleaning	paper towels	4394
home cleaning	laundry accessories	5373
home cleaning	laundry	4545
home cleaning	household gloves	967
home cleaning	dishwashing	6333
home cleaning	cleaning goods	13062
home cleaning	brushware	1020
home cleaning	aircare & disinfect	3009
home indoor	stationery	2614
home indoor	shopping bags	849
home indoor	shoe care	922
home indoor	photographics	62
home indoor	nursery	7
home indoor	kitchenware	4810
home indoor	kitchen needs/bags	10317
home indoor	household appliances	142
home indoor	homewares	1304
home indoor	home textiles	385
home indoor	home organisation	55
home indoor	heating & cooling	82
home indoor	hardware	658
home indoor	electrical	2734
home indoor	audio / video	160
home outdoor	pool and outdoor acc	40
home outdoor	picnic pool bbq acc	1321
home outdoor	outdoor living	12
home outdoor	leisure	271
home outdoor	garden non greens	700
home outdoor	disposable tableware	4166
home outdoor	auto	311
international food	mexican foods	7011
international food	international foods	2540
international food	instant noodles	4339
international food	asian & indian foods	10340
leisure	toys & hobbies	1291
leisure	telco	1016
leisure	prerecorded media	776

parent category (domain)	subcategory	number of records in subcategory
leisure	magazines	7869
leisure	books	771
pets	pet food	25451
pets	pet accessories	746
pets	pest control	1662
pets	fresh pet food	2488
pets	bird food	738
prepared meals & snacks	sushi	166
prepared meals & snacks	soup	8364
prepared meals & snacks	snacks	38451
prepared meals & snacks	salads	1606
prepared meals & snacks	salad bar	19
prepared meals & snacks	protein & meals	2479
prepared meals & snacks	prepared foods	6
prepared meals & snacks	packaged salads	27877
prepared meals & snacks	nuts/dried	9142
prepared meals & snacks	nutritional snacks	12093
prepared meals & snacks	meals	12809
prepared meals & snacks	local foods	281
prepared meals & snacks	instore pseudo brand	2
prepared meals & snacks	infant food/formula	6237
prepared meals & snacks	hmr	371
prepared meals & snacks	heat & eat frozen	10533
prepared meals & snacks	healthfoods	1288
prepared meals & snacks	health foods	15613
prepared meals & snacks	grab & go	724
prepared meals & snacks	frozen snacks	1505
prepared meals & snacks	entertainment	11761
prepared meals & snacks	dried fruit/nuts	6905
prepared meals & snacks	dl prepared foods	709
prepared meals & snacks	dl hot pies & foods	97
prepared meals & snacks	convenience meals	2435
prepared meals & snacks	convenience frozen	12357
prepared meals & snacks	christmas gr food	1818
prepared meals & snacks	cereal	21100
prepared meals & snacks	biscuits & cookies	49462
prepared meals & snacks	bars gum pocket pack	21212
soft drinks, tea & coffee	tea	5664
soft drinks, tea & coffee	still water	8545
soft drinks, tea & coffee	softdrinks	38018

parent category (domain)	subcategory	number of records in subcategory
soft drinks, tea & coffee	non alco wine & hbrw	510
soft drinks, tea & coffee	milk additives	2238
soft drinks, tea & coffee	juices/drinks	9608
soft drinks, tea & coffee	juices & cordials	6589
soft drinks, tea & coffee	juices	11155
soft drinks, tea & coffee	instore cafe	265
soft drinks, tea & coffee	energy/sport/icedtea	9004
soft drinks, tea & coffee	cordial	1699
soft drinks, tea & coffee	coffee	5654
sweets	spreads	9258
sweets	patisserie	130
sweets	instore cake	11276
sweets	ice cream	17393
sweets	frozen desserts	1381
sweets	desserts (gr)	5285
sweets	desserts	5683
sweets	confectionery	34541
sweets	christmas confect	87
sweets	chilled desserts	47169
sweets	brought in seasonal	1293
sweets	boxed chocolates	3870
sweets	baking mixes	3021
sweets	bakery snacks	5854
sweets	bakery packaged cake	6668
sweets	bake instore seasonl	1680

A.2 DOMAIN PAIR STATISTICS FOR THE SUPERMARKET DATASET

Table 37: Domain and domain-pair data size statistics for the supermarket dataset

bread	canned & pickled	1434	608	929	0.0290	0.0179	2.3586	1.5436	0.6545	1.6200
bread	dairy	1498	612	1149	0.0278	0.0209	2.4477	1.3037	0.5326	1.3325
bread	events	991	588	859	0.0344	0.0064	1.6854	1.1537	0.6845	5.4176
bread	fruit & vegetables	1504	612	980	0.0277	0.0642	2.4575	1.5347	0.6245	0.4323
bread	gifts	1111	594	573	0.0325	0.0083	1.8704	1.9389	1.0366	3.9188
bread	home cleaning	1437	612	1123	0.0287	0.0185	2.3480	1.2796	0.5450	1.5541
bread	home outdoor	1096	597	518	0.0328	0.0098	1.8358	2.1158	1.1525	3.3378
bread	international food	1342	610	1184	0.0299	0.0095	2.2000	1.1334	0.5152	3.1548
canned & pickled	bread	1434	929	608	0.0179	0.0290	1.5436	2.3586	1.5280	0.6173
canned & pickled	dairy	1440	929	1147	0.0179	0.0216	1.5501	1.2554	0.8099	0.8259
canned & pickled	events	973	921	859	0.0210	0.0064	1.0565	1.1327	1.0722	3.2627
canned & pickled	fruit & vegetables	1446	929	980	0.0178	0.0664	1.5565	1.4755	0.9480	0.2680
canned & pickled	gifts	1089	919	571	0.0204	0.0084	1.1850	1.9072	1.6095	2.4290
canned & pickled	home cleaning	1397	929	1123	0.0182	0.0189	1.5038	1.2440	0.8272	0.9641
canned & pickled	home outdoor	1071	927	516	0.0203	0.0100	1.1553	2.0756	1.7965	2.0333
canned & pickled	international food	1319	928	1182	0.0190	0.0096	1.4213	1.1159	0.7851	1.9723
dairy	bread	1498	1149	612	0.0209	0.0278	1.3037	2.4477	1.8775	0.7505
dairy	canned & pickled	1440	1147	929	0.0216	0.0179	1.2554	1.5501	1.2347	1.2108
dairy	fruit & vegetables	1520	1150	980	0.0207	0.0637	1.3217	1.5510	1.1735	0.3241
dairy	home cleaning	1448	1147	1123	0.0215	0.0184	1.2624	1.2894	1.0214	1.1688
dairy	international food	1351	1144	1184	0.0224	0.0094	1.1809	1.1410	0.9662	2.3796
events	bread	991	859	588	0.0064	0.0344	1.1537	1.6854	1.4609	0.1846
events	canned & pickled	973	859	921	0.0064	0.0210	1.1327	1.0565	0.9327	0.3065
events	fruit & vegetables	997	859	973	0.0063	0.0747	1.1607	1.0247	0.8828	0.0848
fruit & vegetables	bread	1504	980	612	0.0642	0.0277	1.5347	2.4575	1.6013	2.3131
fruit & vegetables	canned & pickled	1446	980	929	0.0664	0.0178	1.4755	1.5565	1.0549	3.7320
fruit & vegetables	dairy	1520	980	1150	0.0637	0.0207	1.5510	1.3217	0.8522	3.0857
fruit & vegetables	events	997	973	859	0.0747	0.0063	1.0247	1.1607	1.1327	11.7895
fruit & vegetables	gifts	1117	973	573	0.0734	0.0083	1.1480	1.9494	1.6981	8.8739
fruit & vegetables	home cleaning	1452	979	1123	0.0661	0.0183	1.4831	1.2930	0.8718	3.6005
fruit & vegetables	home outdoor	1097	978	518	0.0734	0.0098	1.1217	2.1178	1.8880	7.4688
fruit & vegetables	international food	1353	980	1185	0.0688	0.0094	1.3806	1.1418	0.8270	7.3155
gifts	bread	1111	573	594	0.0083	0.0325	1.9389	1.8704	0.9646	0.2552
gifts	canned & pickled	1089	571	919	0.0084	0.0204	1.9072	1.1850	0.6213	0.4117
gifts	fruit & vegetables	1117	573	973	0.0083	0.0734	1.9494	1.1480	0.5889	0.1127
gifts	home outdoor	902	547	502	0.0093	0.0108	1.6490	1.7968	1.0896	0.8622
home cleaning	bread	1437	1123	612	0.0185	0.0287	1.2796	2.3480	1.8350	0.6435

Domain and domain-pair data size statistics for the supermarket dataset contd.

source	target	user size	source item size	target item size	source density	target density	user to source item ratio	user to target item ratio	source to target item ratio	source to target density ratio
home cleaning	canned & pickled	1397	1123	929	0.0189	0.0182	1.2440	1.5038	1.2088	1.0372
home cleaning	dairy	1448	1123	1147	0.0184	0.0215	1.2894	1.2624	0.9791	0.8556
home cleaning	fruit & vegetables	1452	1123	979	0.0183	0.0661	1.2930	1.4831	1.1471	0.2777
home cleaning	international food	1312	1123	1184	0.0196	0.0096	1.1683	1.1081	0.9485	2.0329
home outdoor	bread	1096	518	597	0.0098	0.0328	2.1158	1.8358	0.8677	0.2996
home outdoor	canned & pickled	1071	516	927	0.0100	0.0203	2.0756	1.1553	0.5566	0.4918
home outdoor	fruit & vegetables	1097	518	978	0.0098	0.0734	2.1178	1.1217	0.5297	0.1339
home outdoor	gifts	902	502	547	0.0108	0.0093	1.7968	1.6490	0.9177	1.1599
international food	bread	1342	1184	610	0.0095	0.0299	1.1334	2.2000	1.9410	0.3170
international food	canned & pickled	1319	1182	928	0.0096	0.0190	1.1159	1.4213	1.2737	0.5070
international food	dairy	1351	1184	1144	0.0094	0.0224	1.1410	1.1809	1.0350	0.4202
international food	fruit & vegetables	1353	1185	980	0.0094	0.0688	1.1418	1.3806	1.2092	0.1367
international food	home cleaning	1312	1184	1123	0.0096	0.0196	1.1081	1.1683	1.0543	0.4919

 ${\it Table~38:~Each~domain~ratings' central~tendency~and~dispersion~statistics~for~the~supermarket~dataset}$

bread	canned & pickled	4.6617	3.8064	3.5065	2.9594	1.6692	2.0968	23.7129	9.2576
bread	dairy	4.6474	5.8235	3.4930	3.7863	1.6763	2.0883	23.5075	53.1673
bread	events	4.8059	2.3285	3.6030	1.9607	2.0971	1.8357	25.9102	1.9093
bread	fruit & vegetables	4.6458	6.4902	3.4917	4.5464	1.6771	15.0120	23.4881	46.3169
bread	gifts	4.7498	2.3800	3.5572	2.0322	2.1251	1.8100	25.1426	7.8743
bread	home cleaning	4.6724	3.1655	3.5130	2.5181	1.6638	1.4172	23.7344	4.8737
bread	home outdoor	4.7619	2.4366	3.5803	2.0544	1.6190	1.7817	25.1580	1.9147
bread	international food	4.6774	3.2257	3.5126	2.6125	2.1613	1.3871	23.9487	5.0982
canned & pickled	bread	3.8064	4.6617	2.9594	3.5065	2.0968	1.6692	9.2576	23.7129
canned & pickled	dairy	3.8194	5.8468	2.9606	3.7990	2.0903	2.0766	9.5062	53.7226
canned & pickled	events	3.9364	2.3299	3.0366	1.9601	2.0318	1.8351	10.4737	1.9292
canned & pickled	fruit & vegetables	3.8190	6.5327	2.9597	4.5595	2.0905	15.4050	9.5035	47.7325
canned & pickled	gifts	3.8738	2.3657	3.0025	2.0354	2.0631	1.8171	9.7034	7.7832
canned & pickled	home cleaning	3.8307	3.1729	2.9693	2.5244	2.0847	1.4135	9.5770	4.9006
canned & pickled	home outdoor	3.8907	2.4376	3.0096	2.0539	2.0546	1.7812	10.0123	1.9308
canned & pickled	international food	3.8396	3.2289	2.9767	2.6163	2.0802	1.3856	9.5532	5.1027
dairy	bread	5.8235	4.6474	3.7863	3.4930	2.0883	1.6763	53.1673	23.5075
dairy	canned & pickled	5.8468	3.8194	3.7990	2.9606	2.0766	2.0903	53.7226	9.5062
dairy	fruit & vegetables	5.8236	6.5023	3.7873	4.5447	2.0882	15.0480	53.2220	47.1214
dairy	home cleaning	5.8574	3.1666	3.7975	2.5196	2.0713	1.4167	53.9368	4.8671
dairy	international food	5.8727	3.2249	3.7947	2.6111	1.0636	1.3876	54.6240	5.0961
events	bread	2.3285	4.8059	1.9607	3.6030	1.8357	2.0971	1.9093	25.9102
events	canned & pickled	2.3299	3.9364	1.9601	3.0366	1.8351	2.0318	1.9292	10.4737
events	fruit & vegetables	2.3274	6.8562	1.9613	4.7089	1.8363	3.5719	1.9028	55.1503
fruit & vegetables	bread	6.4902	4.6458	4.5464	3.4917	15.0120	1.6771	46.3169	23.4881
fruit & vegetables	canned & pickled	6.5327	3.8190	4.5595	2.9597	15.4050	2.0905	47.7325	9.5035
fruit & vegetables	dairy	6.5023	5.8236	4.5447	3.7873	15.0480	2.0882	47.1214	53.2220
fruit & vegetables	events	6.8562	2.3274	4.7089	1.9613	3.5719	1.8363	55.1503	1.9028
fruit & vegetables	gifts	6.7557	2.3794	4.6663	2.0325	1.6221	1.8103	52.0547	7.8622
fruit & vegetables	home cleaning	6.5364	3.1659	4.5637	2.5186	15.3260	1.4170	47.7540	4.8647
fruit & vegetables	home outdoor	6.7654	2.4358	4.6665	2.0548	2.7840	1.7821	52.8557	1.9126
fruit & vegetables	international food	6.5908	3.2246	4.5828	2.6119	2.1880	1.3877	48.9024	5.0948
gifts	bread	2.3800	4.7498	2.0322	3.5572	1.8100	2.1251	7.8743	25.1426
gifts	canned & pickled	2.3657	3.8738	2.0354	3.0025	1.8171	2.0631	7.7832	9.7034
gifts	fruit & vegetables	2.3794	6.7557	2.0325	4.6663	1.8103	1.6221	7.8622	52.0547
gifts	home outdoor	2.3977	2.4335	2.0234	2.0552	1.8012	1.7832	8.9933	1.8534
home cleaning	bread	3.1655	4.6724	2.5181	3.5130	1.4172	1.6638	4.8737	23.7344
home cleaning	canned & pickled	3.1729	3.8307	2.5244	2.9693	1.4135	2.0847	4.9006	9.5770
home cleaning	dairy	3.1666	5.8574	2.5196	3.7975	1.4167	2.0713	4.8671	53.9368

Each domain ratings' central tendency and dispersion statistics for the supermarket dataset contd.

source	target	source mean rating	target mean rating	source median rating	target median rating	source mode rating	target mode rating	source var. rating	target var. rating
home cleaning	fruit & vegetables	3.1659	6.5364	2.5186	4.5637	1.4170	15.3260	4.8647	47.7540
home cleaning	international food	3.1822	3.2354	2.5298	2.6223	1.4089	1.3823	4.9562	5.1364
home outdoor	bread	2.4366	4.7619	2.0544	3.5803	1.7817	1.6190	1.9147	25.1580
home outdoor	canned & pickled	2.4376	3.8907	2.0539	3.0096	1.7812	2.0546	1.9308	10.0123
home outdoor	fruit & vegetables	2.4358	6.7654	2.0548	4.6665	1.7821	2.7840	1.9126	52.8557
home outdoor	gifts	2.4335	2.3977	2.0552	2.0234	1.7832	1.8012	1.8534	8.9933
international food	bread	3.2257	4.6774	2.6125	3.5126	1.3871	2.1613	5.0982	23.9487
international food	canned & pickled	3.2289	3.8396	2.6163	2.9767	1.3856	2.0802	5.1027	9.5532
international food	dairy	3.2249	5.8727	2.6111	3.7947	1.3876	1.0636	5.0961	54.6240
international food	fruit & vegetables	3.2246	6.5908	2.6119	4.5828	1.3877	2.1880	5.0948	48.9024
international food	home cleaning	3.2354	3.1822	2.6223	2.5298	1.3823	1.4089	5.1364	4.9562

Table 39: Each domain and domain-pair ratings' dispersion statistics for the supermarket dataset

bread dairy 0.0376 2.3587 9.6688 4.7521 32.0583 9.5021 7.9137 6.4620 bread events 1.2489 20.7659 23.6182 68.2540 128.8670 15.309 9.0923 bread fruit & vegetables 0.0920 18.7188 11.907 103.3222 13.1199 558.901 2.0663 55.1349 bread home cleaning 0.0920 18.7188 11.907 103.3222 13.01972 75.6465 78.811 6.813 bread home outdoor 0.6154 17.3761 15.0560 25.0669 13.4117 66.3014 8.0414 9.733 bread international food 0.3854 10.9669 3.0712 151.8759 3.6366 82.763 13.098 5.741 canned & pickled darity 4.082 1.0899 1.8185 2.2828 3.5256 371.0322 4.6630 4.5396 2.4241 canned & pickled demit & vegetables 0.2919 9.8182 2.4052 14										
bread cents 1.2489 20.7659 23.6158 268.2549 128.8670 158.3910 7.8300 92.9263 bread fruit & vegetables 0.6232 18.7729 17.8555 62.3595 134.1996 25.006 51.349 bread home cleaning 0.0920 13.7158 11.1967 103.3821 134.1996 35.901 7.8465 7.8416 5.1349 bread home cutdoor 0.6154 17.3764 15.0650 225.0669 13.4117 166.3014 8.0474 9.7343 bread bread 0.4821 10.806 2.0752 124.986 35.309 13.10856 4.5297 7.8760 canned & pickled bread 1.0102 10.9661 3.9712 181.8759 36.3366 82.735 4.5936 4.5297 7.8780 canned & pickled fruit & vegetables 0.0300 8.8129 5.2049 36.3366 8716.302 4.5129 6.6101 canned & pickled fruit & vegetables 0.0255 1.5459 2.62	bread	canned & pickled	0.7974	20.1432	19.5878	111.7299	131.0856	35.3695	7.8870	4.5297
bread fruit & vegetables 0.6232 18.7729 7.8855 62.3595 13.21253 31.809 7.9163 4.2681 bread gifts 1.9945 20.6689 28.4264 316.3883 13.1196 358.913 ⋅ 8009 5.01349 bread home outdoor 0.6154 13.7188 11.1967 13.3222 130.9721 75.6455 7.8811 6.9184 bread international food 0.3585 15.1734 15.0650 22.0669 3.43117 16.3014 8.0473 8.7830 8.7741 canned & pickled dairy 0.3864 19.9661 3.9712 151.8759 36.366 8.2763 4.5936 6.2644 canned & pickled diffus 0.8801 1.50459 1.84539 2.2373 28.5855 34.2071 156.932 4.533 4.8361 4.5369 4.2661 canned & pickled gifus 1.6880 15.0496 1.84830 35.2556 36.2206 371.6302 4.5781 4.5789 4.6379 4.5789 4.2489 4.2499<	bread	dairy	0.0376	12.3587	9.2668	84.7521	132.0583	89.5021	7.9137	6.4620
bread gifts 1.9945 2.0689 28.4264 316.3881 314.1996 38.901: 8.006 55.1349 bread home cleaning 0.0920 13.7158 11.1967 103.3222 130.9721 75.6465 7.811 6.0813 bread home outdoor 0.1544 17.3764 15.0602 225.0669 134.317 16.0314 8.0474 9.7343 bread home outdoor 0.4832 10.0806 2.0752 182.4966 35.305 13.1056 4.5977 7.8870 canned & pickled dairy 0.3864 1.0960 3.9712 151.8759 36.366 82.763 45.936 6.264 canned & pickled fruit & vegetables 0.0300 8.819 2.2405 47.694 36.306 35.655 4.5938 4.6366 canned & pickled fruit & vegetables 0.5059 8.1282 2.7405 42.5258 35.256 45.912 4.5308 4.5366 canned & pickled home cleaning 0.9152 9.6909 2.6327 <t< td=""><td>bread</td><td>events</td><td>1.2489</td><td>20.7659</td><td>23.6158</td><td>268.2549</td><td>128.8670</td><td>158.3910</td><td>7.8300</td><td>9.9263</td></t<>	bread	events	1.2489	20.7659	23.6158	268.2549	128.8670	158.3910	7.8300	9.9263
bread home cleaning 0.0920 13.7158 11.1967 103.3222 13.0721 75.6465 7.8811 60.813 bread home outdoor 0.6154 17.3764 15.0650 225.0669 134.311 16.63014 8.0474 9.7343 bread international food 0.2358 15.1743 12.9751 134.176 132.0875 64.6583 7.908 5.771 canned & pickled dairy 0.3864 10.9661 3.9712 151.8759 36.3366 82.273 15.9382 4.6830 9.8182 canned & pickled fruit & vegetables 0.0300 8.8319 5.2962 74.7694 36.306 55.2655 4.5938 4.6363 canned & pickled home outdoor 0.8705 13.3895 2.1409 263.271 35.5055 4.5791 6.6101 canned & pickled home outdoor 0.8705 13.3895 2.1409 263.271 35.555 45.591 9.7181 canned & pickled international food 0.1595 18.8501 <td< td=""><td>bread</td><td>fruit & vegetables</td><td>0.6232</td><td>18.7729</td><td>17.8555</td><td>62.3595</td><td>132.1253</td><td>33.1809</td><td>7.9163</td><td>4.2681</td></td<>	bread	fruit & vegetables	0.6232	18.7729	17.8555	62.3595	132.1253	33.1809	7.9163	4.2681
bread home outdoor 0.6154 17.3764 15.0650 225.0669 13.4317 16.3014 8.0474 9.7343 bread international food 0.338 15.1743 12.9371 134.716 132.087 64.4583 7.9308 5.7741 canned & pickled dariny 0.4832 10.896 2.9772 182.4986 33.2051 31.0556 4.5977 7.8870 canned & pickled fruit & vegetables 0.0300 8.819 5.2962 74.7981 36.306 35.2652 4.5938 4.3636 canned & pickled fruit & vegetables 0.0300 8.819 5.2962 74.7981 36.306 35.2652 4.5938 4.3636 canned & pickled fruit & vegetables 0.3291 9.8128 2.7405 147.2051 36.306 35.2555 4.5398 4.3636 canned & pickled fruit method of of openal 0.9129 9.8128 2.7405 147.2051 36.306 8.5121 4.5306 7.7181 canned & pickled international food	bread	gifts	1.9945	20.6689	28.4264	316.3883	134.1996	3589.9013	8.0206	55.1349
bread international food 0.2358 15.1743 12.9731 134.7176 132.2087 64.4583 7.9308 5.7741 canned & pickled dairy 0.4832 10.8096 2.0752 182.4986 35.3695 131.0856 4.5297 7.8870 canned & pickled cents 1.1012 14.5539 2.3273 285.5555 34.2207 150.9432 4.653 9.8811 canned & pickled fruit & vegetables 0.0300 8.8319 5.2662 74.7694 36.3066 35.2655 4.5938 4.5636 canned & pickled fruit & vegetables 0.0300 8.8119 5.2662 74.7694 36.3066 3716.3024 4.5125 56.6101 canned & pickled home outdoor 0.8705 13.3895 2.0149 263.4571 35.5754 165.3755 4.5391 9.7131 canned & pickled international food 0.1529 9.6909 2.6327 156.7528 55.3256 64.5121 4506 7.773 dairy fruit & vegetables 1.52	bread	home cleaning	0.0920	13.7158	11.1967	103.3222	130.9721	75.6465	7.8811	6.0813
canned & pickled bread 0.4832 10.8096 2.0752 182.4986 35.3695 131.0856 4.5297 7.8870 canned & pickled dairy 0.3864 10.9661 3.9712 151.8759 36.3366 88.2763 4.5936 6.4264 canned & pickled fruit & vegetables 0.0300 8.8319 5.2962 74.7694 36.3406 35.2655 4.5934 4.3636 canned & pickled fruit & vegetables 0.0300 8.8319 5.2962 74.7694 36.3406 35.2655 4.5934 4.3636 canned & pickled home cleaning 0.2919 9.8128 2.7405 147.2051 36.0787 75.0585 4.5799 6.0571 canned & pickled international food 0.1529 9.6909 2.6327 156.7528 35.3256 64.5412 4.5006 5.7773 dairy bread 0.5985 18.8501 17.5246 104.971 82.2763 36.3366 6.4261 4.5936 dairy international food 0.1559 <	bread	home outdoor	0.6154	17.3764	15.0650	225.0669	134.3117	166.3014	8.0474	9.7343
canned & pickled dairy 0.3864 10.9661 3.9712 151.8759 36.3366 88.2763 4.5936 6.4264 canned & pickled events 1.1012 14.5539 2.3273 285.8555 34.2207 156.9432 4.653 9.8891 canned & pickled fruit & vegetables 0.0300 8.8319 5.2962 74.7694 36.3406 35.2655 4.5938 4.3636 canned & pickled home cleaning 0.2919 9.8128 2.7405 147.2051 36.9367 75.0585 4.5391 9.0718 canned & pickled home outdoor 0.8705 13.3895 2.0149 263.4571 35.5756 64.5412 4.5306 6.7773 dairy bread 0.0265 11.0937 70.555 90.383 89.021 132.0583 6.4264 4.5936 dairy fruit & vegetables 0.3525 18.5017 15.4814 10.4910 88.2763 35.4211 6.4505 4.3693 dairy fruit & vegetables 0.3625 16.0073	bread	international food	0.2358	15.1743	12.9731	134.7176	132.2087	64.4583	7.9308	5.7741
canned & pickled events 1.1012 14.5539 2.3273 285.8555 34.2207 156.9432 4.4653 9.891 canned & pickled fruit & vegetables 0.0300 8.8319 5.2962 74.7694 36.3406 35.2655 4.5938 4.3636 canned & pickled home cleaning 0.2919 9.8128 2.7405 147.2051 36.0978 75.0585 4.5789 6.0571 canned & pickled home outdoor 0.8705 13.3895 2.0149 263.4571 35.5754 165.3755 4.530 9.7181 canned & pickled international food 0.1529 9.9999 2.6327 156.7528 35.2566 64.5412 4.306 5.7773 dairy bread 0.0265 11.0937 7.9055 99.0383 89.021 132.0583 6.4620 7.9137 dairy brint & vegetables 0.3525 16.0073 14.580 57.1452 89.0897 35.4211 6.4505 4.3636 dairy international food 0.1450 1	canned & pickled	bread	0.4832	10.8096	2.0752	182.4986	35.3695	131.0856	4.5297	7.8870
canned & pickled fruit & vegetables 0.0300 8.8319 5.2962 74.7694 36.3406 35.2655 4.5938 4.3636 canned & pickled gifts 1.6880 15.0459 1.8458 328.3858 35.2596 3716.302 4.5155 56.6101 canned & pickled home cleaning 0.2919 9.8128 2.7405 147.2051 36.0978 75.0585 4.5789 6.0571 canned & pickled home outdoor 0.8705 13.3895 2.0149 263.4571 35.5754 165.3755 4.5306 5.7773 dairy bread 0.05265 11.0937 7.9055 99.0383 85.021 132.0583 6.4620 7.9137 dairy fruit & vegetables 0.3525 16.0073 14.5840 57.1452 80.987 35.211 6.4502 4.5936 dairy international food 0.1450 15.4814 12.9998 131.485 81.809 75.5464 6.410 6.4500 4.3693 dairy international food 0.1450 <td>canned & pickled</td> <td>dairy</td> <td>0.3864</td> <td>10.9661</td> <td>3.9712</td> <td>151.8759</td> <td>36.3366</td> <td>88.2763</td> <td>4.5936</td> <td>6.4264</td>	canned & pickled	dairy	0.3864	10.9661	3.9712	151.8759	36.3366	88.2763	4.5936	6.4264
canned & pickled gifts 1.6880 15.0459 1.8458 328.3858 35.2596 3716.302	canned & pickled	events	1.1012	14.5539	2.3273	285.8555	34.2207	156.9432	4.4653	9.8891
canned & pickled home cleaning 0.2919 9.8128 2.7405 147.2051 36.0785 75.0885 4.5789 6.0571 canned & pickled home outdoor 0.8705 13.3895 2.0149 263.4571 35.5754 165.3755 4.5306 5.7773 dairy bread 0.0265 11.0937 7.9055 99.0883 89.5021 132.0583 6.4204 7.9137 dairy canned & pickled 0.5985 18.8501 17.5346 104.9710 88.2763 36.366 6.4264 4.5936 dairy home cleaning 0.0469 13.3472 10.9040 100.6738 87.832 75.5464 6.4103 6.0762 dairy international food 0.1450 15.4814 12.9998 131.4885 8.81089 64.4671 6.4261 5.7740 events bread 0.1598 8.3681 4.8108 99.3721 158.3910 182.8670 9.9891 4.4653 fruit & vegetables bread 0.7511 7.6313 5.2695 <td>canned & pickled</td> <td>fruit & vegetables</td> <td>0.0300</td> <td>8.8319</td> <td>5.2962</td> <td>74.7694</td> <td>36.3406</td> <td>35.2655</td> <td>4.5938</td> <td>4.3636</td>	canned & pickled	fruit & vegetables	0.0300	8.8319	5.2962	74.7694	36.3406	35.2655	4.5938	4.3636
canned & pickledhome outdoor0.870513.38952.0149263.457135.5754165.37554.53919.7181canned & pickledinternational food0.15299.69092.6327156.752835.325664.54124.53065.7773dairybread0.026511.09377.905599.038389.5021132.05836.46207.9137dairycanned & pickled0.598518.850117.5346104.971088.276336.33666.42644.5936dairyhome cleaning0.046913.347210.9040100.673887.883275.54646.41036.0762dairyinternational food0.145015.481412.9998131.488588.108964.46716.42615.7740eventsbread0.10598.36814.810899.3721158.3910128.86709.92637.8300eventsfruit & vegetables0.719117.252516.003379.5281158.885034.13319.94224.3249fruit & vegetablesbread0.586812.36448.6807141.414733.1809132.12534.26817.9163fruit & vegetablescanned & pickled0.07517.63135.269558.394035.265536.34064.36364.5938fruit & vegetablesdairy0.361310.80537.0845100.690735.71189.08774.36936.4565fruit & vegetablespinternational food1.765022.927126.6697243.9	canned & pickled	gifts	1.6880	15.0459	1.8458	328.3858	35.2596	3716.3020	4.5125	56.6101
canned & pickled international food 0.1529 9.6909 2.6327 156.7528 35.356 64.5412 4.5306 5.7773 dairy bread 0.0265 11.0937 7.9055 99.0383 89.5021 132.0583 6.4620 7.9137 dairy canned & pickled 0.5985 18.8501 17.5346 104.9710 88.2763 36.3366 6.4264 4.5936 dairy home cleaning 0.0469 13.3472 10.9040 100.6738 87.8832 75.5464 6.4103 6.0762 dairy international food 0.1450 15.4814 12.9998 131.4885 88.1089 64.4671 6.4261 5.7740 devents bread 0.1059 8.3681 4.8108 99.3721 158.3910 128.8670 9.9263 7.8300 events fruit & vegetables 0.7191 17.2525 16.0033 79.5281 158.890 34.1331 9.9422 4.2349 fruit & vegetables bread 0.5868 12.364 8.6807 </td <td>canned & pickled</td> <td>home cleaning</td> <td>0.2919</td> <td>9.8128</td> <td>2.7405</td> <td>147.2051</td> <td>36.0978</td> <td>75.0585</td> <td>4.5789</td> <td>6.0571</td>	canned & pickled	home cleaning	0.2919	9.8128	2.7405	147.2051	36.0978	75.0585	4.5789	6.0571
dairy bread 0.0265 11.0937 7.9055 99.0383 89.5021 132.0583 6.4620 7.9137 dairy canned & pickled 0.5985 18.8501 17.5346 104.9710 88.2763 36.3366 6.4264 4.5936 dairy home cleaning 0.0469 13.3472 10.9040 100.6738 87.8832 75.5464 6.4103 6.0762 dairy international food 0.1450 15.4814 12.9998 131.4885 88.1089 64.4671 6.4261 5.7740 events bread 0.1059 8.3681 4.8108 99.3721 158.3910 128.86670 9.9263 7.8300 events fruit & vegetables 0.7191 17.2525 16.0033 79.5281 158.8910 32.1253 4.2681 7.9163 fruit & vegetables bread 0.5868 12.3644 8.6807 141.4147 33.1809 132.1253 4.2681 7.9163 fruit & vegetables dairy 0.3613 10.8053 7.0845	canned & pickled	home outdoor	0.8705	13.3895	2.0149	263.4571	35.5754	165.3755	4.5391	9.7181
$\begin{array}{llllllllllllllllllllllllllllllllllll$	canned & pickled	international food	0.1529	9.6909	2.6327	156.7528	35.3256	64.5412	4.5306	5.7773
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	dairy	bread	0.0265	11.0937	7.9055	99.0383	89.5021	132.0583	6.4620	7.9137
$\begin{array}{c} \text{dairy} & \text{home cleaning} \\ \text{dairy} & \text{international food} \\ \text{dairy} & \text{international food} \\ \text{ol.}1450 & 15.4814 & 12.9998 & 131.4885 & 88.1089 & 64.4671 & 6.4261 & 5.7740 \\ \text{events} & \text{bread} & 0.1059 & 8.3681 & 4.8108 & 99.3721 & 158.3910 & 128.8670 & 9.9263 & 7.8300 \\ \text{events} & \text{canned \& pickled} & 1.1206 & 20.0165 & 19.9476 & 134.6140 & 156.9432 & 34.2207 & 9.8891 & 4.4653 \\ \text{events} & \text{fruit \& vegetables} & 0.7191 & 17.2525 & 16.0033 & 79.5281 & 158.8850 & 34.1331 & 9.9422 & 4.3249 \\ \text{fruit \& vegetables} & \text{bread} & 0.5868 & 12.3644 & 8.6807 & 141.4147 & 33.1809 & 132.1253 & 4.2681 & 7.9163 \\ \text{fruit \& vegetables} & \text{canned \& pickled} & 0.0751 & 7.6313 & 5.2695 & 58.3940 & 35.2655 & 36.3406 & 4.3636 & 4.5938 \\ \text{fruit \& vegetables} & \text{canned \& pickled} & 0.0751 & 7.6313 & 5.2695 & 58.3940 & 35.2655 & 36.3406 & 4.3636 & 4.5938 \\ \text{fruit \& vegetables} & \text{canned \& pickled} & 0.0751 & 7.6313 & 5.2695 & 58.3940 & 35.2655 & 36.3406 & 4.3636 & 4.5938 \\ \text{fruit \& vegetables} & \text{cents} & 2.6268 & 26.9012 & 35.3657 & 253.7048 & 34.1331 & 158.8850 & 4.3249 & 9.9422 \\ \text{fruit \& vegetables} & \text{gifts} & 4.1216 & 31.2020 & 40.0139 & 235.7818 & 32.1221 & 3595.5916 & 4.2237 & 55.1795 \\ \text{fruit \& vegetables} & \text{home cleaning} & 0.2820 & 11.1499 & 7.2162 & 112.2010 & 35.1904 & 75.5778 & 4.3581 & 6.0774 \\ \text{fruit \& vegetables} & \text{home outdoor} & 1.7650 & 22.9271 & 26.6697 & 243.9330 & 34.0048 & 166.4065 & 4.3028 & 9.7366 \\ \text{fruit \& vegetables} & \text{home outdoor} & 1.7650 & 22.9271 & 26.6697 & 243.9330 & 34.0048 & 166.4065 & 4.3028 & 9.7366 \\ \text{fruit \& vegetables} & \text{home outdoor} & 1.7650 & 29.9687 & 33.1800 & 62.1844 & 3589.9015 & 134.1996 & 55.1349 & 8.0206 \\ \text{gifts} & \text{bread} & 5.8374 & 29.6087 & 33.1800 & 62.1844 & 3589.9015 & 134.1996 & 55.1349 & 8.0206 \\ \text{gifts} & \text{canned \& pickled} & 19.3257 & 33.4576 & 34.8906 & 21.6889 & 3716.302 & 35.2596 & 56.6101 & 4.5125 \\ \text{gifts} & \text{home outdoor} & 4.2716 & 17.4545 & 16.8812 & 204.3875 & 3165.0375 & 19.9875 & 51.9084 & 10.4563 \\ home clean$	dairy	canned & pickled	0.5985	18.8501	17.5346	104.9710	88.2763	36.3366	6.4264	4.5936
dairyinternational food 0.1450 15.4814 12.9998 131.4885 88.1089 64.4671 6.4261 5.7740 eventsbread 0.1059 8.3681 4.8108 99.3721 158.3910 128.8670 9.9263 7.8300 eventscanned & pickled 1.1206 20.0165 19.9476 134.6140 156.9432 34.2207 9.8891 4.4653 eventsfruit & vegetables 0.7191 17.2525 16.0033 79.5281 158.8850 34.1331 9.9422 4.3249 fruit & vegetablesbread 0.5868 12.3644 8.6807 141.4147 33.1809 132.1253 4.2681 7.9163 fruit & vegetablescanned & pickled 0.0751 7.6313 5.2695 58.3940 35.2655 36.3406 4.3636 4.5938 fruit & vegetablesdairy 0.3613 10.8053 7.0845 100.6907 35.4211 89.0897 4.3693 6.4505 fruit & vegetablesgifts 4.1216 31.2020 40.0139 235.7818 32.1221 3595.5916 4.2237 55.1795 fruit & vegetableshome cleaning 0.2820 11.1499 7.2162 112.2010 35.1904 75.5778 4.3581 6.0774 fruit & vegetablesinternational food 0.1753 10.5574 6.2214 123.0611 34.9631 64.4866 4.3482 5.7749 giftsbread 5.8374 29.6087 33.1800 21.6889 </td <td>dairy</td> <td>fruit & vegetables</td> <td>0.3525</td> <td>16.0073</td> <td>14.5840</td> <td>57.1452</td> <td>89.0897</td> <td>35.4211</td> <td>6.4505</td> <td>4.3693</td>	dairy	fruit & vegetables	0.3525	16.0073	14.5840	57.1452	89.0897	35.4211	6.4505	4.3693
bread 0.1059 8.3681 4.8108 99.3721 158.3910 128.8670 9.9263 7.8300 events canned & pickled 1.1206 20.0165 19.9476 134.6140 156.9432 34.2207 9.8891 4.4653 events fruit & vegetables 0.7191 17.2525 16.0033 79.5281 158.8850 34.1331 9.9422 4.3249 fruit & vegetables bread 0.5868 12.3644 8.6807 141.4147 33.1809 132.1253 4.2681 7.9163 fruit & vegetables canned & pickled 0.0751 7.6313 5.2695 58.3940 35.2655 36.3406 4.3636 4.5938 fruit & vegetables dairy 0.3613 10.8053 7.0845 100.6907 35.4211 89.0897 4.3693 6.4505 fruit & vegetables events 2.6268 26.9012 35.3657 253.7048 34.1331 158.8850 4.3249 9.9422 fruit & vegetables gifts 4.1216 31.2020 40.0139 235.7818 32.1221 3595.5916 4.2237 55.1795 fruit & vegetables home cleaning 0.2820 11.1499 7.2162 112.2010 35.1904 75.5778 4.3581 6.0774 fruit & vegetables international food 0.1753 10.5574 6.2214 123.0611 34.9631 64.4866 4.3482 5.7749 gifts bread 5.8374 29.6087 33.1800 62.1844 3589.9013 134.1996 55.1349 8.0206 gifts canned & pickled 19.3257 33.4576 34.8906 21.6889 3716.3023 35.2596 56.6101 4.5125 gifts home outdoor 4.2716 17.4545 16.8812 204.3875 3165.0375 191.9873 51.9084 10.4563 home cleaning bread 0.0455 5.6154 1.3333 82.6786 75.6465 130.9721 6.0813 7.8811 home cleaning canned & pickled 0.3607 10.8696 7.6347 102.5252 75.0585 36.0978 6.0571 4.5789	dairy	home cleaning	0.0469	13.3472	10.9040	100.6738	87.8832	75.5464	6.4103	6.0762
events canned & pickled 1.1206 20.0165 19.9476 134.6140 156.9432 34.2207 9.8891 4.4653 events fruit & vegetables 0.7191 17.2525 16.0033 79.5281 158.8850 34.1331 9.9422 4.3249 fruit & vegetables bread 0.5868 12.3644 8.6807 141.4147 33.1809 132.1253 4.2681 7.9163 fruit & vegetables canned & pickled 0.0751 7.6313 5.2695 58.3940 35.2655 36.3406 4.3636 4.5938 fruit & vegetables dairy 0.3613 10.8053 7.0845 100.6907 35.4211 89.0897 4.3693 6.4505 fruit & vegetables events 2.6268 26.9012 35.3657 253.7048 34.1331 158.8850 4.3249 9.9422 fruit & vegetables gifts 4.1216 31.2020 40.0139 235.7818 32.1221 3595.591 4.2237 55.1795 fruit & vegetables home cleaning 0.2820 11.1499 7.2162 112.2010 35.1904 75.5778 4.3581 6.0774 6.2214 6.	dairy	international food	0.1450	15.4814	12.9998	131.4885	88.1089	64.4671	6.4261	5.7740
fruit & vegetables bread 0.5868 12.3644 8.6807 141.4147 33.1809 132.1253 4.2681 7.9163 fruit & vegetables canned & pickled 0.0751 7.6313 5.2695 58.3940 35.2655 36.3406 4.3636 4.5938 fruit & vegetables dairy 0.3613 10.8053 7.0845 100.6907 35.4211 89.0897 4.3693 6.4505 fruit & vegetables events 2.6268 26.9012 35.3657 253.7048 34.1331 158.8850 4.3249 9.9422 fruit & vegetables gifts 4.1216 31.2020 40.0139 235.7818 32.1221 3595.5916 4.2237 55.1795 fruit & vegetables home cleaning 0.2820 11.1499 7.2162 112.2010 35.1904 75.5778 4.3581 6.0774 fruit & vegetables international food 0.1753 10.5574 6.2214 123.0611 34.9631 64.4866 4.3482 5.7749 gifts bread 5.8374 29.6087 33.1800 62.1844 3589.9013 134.1996 55.1349 8.0206 gifts canned & pickled 19.3257 33.4576 34.8906 21.6889 3716.3020 35.2596 56.6101 4.5125 gifts home outdoor 4.2716 17.4545 16.8812 204.3875 3165.0378 191.9873 51.9084 10.4563 home cleaning bread 0.0455 5.6154 1.3333 82.6786 75.6465 130.9721 6.0813 7.8811 home cleaning canned & pickled 0.3607 10.8696 7.6347 102.5252 75.0585 36.0978 6.0571 4.5789	events	bread	0.1059	8.3681	4.8108	99.3721	158.3910	128.8670	9.9263	7.8300
fruit & vegetables bread 0.5868 12.3644 8.6807 141.4147 33.1809 132.1253 4.2681 7.9163 fruit & vegetables canned & pickled 0.0751 7.6313 5.2695 58.3940 35.2655 36.3406 4.3636 4.5938 fruit & vegetables dairy 0.3613 10.8053 7.0845 100.6907 35.4211 89.0897 4.3693 6.4505 fruit & vegetables events 2.6268 26.9012 35.3657 253.7048 34.1331 158.8850 4.3249 9.9422 fruit & vegetables gifts 4.1216 31.2020 40.0139 235.7818 32.1221 $3595.5916 4.2237$ 55.1795 fruit & vegetables home cleaning 0.2820 11.1499 7.2162 112.2010 35.1904 75.5778 4.3581 6.0774 fruit & vegetables international food 0.1753 10.5574 6.2214 123.0611 34.9631 64.4866 4.3482 5.7749 gifts bread 5.8374 29.6087 33.1800 62.1844 3589.9013 134.1996 55.1349 8.0206 gifts canned & pickled 19.3257 33.4576 34.8906 21.6889 3716.302 35.2596 56.6101 4.5125 gifts home outdoor 4.2716 17.4545 16.8812 204.3875 3165.0375 191.9873 51.9084 10.4563 home cleaning bread 0.0455 5.6154 1.3333 82.6786 75.6465 130.9721 6.0813 7.8811 home cleaning canned & pickled 0.3607 10.8696 7.6347 102.5252 75.0585 36.0978 6.0571 4.5789	events	canned & pickled	1.1206	20.0165	19.9476	134.6140	156.9432	34.2207	9.8891	4.4653
fruit & vegetables canned & pickled 0.0751 7.6313 5.2695 58.3940 35.2655 36.3406 4.3636 4.5938 fruit & vegetables dairy 0.3613 10.8053 7.0845 100.6907 35.4211 89.0897 4.3693 6.4505 fruit & vegetables events 2.6268 26.9012 35.3657 253.7048 34.1331 158.8850 4.3249 9.9422 fruit & vegetables gifts 4.1216 31.2020 40.0139 235.7818 32.1221 3595.5916 4.2237 55.1795 fruit & vegetables home cleaning 0.2820 11.1499 7.2162 112.2010 35.1904 75.5778 4.3581 6.0774 fruit & vegetables home outdoor 1.7650 22.9271 26.6697 243.9330 34.0048 166.4065 4.3028 9.7366 fruit & vegetables international food 0.1753 10.5574 6.2214 123.0611 34.9631 64.4866 4.3482 5.7749 gifts bread 5.8374 29.6087 33.1800 62.1844 3589.9013 134.1996 55.1349 8.0206 gifts canned & pickled 19.3257 33.4576 34.8906 21.6889 3716.302(35.2596 56.6101 4.5125 gifts home outdoor 4.2716 17.4545 16.8812 204.3875 3165.037£ 191.9873 51.9084 10.4563 home cleaning bread 0.0455 5.6154 1.3333 82.6786 75.6465 130.9721 6.0813 7.8811 home cleaning canned & pickled 0.3607 10.8696 7.6347 102.5252 75.0585 36.0978 6.0571 4.5789	events	fruit & vegetables	0.7191	17.2525	16.0033	79.5281	158.8850	34.1331	9.9422	4.3249
fruit & vegetables events 2.6268 26.9012 35.3657 253.7048 34.1331 158.8850 4.3249 9.9422 fruit & vegetables gifts 4.1216 31.2020 40.0139 235.7818 32.1221 $3595.591 4.2237$ 55.1795 fruit & vegetables home cleaning 0.2820 11.1499 7.2162 112.2010 35.1904 75.5778 4.3581 6.0774 fruit & vegetables home outdoor 1.7650 22.9271 26.6697 243.9330 34.0048 166.4065 4.3028 9.7366 fruit & vegetables international food 0.1753 10.5574 6.2214 123.0611 34.9631 64.4866 4.3482 5.7749 gifts bread 5.8374 29.6087 33.1800 62.1844 3589.9013 134.1996 55.1349 8.0206 gifts canned & pickled 19.3257 33.4576 34.8906 21.6889 3716.302 35.2596 56.6101 4.5125 gifts home outdoor 4.2716 17.4545 16.8812 204.3875 3165.0375 191.9873 51.9084 10.4563 home cleaning bread 0.0455 5.6154 1.3333 82.6786 75.6465 130.9721 6.0813 7.8811 home cleaning canned & pickled 0.3607 10.8696 7.6347 102.5252 75.0585 36.0978 6.0571 4.5789	fruit & vegetables	bread	0.5868	12.3644	8.6807	141.4147	33.1809	132.1253	4.2681	7.9163
fruit & vegetables events 2.6268 26.9012 35.3657 253.7048 34.1331 158.8850 4.3249 9.9422 fruit & vegetables gifts 4.1216 31.2020 40.0139 235.7818 32.1221 3595.591€ 4.2237 55.1795 fruit & vegetables home cleaning 0.2820 11.1499 7.2162 112.2010 35.1904 75.5778 4.3581 6.0774 fruit & vegetables home outdoor 1.7650 22.9271 26.6697 243.9330 34.0048 166.4065 4.3028 9.7366 fruit & vegetables international food 0.1753 10.5574 6.2214 123.0611 34.9631 64.4866 4.3482 5.7749 gifts bread 5.8374 29.6087 33.1800 62.1844 3589.9013 134.1996 55.1349 8.0206 gifts canned & pickled 19.3257 33.4576 34.8906 21.6889 3716.302€ 35.2596 56.6101 4.5125 gifts fruit & vegetables 16.5496 33.6290 34.3409 7.3027 3595.591€ 32.1221 55.1795 4.2237 gifts home outdoor 4.2716 17.4545 16.8812 204.3875 3165.0375 191.9873 51.9084 10.4563 home cleaning bread 0.0455 5.6154 1.3333 82.6786 75.6465 130.9721 6.0813 7.8811 home cleaning canned & pickled 0.3607 10.8696 7.6347 102.5252 75.0585 36.0978 6.0571 4.5789	fruit & vegetables	canned & pickled	0.0751	7.6313	5.2695	58.3940	35.2655	36.3406	4.3636	4.5938
fruit & vegetables gifts	fruit & vegetables	dairy	0.3613	10.8053	7.0845	100.6907	35.4211	89.0897	4.3693	6.4505
fruit & vegetables home cleaning 0.2820 11.1499 7.2162 112.2010 35.1904 75.5778 4.3581 6.0774 fruit & vegetables home outdoor 1.7650 22.9271 26.6697 243.9330 34.0048 166.4065 4.3028 9.7366 fruit & vegetables international food 0.1753 10.5574 6.2214 123.0611 34.9631 64.4866 4.3482 5.7749 gifts bread 5.8374 29.6087 33.1800 62.1844 3589.9013 134.1996 55.1349 8.0206 gifts canned & pickled 19.3257 33.4576 34.8906 21.6889 3716.302 C 35.2596 56.6101 4.5125 gifts fruit & vegetables 16.5496 33.6290 34.3409 7.3027 3595.591 C 32.1221 55.1795 4.2237 home outdoor 4.2716 17.4545 16.8812 204.3875 3165.037 E 191.9873 51.9084 10.4563 home cleaning bread 0.0455 5.6154 1.3333 82.6786 75.6465 130.9721 6.0813 7.8811 home cleaning canned & pickled 0.3607 10.8696 7.6347 102.5252 75.0585 36.0978 6.0571 4.5789	fruit & vegetables	events	2.6268	26.9012	35.3657	253.7048	34.1331	158.8850	4.3249	9.9422
fruit & vegetables home outdoor 1.7650 22.9271 26.6697 243.9330 34.0048 166.4065 4.3028 9.7366 fruit & vegetables international food 0.1753 10.5574 6.2214 123.0611 34.9631 64.4866 4.3482 5.7749 gifts bread 5.8374 29.6087 33.1800 62.1844 $3589.9015134.1996$ 55.1349 8.0206 gifts canned & pickled 19.3257 33.4576 34.8906 21.6889 3716.302×35.2596 56.6101 4.5125 gifts fruit & vegetables 16.5496 33.6290 34.3409 7.3027 $3595.591632.1221$ 55.1795 4.2237 gifts home outdoor 4.2716 17.4545 16.8812 204.3875 3165.0375191.9873 51.9084 10.4563 home cleaning bread 0.0455 5.6154 1.3333 82.6786 75.6465 130.9721 6.0813 7.8811 home cleaning canned & pickled 0.3607 10.8696 7.6347 102.5252 75.0585 36.0978 6.0571 4.5789	fruit & vegetables	gifts	4.1216	31.2020	40.0139	235.7818	32.1221	3595.5910	4.2237	55.1795
fruit & vegetables international food 0.1753 10.5574 6.2214 123.0611 34.9631 64.4866 4.3482 5.7749 gifts bread 5.8374 29.6087 33.1800 62.1844 3589.9013 134.1996 55.1349 8.0206 gifts canned & pickled 19.3257 33.4576 34.8906 21.6889 3716.302 35.2596 56.6101 4.5125 gifts fruit & vegetables 16.5496 33.6290 34.3409 7.3027 3595.5916 32.1221 55.1795 4.2237 gifts home outdoor 4.2716 17.4545 16.8812 204.3875 3165.0375 191.9873 51.9084 10.4563 home cleaning bread 0.0455 5.6154 1.3333 82.6786 75.6465 130.9721 6.0813 7.8811 home cleaning canned & pickled 0.3607 10.8696 7.6347 102.5252 75.0585 36.0978 6.0571 4.5789	fruit & vegetables	home cleaning	0.2820	11.1499	7.2162	112.2010	35.1904	75.5778	4.3581	6.0774
gifts bread 5.8374 29.6087 33.1800 62.1844 $3589.9013 134.1996$ 55.1349 8.0206 gifts canned & pickled 19.3257 33.4576 34.8906 21.6889 $3716.302 (35.2596$ 56.6101 4.5125 gifts fruit & vegetables 16.5496 33.6290 34.3409 7.3027 $3595.591 (32.1221$ 55.1795 4.2237 gifts home outdoor 4.2716 17.4545 16.8812 204.3875 $3165.0375 191.9873$ 51.9084 10.4563 home cleaning bread 0.0455 5.6154 1.3333 82.6786 75.6465 130.9721 6.0813 7.8811 home cleaning canned & pickled 0.3607 10.8696 7.6347 102.5252 75.0585 36.0978 6.0571 4.5789	fruit & vegetables	home outdoor	1.7650	22.9271	26.6697	243.9330	34.0048	166.4065	4.3028	9.7366
gifts canned & pickled 19.3257 33.4576 34.8906 21.6889 3716.302C35.2596 56.6101 4.5125 gifts fruit & vegetables 16.5496 33.6290 34.3409 7.3027 3595.5916 32.1221 55.1795 4.2237 gifts home outdoor 4.2716 17.4545 16.8812 204.3875 3165.0375 191.9873 51.9084 10.4563 home cleaning bread 0.0455 5.6154 1.3333 82.6786 75.6465 130.9721 6.0813 7.8811 home cleaning canned & pickled 0.3607 10.8696 7.6347 102.5252 75.0585 36.0978 6.0571 4.5789	fruit & vegetables	international food	0.1753	10.5574	6.2214	123.0611	34.9631	64.4866	4.3482	5.7749
gifts canned & pickled 19.3257 33.4576 34.8906 21.6889 3716.302×35.2596 56.6101 4.5125 gifts fruit & vegetables 16.5496 33.6290 34.3409 7.3027 3595.5916×32.1221 55.1795 4.2237 gifts home outdoor 4.2716 17.4545 16.8812 204.3875 3165.037 \times 191.9873 51.9084 10.4563 home cleaning bread 0.0455 5.6154 1.3333 82.6786 75.6465 130.9721 6.0813 7.8811 home cleaning canned & pickled 0.3607 10.8696 7.6347 102.5252 75.0585 36.0978 6.0571 4.5789	gifts	bread	5.8374	29.6087	33.1800	62.1844	3589.9013	134.1996	55.1349	8.0206
gifts fruit & vegetables 16.5496 33.6290 34.3409 7.3027 3595.5916 32.1221 55.1795 4.2237 gifts home outdoor 4.2716 17.4545 16.8812 204.3875 3165.0375 191.9873 51.9084 10.4563 home cleaning bread 0.0455 5.6154 1.3333 82.6786 75.6465 130.9721 6.0813 7.8811 home cleaning canned & pickled 0.3607 10.8696 7.6347 102.5252 75.0585 36.0978 6.0571 4.5789	gifts						3716.3020	35.2596	56.6101	
gifts home outdoor 4.2716 17.4545 16.8812 204.3875 3165.0375 191.9873 51.9084 10.4563 home cleaning bread 0.0455 5.6154 1.3333 82.6786 75.6465 130.9721 6.0813 7.8811 home cleaning canned & pickled 0.3607 10.8696 7.6347 102.5252 75.0585 36.0978 6.0571 4.5789	gifts									
home cleaning bread 0.0455 5.6154 1.3333 82.6786 75.6465 130.9721 6.0813 7.8811 home cleaning canned & pickled 0.3607 10.8696 7.6347 102.5252 75.0585 36.0978 6.0571 4.5789	gifts									10.4563
home cleaning canned & pickled 0.3607 10.8696 7.6347 102.5252 75.0585 36.0978 6.0571 4.5789	home cleaning									
	home cleaning	dairy	0.0165	6.7582	3.2583	75.2279	75.5464	87.8832	6.0762	6.4103

Each domain and domain-pair ratings' dispersion statistics for the supermarket dataset contd.

source	target	total KL- divergence		median user KL- divergend		Kurtosis	target Kurtosis rating	source skewness rating	target skewness rating
home cleaning	fruit & vegetables	0.1981	9.3715	6.8456	62.3803	75.5778	35.1904	6.0774	4.3581
home cleaning	international food	0.0521	7.6893	2.8066	111.0918	75.2303	63.9973	6.0657	5.7524
home outdoor	bread	0.0461	7.5142	3.6506	97.6236	166.3014	134.3117	9.7343	8.0474
home outdoor	canned & pickled	0.8344	18.8026	17.7775	129.5316	165.3755	35.5754	9.7181	4.5391
home outdoor	fruit & vegetables	0.5194	16.1495	14.7704	82.4525	166.4065	34.0048	9.7366	4.3028
home outdoor	gifts	0.1776	2.6581	0.0000	85.2015	191.9873	3165.0375	10.4563	51.9084
international food	bread	0.1111	8.5279	2.6630	129.1309	64.4583	132.2087	5.7741	7.9308
international food	canned & pickled	0.2045	13.5800	10.2547	128.4001	64.5412	35.3256	5.7773	4.5306
international food	dairy	0.0641	9.9652	5.2828	115.3590	64.4671	88.1089	5.7740	6.4261
international food	fruit & vegetables	0.0850	12.0788	9.5737	85.3462	64.4866	34.9631	5.7749	4.3482
international food	home cleaning	0.0365	9.6382	4.6167	124.7317	63.9973	75.2303	5.7524	6.0657

A.3 ERROR OF ALGORITHMS ON DOMAIN PAIRS IN SUPERMARKET DATASET

Table 40: RMSE and MAE for domain-pairs in the supermarket dataset

bread	canned & pickled	0.3079	0.5052	0.4909	0.2903	0.5427	0.2681	0.4161	0.4016	0.1690	0.4414
bread	dairy	0.3242	0.4956	0.4934	0.2443	0.7641	0.2857	0.4048	0.4010	0.1470	0.3233
bread	events	0.3251	0.4177	0.2406	0.5641	0.4975	0.2464	0.2738	0.1474	0.3631	0.3774
bread	fruit & vegetables	0.2909	0.4515	0.4533	0.1527	0.3495	0.2583	0.3637	0.3657	0.0980	0.1678
bread	gifts	0.3583	0.4230	0.2784	0.6110	2.1877	0.2742	0.2988	0.1930	0.4172	0.4741
bread	home cleaning	0.2877	0.4110	0.3692	0.2364	0.5288	0.2437	0.3332	0.2975	0.1331	0.4400
bread	home outdoor	0.3577	0.5301	0.3505	0.5749	0.5180	0.2700	0.4037	0.2388	0.3740	0.3904
bread	international food	0.3590	0.5177	0.4491	0.3617	0.8108	0.2977	0.4208	0.3485	0.2121	0.4500
canned & pickled	bread	0.3821	0.4889	0.4967	0.2785	0.4732	0.3472	0.4011	0.4102	0.1702	0.3594
canned & pickled	dairy	0.3459	0.5666	0.5790	0.2474	0.6084	0.3111	0.4782	0.4919	0.1702	0.2604
canned & pickled	events	0.3613	0.3365	0.2567	0.5528	0.6140	0.2828	0.2026	0.1543	0.3436	0.3588
canned & pickled	fruit & vegetables	0.3198	0.4607	0.4712	0.1529	0.2677	0.2883	0.3722	0.3824	0.0995	0.1524
canned & pickled	gifts	0.3563	0.3468	0.2633	0.5902	0.8015	0.2858	0.2292	0.1788	0.3915	0.4230
canned & pickled	home cleaning	0.2982	0.3896	0.3725	0.2468	0.9035	0.2529	0.3143	0.3005	0.1379	0.3245
canned & pickled	home outdoor	0.3688	0.3925	0.3049	0.5768	0.5440	0.2817	0.2767	0.2214	0.3739	0.3695
canned & pickled	international food	0.3955	0.4547	0.3717	0.3577	0.6034	0.3174	0.3637	0.2948	0.2054	0.4759
dairy	bread	0.3831	0.4711	0.4801	0.2826	0.8269	0.3485	0.3844	0.3930	0.1768	0.3469
dairy	canned & pickled	0.3387	0.5532	0.5319	0.3051	0.5480	0.3001	0.4637	0.4397	0.1827	0.4469
dairy	fruit & vegetables	0.3298	0.4473	0.4592	0.1513	0.2886	0.3026	0.3593	0.3710	0.0975	0.1625
dairy	home cleaning	0.3075	0.5071	0.4746	0.2407	0.5545	0.2637	0.4216	0.3877	0.1395	0.4520
dairy	international food	0.3945	0.4758	0.3795	0.3747	0.6692	0.3177	0.3837	0.3014	0.2247	0.4404
events	bread	0.3791	0.3930	0.3932	0.2671	0.4269	0.3411	0.3165	0.3134	0.1712	0.3058
events	canned & pickled	0.3417	0.3964	0.4025	0.2641	0.4680	0.2942	0.3207	0.3240	0.1562	0.3575
events	fruit & vegetables	0.3248	0.3549	0.3524	0.1486	0.3930	0.2850	0.2777	0.2737	0.0963	0.2298
fruit & vegetables	bread	0.3830	0.4779	0.4717	0.2878	0.5003	0.3480	0.3901	0.3843	0.1749	0.3482
fruit & vegetables	canned & pickled	0.3424	0.5180	0.4917	0.3047	0.5646	0.3036	0.4291	0.4024	0.1801	0.4361
fruit & vegetables	dairy	0.3472	0.4979	0.4917	0.2355	0.5321	0.3144	0.4065	0.4014	0.1417	0.4053
fruit & vegetables	events	0.3528	0.6251	0.2484	0.5661	0.4967	0.2772	0.5294	0.1487	0.3700	0.3904
fruit & vegetables	gifts	0.3687	0.5832	0.2843	0.5981	0.6281	0.2906	0.4949	0.1937	0.4070	0.3735
fruit & vegetables	home cleaning	0.2993	0.5435	0.4736	0.2502	0.5393	0.2544	0.4597	0.3870	0.1416	0.4422
fruit & vegetables	home outdoor	0.3693	0.5561	0.3270	0.5913	0.6861	0.2821	0.4722	0.2315	0.4021	0.3479
fruit & vegetables	international food	0.3903	0.4932	0.3822	0.3938	0.5942	0.3136	0.4081	0.3060	0.2371	0.4953
gifts	bread	0.3665	0.3938	0.4052	0.2617	0.4166	0.3273	0.3159	0.3260	0.1631	0.3037
gifts	canned & pickled	0.3226	0.3968	0.3995	0.2691	0.4597	0.2796	0.3201	0.3209	0.1637	0.3556
gifts	fruit & vegetables	0.3027	0.3468	0.3607	0.1481	0.6015	0.2656	0.2712	0.2809	0.0956	0.1791
gifts	home outdoor	0.3465	0.3402	0.3339	0.5783	1.1719	0.2627	0.2295	0.2241	0.3753	0.4182

RMSE and MAE for domain-pairs in the supermarket dataset contd.

source	target	CCA RMSE	CD- SVD RMSE	SD- SVD RMSE	RMGM RMSE	CMF RMSE	CCA MAE	CD- SVD MAE	SD- SVD MAE	RMGM MAE	CMF MAE
home cleaning	bread	0.3852	0.3775	0.4031	0.2858	0.4801	0.3504	0.3002	0.3228	0.1739	0.3649
home cleaning	canned & pickled	0.3466	0.4024	0.3971	0.2948	0.5565	0.3068	0.3246	0.3212	0.1711	0.4448
home cleaning	dairy	0.3547	0.4922	0.4913	0.2382	0.5311	0.3222	0.4024	0.4019	0.1448	0.4049
home cleaning	fruit & vegetables	0.3347	0.5020	0.5170	0.1502	0.2700	0.3076	0.4114	0.4274	0.0971	0.1549
home cleaning	international food	0.4043	0.5097	0.4548	0.3700	0.6406	0.3224	0.4068	0.3518	0.2151	0.4581
home outdoor	bread	0.3517	0.4847	0.4857	0.2629	0.4540	0.3119	0.3979	0.3985	0.1652	0.3167
home outdoor	canned & pickled	0.3212	0.4052	0.3897	0.2620	0.4637	0.2778	0.3279	0.3151	0.1587	0.3594
home outdoor	fruit & vegetables	0.3034	0.3495	0.3511	0.1473	0.3537	0.2659	0.2713	0.2745	0.0960	0.2188
home outdoor	gifts	0.3232	0.3128	0.3057	0.6024	0.6012	0.2438	0.1982	0.1942	0.4018	0.3945
international food	bread	0.3912	0.4873	0.4867	0.2956	0.4548	0.3549	0.3994	0.3996	0.1782	0.3189
international food	canned & pickled	0.3356	0.3873	0.3962	0.2722	0.4583	0.2955	0.3141	0.3202	0.1603	0.3579
international food	dairy	0.3484	0.3968	0.4101	0.2261	0.4811	0.3123	0.3173	0.3293	0.1416	0.3597
international food	fruit & vegetables	0.3219	0.3468	0.3551	0.1462	0.3009	0.2883	0.2685	0.2770	0.0952	0.1604
international food	home cleaning	0.2971	0.4891	0.4688	0.2414	0.4078	0.2522	0.4012	0.3816	0.1331	0.2649

 $\begin{tabular}{ll} Table 41: Significant RMSE relations of algorithms in each domain pair for the Supermarket dataset \\ \end{tabular}$

bread canned & pickled 1 0 1 0 1 0 1 0 0 0 1 1 0 1 0 1 0 1 0																							
bread fruit & vegetables 1 0 0 1 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1		canned & pickled																					10
bread gifts 0 0 1 0 1 0 1 0 1 0 0 1 0 0 1 0 0 1 0 0 1 0 0 0 1 0 0 0 1 0 0 0 1 0 0 0 0 1 0		v																					
bread gifts 0 0 0 1 0 1 0 0 1 0 0 0 1 0 0 0 0 0 0																							
bread home cleaning 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1	bread	_	1	0	1	0	1	0	0	1	1	0	1	0	1	0	1	0	0	0			
bread home outdoor 1 0 0 0 1 0 1 0 1 0 0 0 1 0 0 1 0 0 0 0 1 0	bread		0	0	0	1	0	0	1	0	0	0	0	0	0	1	0	1	0	1	0	0	5
bread international food 1 0 1 0 1 0 1 0 0 0 0 1 0 1 0 1 0 1 0	bread	home cleaning	1	0	1	0	1	0	0	1	0	1	0	1	1	0	1	0	0	1	0	1	10
canned & pickled bread	bread	home outdoor	1	0	0	0	1	0	1	0	0	1	0	0	0	1	0	1	0	1	0	0	7
canned & pickled dairy 1 0 1 0 0 0 0 1 0 1 0 0 0 0 1 0 1 0 1	bread	international food	1	0	1	0	1	0	0	0	0	1	0	1	1	0	1	0	0	1	0	1	9
canned & pickled events 0 0 1 1 0 1	canned & pickled	bread	1	0	1	0	1	0	0	1	1	0	1	0	1	0	1	0	0	0	0	1	9
canned & pickled fruit & vegetables 1 0 1	canned & pickled	dairy	1	0	1	0	0	0	0	1	0	0	0	0	1	0	1	0	0	0	0	0	5
canned & pickled gifts 0 0 0 1 1 0	canned & pickled	events	0	0	0	1	1	0	1	0	0	1	0	1	0	1	0	1	0	1	0	0	8
canned & pickled home cleaning 1 0	canned & pickled	fruit & vegetables	1	0	1	0	0	1	0	1	1	0	1	0	1	0	1	0	0	0	0	1	9
canned & pickled home outdoor 0 0 1 1 0 1<	canned & pickled	gifts	0	0	0	1	1	0	1	0	0	1	0	1	0	1	0	1	0	1	0	0	8
canned & pickled international food 1 0 0 1 0 0 1 0 0 1 0 0 1	canned & pickled	home cleaning	1	0	1	0	1	0	0	1	0	1	0	1	1	0	1	0	0	0	0	1	9
dairy bread 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 0 1 0 1 0 0 0 0 1	canned & pickled	home outdoor	0	0	0	1	1	0	1	0	0	1	0	1	0	1	0	1	0	1	0	0	8
dairy canned & pickled 1 0 1 0 1 0 0 1 0 0 0 0 1 0 1 0 1 0 1	canned & pickled	international food	1	0	0	0	1	0	0	1	0	1	0	1	0	0	1	0	0	1	0	1	8
dairy fruit & vegetables 1 0 1 0 0 1 0 1 1 0 1 0 1 0 1 0 1 0 1	dairy	bread	1	0	1	0	1	0	0	1	0	1	0	1	1	0	1	0	0	0	0	1	9
dairy home cleaning 1 0 1 0 1 0 0 1 0 1 0 1 0 1 0 0 1 0 1	dairy	canned & pickled	1	0	1	0	1	0	0	1	0	0	0	0	1	0	1	0	0	1	0	1	8
dairy international food 1 0 0 0 1 0 0 0 1 0 1 0 0 1 0 1 7	dairy	fruit & vegetables	1	0	1	0	0	1	0	1	1	0	1	0	1	0	1	0	1	0	0	1	10
	dairy	home cleaning	1	0	1	0	1	0	0	1	0	1	0	1	1	0	1	0	0	1	0	1	10
events bread 0 0 0 0 1 0 0 1 0 1 0 1 0 1 0 0 0 0 1 7	dairy	international food	1	0	0	0	1	0	0	0	0	1	0	1	0	0	1	0	0	1	0	1	7
	events	bread	0	0	0	0	1	0	0	1	0	1	0	1	1	0	1	0	0	0	0	1	7
events canned & pickled 1 0 1 0 1 0 0 1 0 1 0 1 0 1 0 0 0 0 1 9	events	canned & pickled	1	0	1	0	1	0	0	1	0	1	0	1	1	0	1	0	0	0	0	1	9
events fruit & vegetables 1 0 1 0 0 0 0 1 0 0 0 1 0 1 0 0 0 1 6	events	fruit & vegetables	1	0	1	0	0	0	0	1	0	0	0	0	1	0	1	0	0	0	0	1	6
fruit & vegetables bread 1 0 1 0 1 0 0 1 0 0 0 0 1 0 1 0 0 0 0	fruit & vegetables	bread	1	0	1	0	1	0	0	1	0	0	0	0	1	0	1	0	0	0	0	1	7
fruit & vegetables canned & pickled $\begin{array}{cccccccccccccccccccccccccccccccccccc$	fruit & vegetables	canned & pickled	1	0	1	0	1	0	0	1	0	1	0	1	1	0	1	0	0	1	0	1	10
fruit & vegetables dairy 1 0 1 0 1 0 0 1 0 1 0 1 0 1 0 0 0 0 1 9	fruit & vegetables	dairy	1	0	1	0	1	0	0	1	0	1	0	1	1	0	1	0	0	0	0	1	9
fruit & vegetables events 1 0 0 1 1 0 1 0 0 1 1 0 0 1 1 0 0 1 1 0 10	fruit & vegetables	events	1	0	0	1	1	0	1	0	0	1	1	0	0	1	1	0	0	1	1	0	10
fruit & vegetables gifts 1 0 0 1 1 0 1 0 0 1 0 0 0 1 0 0 0 7	fruit & vegetables	gifts	1	0	0	1	1	0	1	0	0	1	0	0	0	1	0	0	0	1	0	0	7
fruit & vegetables home cleaning 1 0 1 0 1 0 0 1 0 1 0 0 1 0 1 0 1 9	fruit & vegetables	home cleaning	1	0	1	0	1	0	0	1	0	1	0	0	1	0	1	0	0	1	0	1	9
fruit & vegetables home outdoor 1 0 0 0 0 1 0 0 1 0 0 0 1 0 0 5	fruit & vegetables	home outdoor	1	0	0	0	0	0	1	0	0	1	0	0	0	1	0	0	0	1	0	0	5
fruit & vegetables international food $\begin{array}{cccccccccccccccccccccccccccccccccccc$	fruit & vegetables	international food	1	0	0	0	1	0	0	0	0	1	0	1	0	0	1	0	0	1	0	1	7
gifts bread 1 0 1 0 1 0 0 1 0 0 0 1 1 0 0 0 0 1 8	gifts	bread	1	0	1	0	1	0	0	1	0	0	0	1	1	0	1	0	0	0	0	1	8
gifts canned & pickled 1 0 1 0 1 0 0 1 0 1 0 1 0 1 0 0 0 0 1 9		canned & pickled	1	0	1	0	1	0	0		0	1	0	1		0	1	0	0	0	0	1	9
gifts fruit & vegetables 1 0 1 0 1 0 0 1 0 0 0 1 0 1 0 0 0 0 1 7	_	_	1	0																	0		
gifts home outdoor 0 0 0 0 0 0 1 0 0 0 0 1 0 1 0 0 0 0 3			0																				
home cleaning bread 0 0 1 0 1 0 0 1 0 1 0 1 0 1 0 1 0 1 9																							
home cleaning canned & pickled 1 0 1 0 1 0 0 1 0 1 0 1 1 0 1 0 0 0 0																							
home cleaning dairy 1 0 1 0 1 0 0 1 0 1 0 1 0 0 0 0 0 1 9																							

Significant RMSE relations of algorithms in each domain pair for the Supermarket dataset contd.

source	target	CD-CCA >CD-SVD	CD-SVD > CD-CCA	CD-CCA >SD-SVD	SD-SVD >CD-CCA	CD-CCA >CMF	CMF >CD-CCA	CD-CCA >RMGM	RMGM >CDCCA	CMF > SD-SVD	SD-SVD >CMF	CMF >CD-SVD	CD-SVD >CMF	RMGM >SD-SVD	SD-SVD >RMGM	RMGM >CD-SVD	CD-SVD >RMGM	CD-SVD >SD-SVD	SD-SVD >CD-SVD	CMF >RMGM	RMGM >CMF	sum
home cleaning	fruit & vegetables	1	0	1	0	0	1	0	1	1	0	1	0	1	0	1	0	1	0	0	1	10
home cleaning	international food	1	0	1	0	1	0	0	0	0	1	0	1	1	0	1	0	0	1	0	1	9
home outdoor	bread	1	0	1	0	1	0	0	1	0	0	1	0	1	0	1	0	0	0	0	1	8
home outdoor	canned & pickled	1	0	1	0	1	0	0	1	0	1	0	1	1	0	1	0	0	0	0	1	9
home outdoor	fruit & vegetables	1	0	1	0	1	0	0	1	0	0	0	0	1	0	1	0	0	0	0	1	7
home outdoor	gifts	0	0	0	0	1	0	1	0	0	1	0	1	0	1	0	1	0	0	0	0	6
international food	bread	1	0	1	0	1	0	0	1	1	0	1	0	1	0	1	0	0	0	0	1	9
international food	canned & pickled	1	0	1	0	1	0	0	1	0	1	0	1	1	0	1	0	0	0	0	1	9
international food	dairy	1	0	1	0	1	0	0	1	0	1	0	1	1	0	1	0	1	0	0	1	10
international food	fruit & vegetables	1	0	1	0	0	0	0	1	1	0	1	0	1	0	1	0	0	0	0	1	8
international food	home cleaning	1	0	1	0	1	0	0	1	0	0	0	0	1	0	1	0	0	0	0	1	7

 $\begin{tabular}{ll} Table 42: Significant MAE relations of algorithms in each domain pair for the Supermarket dataset \\ \end{tabular}$

bread dairy 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1
bread events 0 0 0 1 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1
bread gifts 0 0 1 0 1 0 0 1 0 0 1 0 0 1 0 0 1 0 0 1 0 0 1 0 0 1 0 0 1 0
bread gifts 0 0 0 1 0 1 0 0 1 0 0 1 0 0 1 0 0 1 0 0 0 1 0 0 0 1 0
bread home cleaning 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 0 1 1 0 0 1 1 0 0 1 0 0 1 0 0 1 0 0 1 0 0 0 1 0 0 0 0 1 0
bread home outdoor 1 0 0 0 1 0 1 0 1 0 0 0 1 0 0 0 1 0 0 0 0 0 1 0
bread international food 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1
canned & pickled bread 1 0 1 0 0 0 1 1 0 1
canned & pickled dairy 1 0 1 0 0 1 0 0 1 0 1 0 1 0 1 0 1 0 1
canned & pickled events 0 1 0 0 0 1 0 1 0 0 0 1 0 1 0 0 0 1 0 0 0 1 0 0 0 1 0 0 0 1 0 0 0 1 0 0 0 1 0 0
canned & pickled fruit & vegetables 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 0 1 0 1 0 0 1 0 1 0 0 1 0 1 0 0 0 1 0 0 0 0 0 0 1 0 0 0 0 1 0
canned & pickled gifts 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 0 1 0 0 1 0 0 0 1 0 0 0 1 0 0 0 0 1 0 0 0 0 1 0 0 0 0 1 0 0 0 0 1 0 0 0 0 1 0 0 0 0 1 0 0 0 0 1 0 0 0 0 1 0 0 0 0 1 0 0 0 1 0 0 1 0 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0
canned & pickled home cleaning 1 0 1 0 1 0 1 0 0 1 0 0 0 1 0 1 0 1 0
canned & pickled home outdoor 0 0 0 1 1 0 1
canned & pickled international food 1 0 0 1 1 0 0 1 0 1 0 1 0 1 0 0 1 1 0 1 1 0 1 1 0 1 1 0 1 1 0 1 1 0 1 1 0 1 1 0 1 1 0 1 1 0 1 1 0 1 1 0 1 1 0 1 1 0 1 1 0 1 1 0 1 1 0 1 1 0 1 1 0 1 1 1 0 1 1 1 0 1 1 1 0 1 1 1 1 0 1
dairy bread 1 0 1 0 0 0 0 1 1 0 1 0 1 0 0 0 0 1 8
·
dairy canned & pickled 1 0 1 0 1 0 0 1 0 0 0 0 1 0 1 0 1 8
dairy fruit & vegetables 1 0 1 0 0 1 0 1 1 0 1 0 1 0 1 0 1 0 1
dairy home cleaning $\begin{array}{cccccccccccccccccccccccccccccccccccc$
dairy international food 1 0 0 0 1 0 0 1 0 1 0 1 0 1 0 0 1 0 1
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$
events canned & pickled 1 0 0 0 1 0 0 1 0 1 0 1 0 1 0 0 0 1 8
events fruit & vegetables 0 0 0 0 0 1 0 1 0 1 0 1 0 1 0 0 0 0 1 7
fruit & vegetables bread 1 0 1 0 0 0 0 1 1 0 1 0 1 0 0 0 0 1 8
fruit & vegetables canned & pickled $\begin{array}{cccccccccccccccccccccccccccccccccccc$
fruit & vegetables dairy 1 0 1 0 1 0 0 1 0 0 0 0 1 0 1 0 0 0 0
fruit & vegetables events $ 1 0 0 1 1 0 0 1 1 0 0$
fruit & vegetables gifts 1 0 0 1 1 0 1 0 0 1 1 0 0 1 1 0 0 9
fruit & vegetables home cleaning $\begin{array}{cccccccccccccccccccccccccccccccccccc$
fruit & vegetables home outdoor 1 0 0 1 1 0 1 0 0 1 1 0 0 1 1 0 0 1 1 0 0 1
fruit & vegetables international food $\begin{array}{cccccccccccccccccccccccccccccccccccc$
gifts bread 0 0 0 0 0 0 0 1 1 0 0 0 1 0 0 0 0 1 5
gifts canned & pickled 1 0 1 0 1 0 0 1 0 1 0 1 0 1 0 0 0 0 1 9
gifts fruit & vegetables 0 0 1 0 0 1 0 1 1 0 1 0 1 0 0 0 0 1 8
gifts home outdoor 0 0 0 0 1 0 1 0 1 0 1 0 1 0 0 0 6
home cleaning bread 0 1 0 1 0 0 0 1 0 1 0 1 0 1 0 1 0 1 9
home cleaning canned & pickled 0 0 0 0 1 0 0 1 0 1 0 1 0 1 0 0 0 0 1 7
home cleaning dairy 1 0 1 0 1 0 0 1 0 0 0 0 1 0 1 0 0 0 0

Significant MAE relations of algorithms in each domain pair for the Supermarket dataset contd.

source	target	CD-CCA >CD-SVD	CD-SVD > CD-CCA	CD-CCA >SD-SVD	SD-SVD >CD-CCA	CD-CCA >CMF	CMF >CD-CCA	CD-CCA >RMGM	RMGM >CDCCA	CMF > SD-SVD	SD-SVD >CMF	CMF >CD-SVD	CD-SVD >CMF	RMGM >SD-SVD	SD-SVD >RMGM	RMGM >CD-SVD	CD-SVD >RMGM	CD-SVD >SD-SVD	SD-SVD >CD-SVD	CMF >RMGM	RMGM >CMF	sum
home cleaning	fruit & vegetables	1	0	1	0	0	1	0	1	1	0	1	0	1	0	1	0	1	0	0	1	10
home cleaning	international food	1	0	0	0	1	0	0	1	0	1	0	1	1	0	1	0	0	1	0	1	9
home outdoor	bread	1	0	1	0	0	0	0	1	1	0	1	0	1	0	1	0	0	0	0	1	8
home outdoor	canned & pickled	1	0	1	0	1	0	0	1	0	1	0	0	1	0	1	0	0	0	0	1	8
home outdoor	fruit & vegetables	0	0	0	0	0	1	0	1	1	0	1	0	1	0	1	0	0	0	0	1	7
home outdoor	gifts	0	1	0	1	1	0	1	0	0	1	0	1	0	1	0	1	0	0	0	0	8
international food	bread	1	0	1	0	0	1	0	1	1	0	1	0	1	0	1	0	0	0	0	1	9
international food	canned & pickled	1	0	1	0	1	0	0	1	0	1	0	1	1	0	1	0	0	0	0	1	9
international food	dairy	0	0	1	0	1	0	0	1	0	1	0	1	1	0	1	0	0	0	0	1	8
international food	fruit & vegetables	0	1	0	0	0	1	0	1	1	0	1	0	1	0	1	0	0	0	0	1	8
international food	home cleaning	1	0	1	0	0	0	0	1	1	0	1	0	1	0	1	0	0	0	0	1	8

A.4 COLD-START ANALYSIS OF DOMAIN PAIRS FOR SUPERMARKET DATASET

A.4.1 MAEs for Target User Profiles

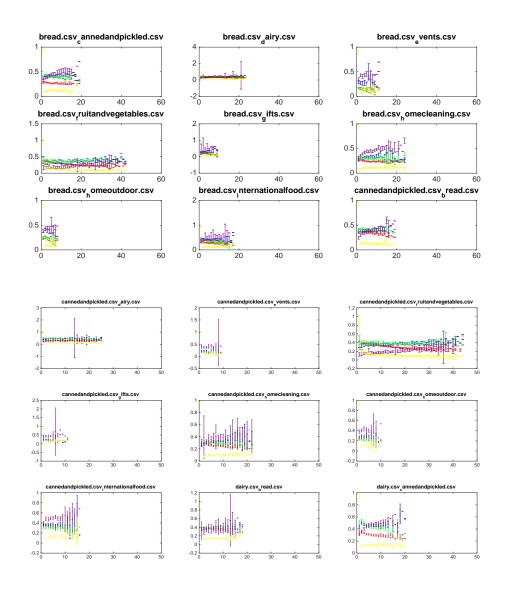


Figure 52: User-based MAE of algorithms in the supermarket dataset, averaged on each domain-pair and sorted based on the users' target domain profile size

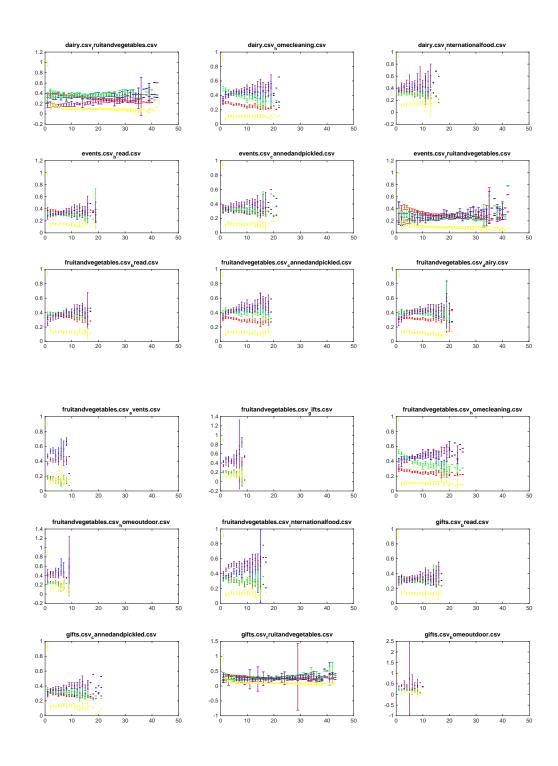


Figure 52: User-based MAE of algorithms in the supermarket dataset, averaged on each domain-pair and sorted based on the users' target domain profile size for domain pairs 19 to 36

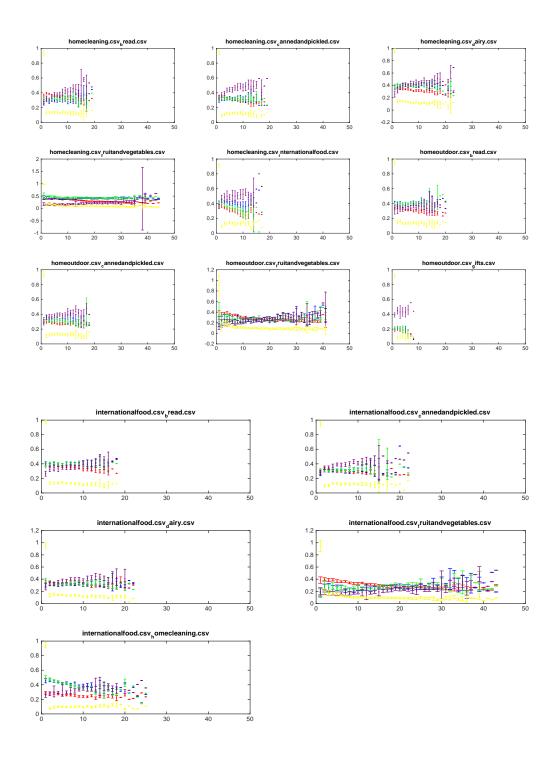


Figure 52: User-based MAE of algorithms in the supermarket dataset, averaged on each domain-pair and sorted based on the users' target domain profile size for domain pairs 37 to 50

A.4.2 RMSEs for Target User Profiles

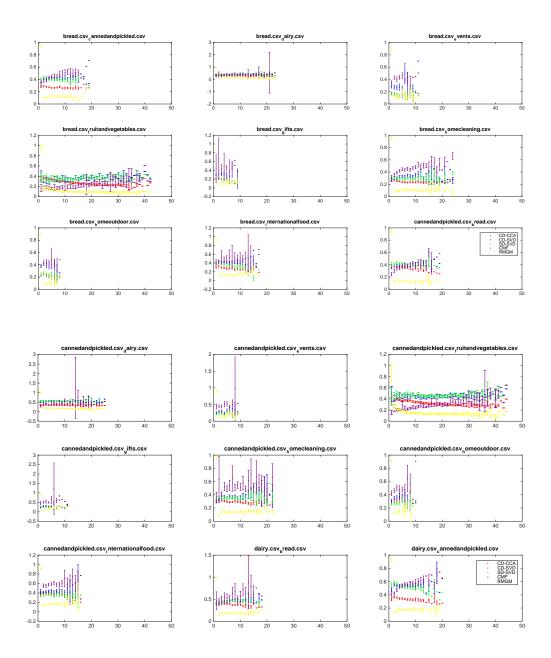


Figure 53: User-based RMSE of algorithms in the supermarket dataset, averaged on each domain-pair and sorted based on the users' Target domain profile size

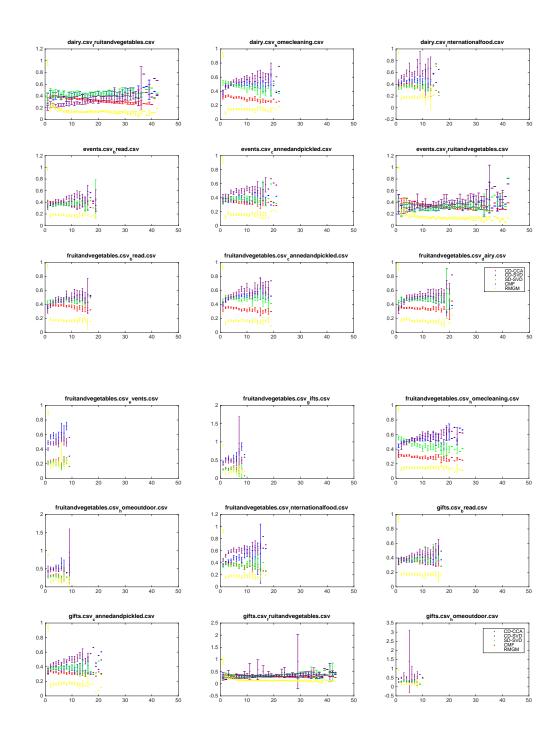


Figure 53: User-based RMSE of algorithms in the supermarket dataset, averaged on each domain-pair and sorted based on the users' Target domain profile size for domain pairs 19 to 36

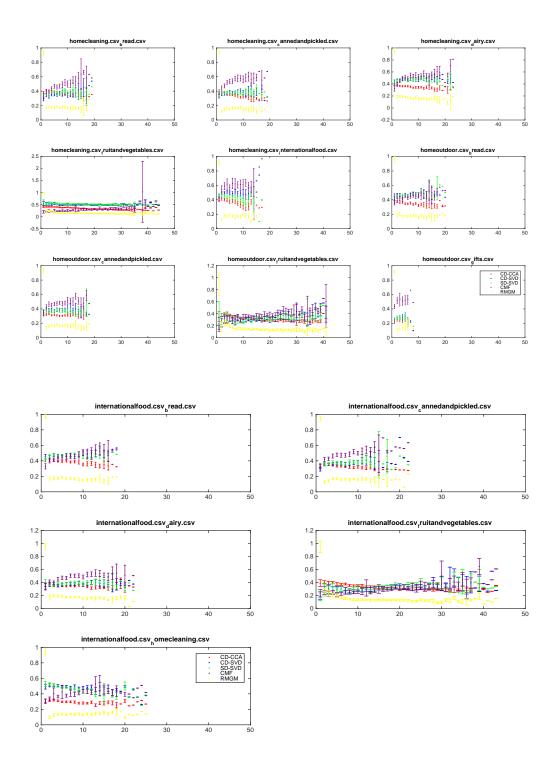


Figure 53: User-based RMSE of algorithms in the supermarket dataset, averaged on each domain-pair and sorted based on the users' Target domain profile size for domain pairs 37 to 50

A.4.3 RMSEs for Source User Profiles

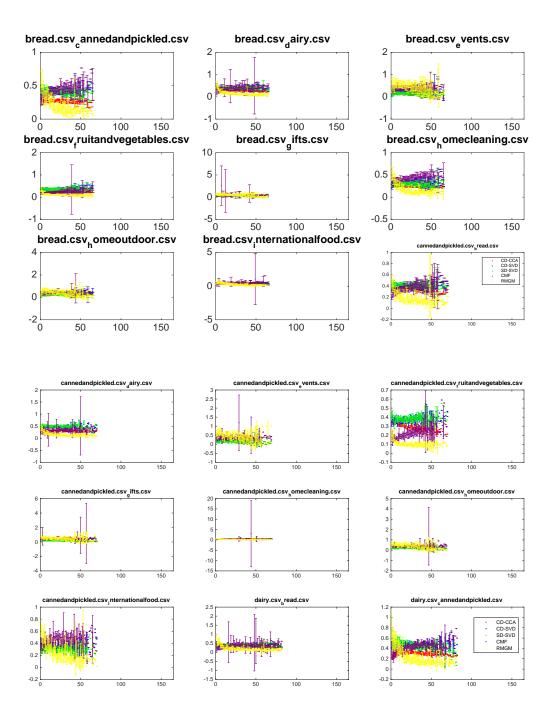


Figure 54: User-based MAE of algorithms in the supermarket dataset, averaged on each domain-pair and sorted based on the users' Source domain profile size

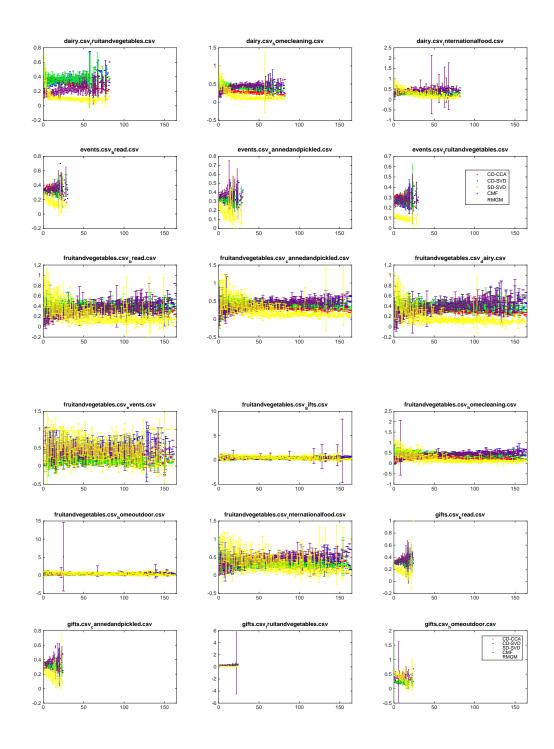


Figure 54: User-based MAE of algorithms in the supermarket dataset, averaged on each domain-pair and sorted based on the users' Source domain profile size for domain pairs 19 to 36

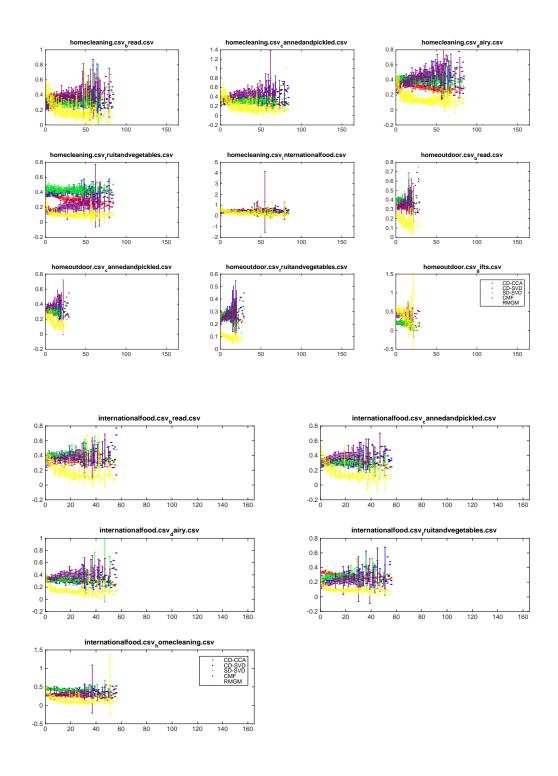


Figure 54: User-based MAE of algorithms in the supermarket dataset, averaged on each domain-pair and sorted based on the users' Source domain profile size for domain pairs 37 to 50

A.4.4 RMSEs for Source User Profiles

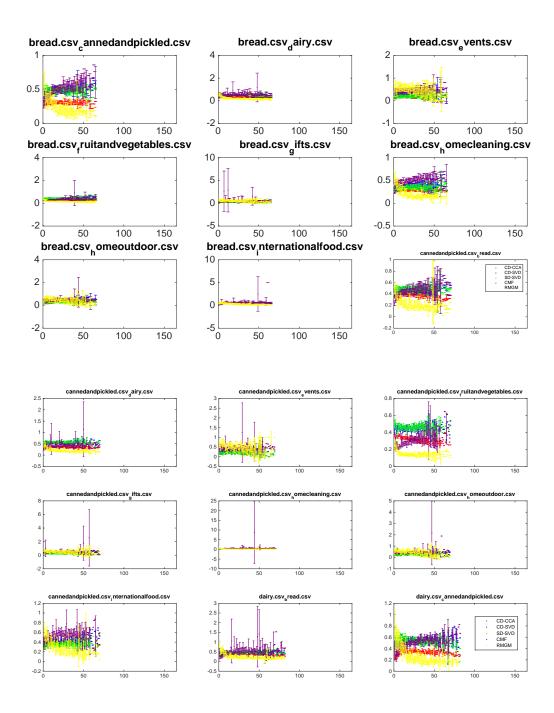


Figure 55: User-based RMSE of algorithms in the supermarket dataset, averaged on each domain-pair and sorted based on the users' Source domain profile size

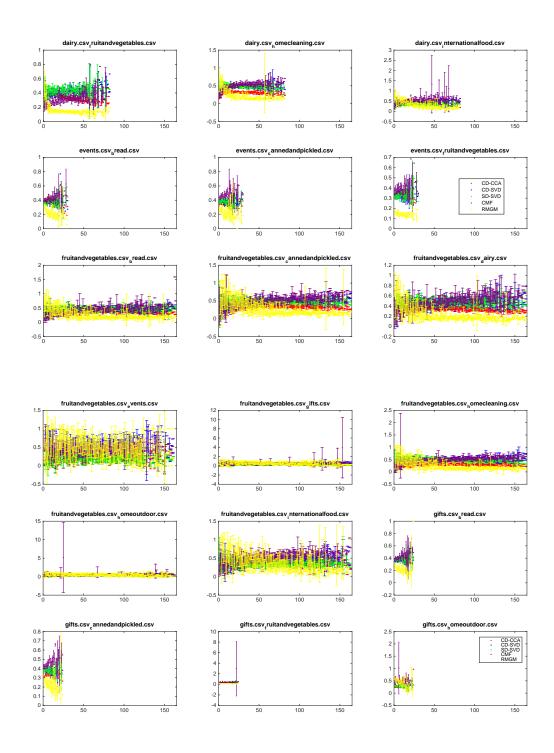


Figure 55: User-based RMSE of algorithms in the supermarket dataset, averaged on each domain-pair and sorted based on the users' Source domain profile size for domain pairs 19 to 36

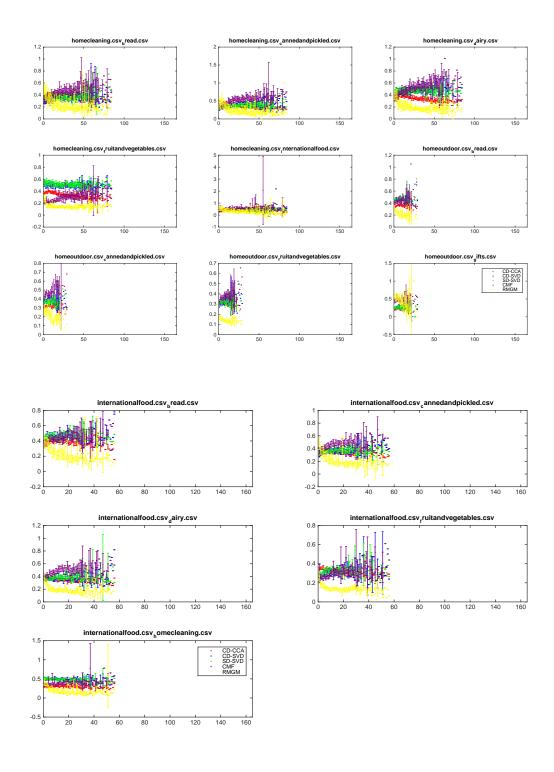


Figure 55: User-based RMSE of algorithms in the supermarket dataset, averaged on each domain-pair and sorted based on the users' Source domain profile size for domain pairs 37 to 50

A.5 CORRELATION ANALYSIS FOR SUPERMARKET DATASET

A.5.1 Correlation Analysis Plots for the RMSE of Algorithms in the Supermarket Dataset

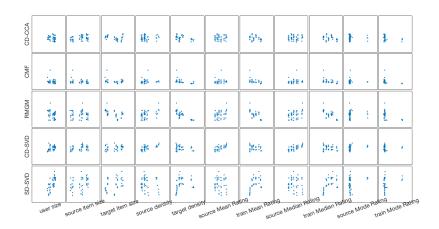


Figure 56: Scatter plot of general and central tendency statistics with the RMSE of algorithms in the Supermarket dataset

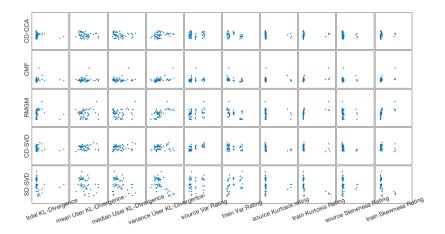


Figure 57: Scatter plot of dispersion statistics with the RMSE of algorithms in the Supermarket dataset

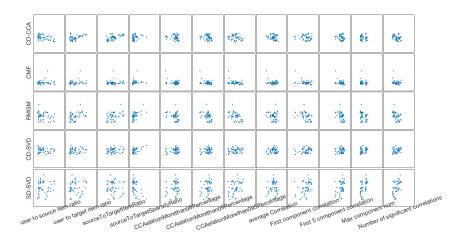


Figure 58: Scatter plot of CCA-related statistics with the RMSE of algorithms in the Supermarket dataset

A.5.2 Correlation Analysis Plots for the Improvement Ratio of Algorithms in the Supermarket Dataset

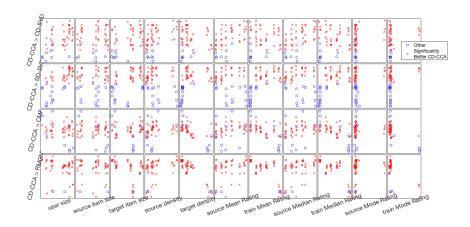


Figure 59: Scatter plot of general and central tendency statistics with the improvement ratio of CD-CCA over other algorithms in the Supermarket dataset; red cross shows the cases in which CD-CCA is significantly better than other algorithms

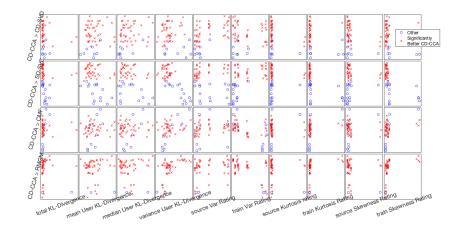


Figure 60: Scatter plot of dispersion statistics with the improvement ratio of CD-CCA over other algorithms in the Supermarket dataset; red cross shows the cases in which CD-CCA is significantly better than other algorithms

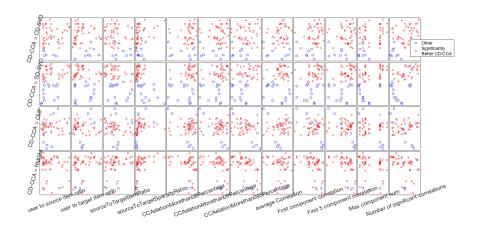


Figure 61: Scatter plot of CCA-related statistics with the improvement ratio of CD-CCA over other algorithms in the Supermarket dataset; red cross shows the cases in which CD-CCA is significantly better than other algorithms

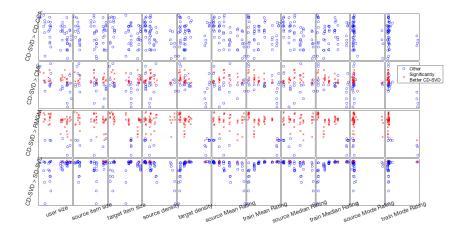


Figure 62: Scatter plot of general and central tendency statistics with the improvement ratio of CD-SVD over other algorithms in the Supermarket dataset; red cross shows the cases in which CD-SVD is significantly better than other algorithms

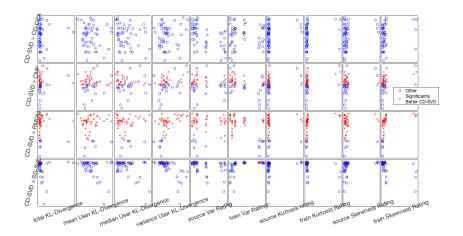


Figure 63: Scatter plot of dispersion statistics with the improvement ratio of CD-SVD over other algorithms in the Supermarket dataset; red cross shows the cases in which CD-SVD is significantly better than other algorithms

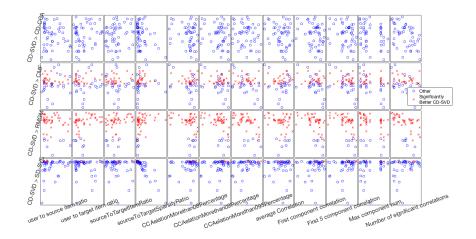


Figure 64: Scatter plot of CCA-related statistics with the improvement ratio of CD-SVD over other algorithms in the Supermarket dataset; red cross shows the cases in which CD-SVD is significantly better than other algorithms

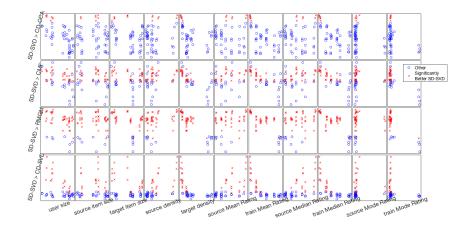


Figure 65: Scatter plot of general and central tendency statistics with the improvement ratio of SD-SVD over other algorithms in the Supermarket dataset; red cross shows the cases in which SD-SVD is significantly better than other algorithms

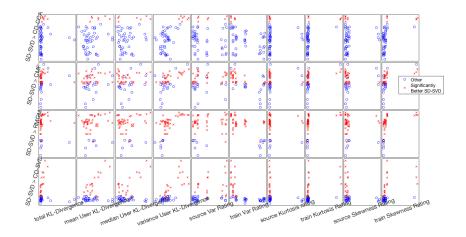


Figure 66: Scatter plot of dispersion statistics with the improvement ratio of SD-SVD over other algorithms in the Supermarket dataset; red cross shows the cases in which SD-SVD is significantly better than other algorithms

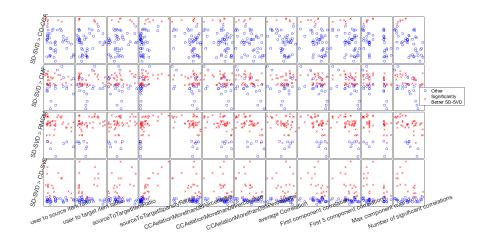


Figure 67: Scatter plot of CCA-related statistics with the improvement ratio of SD-SVD over other algorithms in the Supermarket dataset; red cross shows the cases in which SD-SVD is significantly better than other algorithms

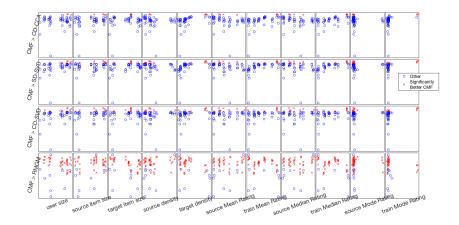


Figure 68: Scatter plot of general and central tendency statistics with the improvement ratio of CMF over other algorithms in the Supermarket dataset; red cross shows the cases in which CMF is significantly better than other algorithms

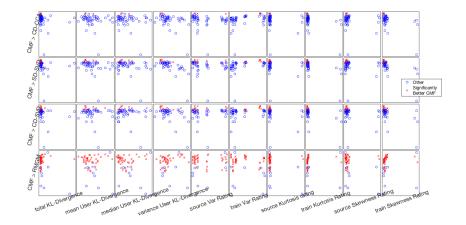


Figure 69: Scatter plot of dispersion statistics with the improvement ratio of CMF over other algorithms in the Supermarket dataset; red cross shows the cases in which CMF is significantly better than other algorithms

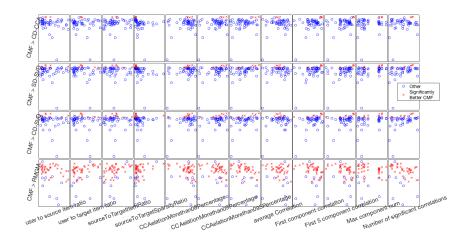


Figure 70: Scatter plot of CCA-related statistics with the improvement ratio of CMF over other algorithms in the Supermarket dataset; red cross shows the cases in which CMF is significantly better than other algorithms

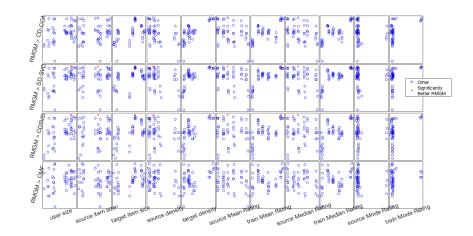


Figure 71: Scatter plot of general and central tendency statistics with the improvement ratio of RMGM over other algorithms in the Supermarket dataset; red cross shows the cases in which RMGM is significantly better than other algorithms

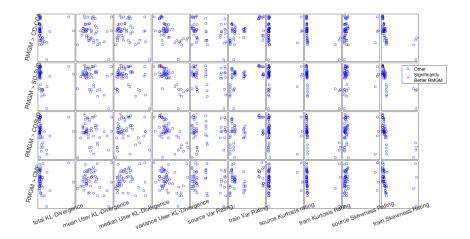


Figure 72: Scatter plot of dispersion statistics with the improvement ratio of RMGM over other algorithms in the Supermarket dataset; red cross shows the cases in which RMGM is significantly better than other algorithms

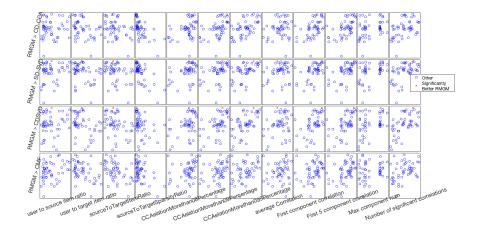


Figure 73: Scatter plot of CCA-related statistics with the improvement ratio of RMGM over other algorithms in the Supermarket dataset; red cross shows the cases in which RMGM is significantly better than other algorithms

APPENDIX B

YELP DATA FIGURES AND TABLES

B.1 DOMAIN PAIR STATISTICS FOR YELP DATASET

Table 43: Domain and domain-pair data size statistics for the Yelp dataset

active life	arts & entertainment	1197	458	278	0.0052	0.0110	2.6135	4.3058	1.6475	0.4756
active life	automotive	590	415	418	0.0066	0.0041	1.4217	1.4115	0.9928	1.6035
active life	beauty & spas	864	442	528	0.0056	0.0035	1.9548	1.6364	0.8371	1.6206
active life	event planning & services	1034	441	330	0.0055	0.0058	2.3447	3.1333	1.3364	0.9473
active life	food	1891	501	1505	0.0040	0.0045	3.7745	1.2565	0.3329	0.8924
active life	health & medical	471	371	322	0.0072	0.0044	1.2695	1.4627	1.1522	1.6327
active life	home services	377	369	249	0.0082	0.0056	1.0217	1.5141	1.4819	1.4621
active life	hotels & travel	935	432	255	0.0058	0.0072	2.1644	3.6667	1.6941	0.8084
active life	local services	410	360	233	0.0082	0.0064	1.1389	1.7597	1.5451	1.2839
active life	nightlife	1761	488	608	0.0042	0.0102	3.6086	2.8964	0.8026	0.4140
active life	pets	343	338	184	0.0092	0.0082	1.0148	1.8641	1.8370	1.1300
arts & entertain- ment	active life	1197	278	458	0.0110	0.0052	4.3058	2.6135	0.6070	2.1026
arts & entertain- ment	automotive	645	261	431	0.0139	0.0040	2.4713	1.4965	0.6056	3.4504
arts & entertain- ment	beauty & spas	896	276	566	0.0119	0.0033	3.2464	1.5830	0.4876	3.5988
arts & entertain- ment	education	214	212	70	0.0233	0.0170	1.0094	3.0571	3.0286	1.3728
arts & entertainment	event planning & services	1215	282	351	0.0108	0.0053	4.3085	3.4615	0.8034	2.0210

source	target	user size	source item size	target item size	source density	target density	user to source item ratio	user to target item ratio	to target item ratio	to target density ratio
arts & entertain- ment	food	2395	297	1543	0.0080	0.0041	8.0640	1.5522	0.1925	1.9552
arts & entertainment	health & medical	460	238	329	0.0153	0.0043	1.9328	1.3982	0.7234	3.5809
arts & entertainment	home services	399	231	260	0.0164	0.0055	1.7273	1.5346	0.8885	2.9656
arts & entertainment	hotels & travel	1083	275	284	0.0115	0.0066	3.9382	3.8134	0.9683	1.7535
arts & entertainment	local flavor	309	237	47	0.0217	0.0313	1.3038	6.5745	5.0426	0.6937
arts & entertainment	local services	451	247	244	0.0161	0.0061	1.8259	1.8484	1.0123	2.6313
arts & entertain- ment	nightlife	2910	295	621	0.0073	0.0083	9.8644	4.6860	0.4750	0.8828
arts & entertainment	pets	338	223	186	0.0194	0.0081	1.5157	1.8172	1.1989	2.3974
arts & entertain- ment	public services & government	284	238	70	0.0206	0.0199	1.1933	4.0571	3.4000	1.0346
arts & entertainment	shopping	1729	292	1510	0.0094	0.0030	5.9212	1.1450	0.1934	3.1490
automotive	active life	590	418	415	0.0041	0.0066	1.4115	1.4217	1.0072	0.6236
automotive	arts & entertainment	645	431	261	0.0040	0.0139	1.4965	2.4713	1.6513	0.2898
automotive	beauty & spas	506	393	456	0.0046	0.0045	1.2875	1.1096	0.8618	1.0224
automotive	event planning & services	475	387	250	0.0048	0.0089	1.2274	1.9000	1.5480	0.5352
automotive	hotels & travel	424	361	183	0.0053	0.0117	1.1745	2.3169	1.9727	0.4485
automotive	nightlife	1026	491	578	0.0031	0.0117	2.0896	1.7751	0.8495	0.2644
beauty & spas	active life	864	528	442	0.0035	0.0056	1.6364	1.9548	1.1946	0.6171
beauty & spas	arts & entertainment	896	566	276	0.0033	0.0119	1.5830	3.2464	2.0507	0.2779
beauty & spas	automotive	506	456	393	0.0045	0.0046	1.1096	1.2875	1.1603	0.9781
beauty & spas	event planning & services	1167	501	303	0.0033	0.0060	2.3293	3.8515	1.6535	0.5427
beauty & spas	food	1737	680	1451	0.0023	0.0045	2.5544	1.1971	0.4686	0.5219
beauty & spas	health & medical	547	451	336	0.0043	0.0040	1.2129	1.6280	1.3423	1.0777
beauty & spas	hotels & travel	1067	459	231	0.0036	0.0076	2.3246	4.6190	1.9870	0.4692
beauty & spas	nightlife	1576	661	599	0.0024	0.0098	2.3843	2.6311	1.1035	0.2478
education	arts & entertainment	214	70	212	0.0170	0.0233	3.0571	1.0094	0.3302	0.7285
education	event planning & services	169	68	159	0.0178	0.0193	2.4853	1.0629	0.4277	0.9254

source	target	user size	source item size	target item size	source density	target density	user to source item ratio	user to target item ratio	source to target item ratio	source to target density ratio
education	hotels & travel	155	59	117	0.0207	0.0235	2.6271	1.3248	0.5043	0.8798
education	local flavor	67	41	40	0.0328	0.0511	1.6341	1.6750	1.0250	0.6409
education	local services	142	54	113	0.0223	0.0149	2.6296	1.2566	0.4779	1.4972
education	public services & government	64	42	47	0.0316	0.0356	1.5238	1.3617	0.8936	0.8890
education	religious organizations	19	15	12	0.0772	0.0965	1.2667	1.5833	1.2500	0.8000
event planning & services	z active life	1034	330	441	0.0058	0.0055	3.1333	2.3447	0.7483	1.0556
event planning & services	arts & entertain- ment	1215	351	282	0.0053	0.0108	3.4615	4.3085	1.2447	0.4948
event planning & services	z automotive	475	250	387	0.0089	0.0048	1.9000	1.2274	0.6460	1.8685
event planning & services	beauty & spas	1167	303	501	0.0060	0.0033	3.8515	2.3293	0.6048	1.8425
event planning & services	z education	169	159	68	0.0193	0.0178	1.0629	2.4853	2.3382	1.0807
event planning & services	z food	2021	395	1481	0.0041	0.0041	5.1165	1.3646	0.2667	0.9886
event planning & services	z health & medical	350	228	298	0.0099	0.0051	1.5351	1.1745	0.7651	1.9457
event planning & services	z home services	336	207	243	0.0109	0.0061	1.6232	1.3827	0.8519	1.7821
event planning & services	z hotels & travel	4019	425	360	0.0032	0.0038	9.4565	11.1639	1.1806	0.8419
event planning & services	z local flavor	227	196	47	0.0149	0.0338	1.1582	4.8298	4.1702	0.4391
event planning & services	z local services	342	215	223	0.0113	0.0070	1.5907	1.5336	0.9641	1.6102
event planning & services	z nightlife	2043	394	611	0.0041	0.0090	5.1853	3.3437	0.6448	0.4569
event planning & services	z pets	295	211	183	0.0115	0.0086	1.3981	1.6120	1.1530	1.3336
event planning & services	public services & government	224	214	69	0.0137	0.0208	1.0467	3.2464	3.1014	0.6599
financial services	professional services	38	24	26	0.0493	0.0567	1.5833	1.4615	0.9231	0.8705
financial services	public services & government	26	24	26	0.0497	0.0577	1.0833	1.0000	0.9231	0.8611
food	active life	1891	1505	501	0.0045	0.0040	1.2565	3.7745	3.0040	1.1206
food	arts & entertain- ment	2395	1543	297	0.0041	0.0080	1.5522	8.0640	5.1953	0.5115
food	beauty & spas	1737	1451	680	0.0045	0.0023	1.1971	2.5544	2.1338	1.9162

source	target	user size	source item size	target item size	source density	target density	user to source item ratio	user to target item ratio	source to target item ratio	source to target density ratio
food	event planning & services	2021	1481	395	0.0041	0.0041	1.3646	5.1165	3.7494	1.0116
food	hotels & travel	1666	1454	316	0.0044	0.0053	1.1458	5.2722	4.6013	0.8341
food	nightlife	5292	1573	632	0.0026	0.0060	3.3643	8.3734	2.4889	0.4320
food	restaurants	10383	1614	4435	0.0017	0.0022	6.4331	2.3411	0.3639	0.7820
food	shopping	3253	1568	1619	0.0035	0.0020	2.0746	2.0093	0.9685	1.7436
health & medical	active life	471	322	371	0.0044	0.0072	1.4627	1.2695	0.8679	0.6125
health & medical	arts & entertain- ment	460	329	238	0.0043	0.0153	1.3982	1.9328	1.3824	0.2793
health & medical	beauty & spas	547	336	451	0.0040	0.0043	1.6280	1.2129	0.7450	0.9279
health & medical	event planning & services	350	298	228	0.0051	0.0099	1.1745	1.5351	1.3070	0.5139
health & medical	home services	237	237	203	0.0067	0.0074	1.0000	1.1675	1.1675	0.9074
health & medical	hotels & travel	293	260	157	0.0059	0.0136	1.1269	1.8662	1.6561	0.4312
health & medical	local services	233	232	190	0.0069	0.0083	1.0043	1.2263	1.2211	0.8302
health & medical	nightlife	706	398	534	0.0033	0.0127	1.7739	1.3221	0.7453	0.2609
home services	active life	377	249	369	0.0056	0.0082	1.5141	1.0217	0.6748	0.6840
home services	arts & entertain- ment	399	260	231	0.0055	0.0164	1.5346	1.7273	1.1255	0.3372
home services	event planning & services	336	243	207	0.0061	0.0109	1.3827	1.6232	1.1739	0.5611
home services	health & medical	237	203	237	0.0074	0.0067	1.1675	1.0000	0.8565	1.1021
home services	hotels & travel	321	235	151	0.0063	0.0138	1.3660	2.1258	1.5563	0.4533
home services	local services	276	209	210	0.0071	0.0074	1.3206	1.3143	0.9952	0.9581
home services	nightlife	648	333	527	0.0039	0.0135	1.9459	1.2296	0.6319	0.2891
home services	pets	188	177	145	0.0088	0.0112	1.0621	1.2966	1.2207	0.7844
home services	professional services	135	95	50	0.0162	0.0233	1.4211	2.7000	1.9000	0.6973
hotels & travel	active life	935	255	432	0.0072	0.0058	3.6667	2.1644	0.5903	1.2370
hotels & travel	arts & entertain- ment	1083	284	275	0.0066	0.0115	3.8134	3.9382	1.0327	0.5703
hotels & travel	automotive	424	183	361	0.0117	0.0053	2.3169	1.1745	0.5069	2.2297
hotels & travel	beauty & spas	1067	231	459	0.0076	0.0036	4.6190	2.3246	0.5033	2.1311
hotels & travel	education	155	117	59	0.0235	0.0207	1.3248	2.6271	1.9831	1.1366
hotels & travel	event planning & services	4019	360	425	0.0038	0.0032	11.1639	9.4565	0.8471	1.1878
hotels & travel	food	1666	316	1454	0.0053	0.0044	5.2722	1.1458	0.2173	1.1989
hotels & travel	health & medical	293	157	260	0.0136	0.0059	1.8662	1.1269	0.6038	2.3192
hotels & travel	home services	321	151	235	0.0138	0.0063	2.1258	1.3660	0.6426	2.2058
hotels & travel	local flavor	223	147	43	0.0178	0.0368	1.5170	5.1860	3.4186	0.4839

source	target	user size	source item size	target item size	source density	target density	user to source item ratio	user to target item ratio	source to target item ratio	source to target density ratio
hotels & travel	local services	303	154	209	0.0144	0.0078	1.9675	1.4498	0.7368	1.8574
hotels & travel	nightlife	1787	319	608	0.0052	0.0093	5.6019	2.9391	0.5247	0.5566
hotels & travel	pets	258	152	170	0.0146	0.0096	1.6974	1.5176	0.8941	1.5249
hotels & travel	public services & government	258	153	68	0.0159	0.0209	1.6863	3.7941	2.2500	0.7593
local flavor	arts & entertainment	309	47	237	0.0313	0.0217	6.5745	1.3038	0.1983	1.4416
local flavor	education	67	40	41	0.0511	0.0328	1.6750	1.6341	0.9756	1.5603
local flavor	event planning & services	227	47	196	0.0338	0.0149	4.8298	1.1582	0.2398	2.2775
local flavor	hotels & travel	223	43	147	0.0368	0.0178	5.1860	1.5170	0.2925	2.0664
local flavor	mass media	19	19	13	0.1302	0.1579	1.0000	1.4615	1.4615	0.8246
local flavor	pets	106	42	94	0.0429	0.0185	2.5238	1.1277	0.4468	2.3232
local flavor	public services & government	107	40	51	0.0416	0.0313	2.6750	2.0980	0.7843	1.3272
local services	active life	410	233	360	0.0064	0.0082	1.7597	1.1389	0.6472	0.7789
local services	arts & entertainment	451	244	247	0.0061	0.0161	1.8484	1.8259	0.9879	0.3800
local services	education	142	113	54	0.0149	0.0223	1.2566	2.6296	2.0926	0.6679
local services	event planning & services	342	223	215	0.0070	0.0113	1.5336	1.5907	1.0372	0.6210
local services	health & medical	233	190	232	0.0083	0.0069	1.2263	1.0043	0.8190	1.2046
local services	home services	276	210	209	0.0074	0.0071	1.3143	1.3206	1.0048	1.0438
local services	hotels & travel	303	209	154	0.0078	0.0144	1.4498	1.9675	1.3571	0.5384
local services	nightlife	667	273	539	0.0050	0.0147	2.4432	1.2375	0.5065	0.3425
local services	pets	185	172	131	0.0096	0.0120	1.0756	1.4122	1.3130	0.8063
mass media	local flavor	19	13	19	0.1579	0.1302	1.4615	1.0000	0.6842	1.2128
mass media	public services & government	18	13	18	0.1581	0.0864	1.3846	1.0000	0.7222	1.8297
nightlife	active life	1761	608	488	0.0102	0.0042	2.8964	3.6086	1.2459	2.4152
nightlife	arts & entertain- ment	2910	621	295	0.0083	0.0073	4.6860	9.8644	2.1051	1.1327
nightlife	automotive	1026	578	491	0.0117	0.0031	1.7751	2.0896	1.1772	3.7815
nightlife	beauty & spas	1576	599	661	0.0098	0.0024	2.6311	2.3843	0.9062	4.0358
nightlife	event planning & services	2043	611	394	0.0090	0.0041	3.3437	5.1853	1.5508	2.1885
nightlife	food	5292	632	1573	0.0060	0.0026	8.3734	3.3643	0.4018	2.3149
nightlife	health & medical	706	534	398	0.0127	0.0033	1.3221	1.7739	1.3417	3.8323
nightlife	home services	648	527	333	0.0135	0.0039	1.2296	1.9459	1.5826	3.4592
nightlife	hotels & travel	1787	608	319	0.0093	0.0052	2.9391	5.6019	1.9060	1.7966

source	target	user size	source item size	target item size	source density	target density	user to source item ratio	user to target item ratio	source to target item ratio	source to target density ratio
nightlife	local services	667	539	273	0.0147	0.0050	1.2375	2.4432	1.9744	2.9199
nightlife	pets	559	535	215	0.0140	0.0065	1.0449	2.6000	2.4884	2.1606
nightlife	restaurants	11013	640	4396	0.0039	0.0021	17.2078	2.5052	0.1456	1.8657
nightlife	shopping	2657	627	1597	0.0085	0.0022	4.2376	1.6637	0.3926	3.8539
pets	active life	343	184	338	0.0082	0.0092	1.8641	1.0148	0.5444	0.8850
pets	arts & entertainment	338	186	223	0.0081	0.0194	1.8172	1.5157	0.8341	0.4171
pets	event planning & services	295	183	211	0.0086	0.0115	1.6120	1.3981	0.8673	0.7499
pets	home services	188	145	177	0.0112	0.0088	1.2966	1.0621	0.8192	1.2748
pets	hotels & travel	258	170	152	0.0096	0.0146	1.5176	1.6974	1.1184	0.6558
pets	local flavor	106	94	42	0.0185	0.0429	1.1277	2.5238	2.2381	0.4304
pets	local services	185	131	172	0.0120	0.0096	1.4122	1.0756	0.7616	1.2403
pets	nightlife	559	215	535	0.0065	0.0140	2.6000	1.0449	0.4019	0.4628
professional services	financial services	38	26	24	0.0567	0.0493	1.4615	1.5833	1.0833	1.1487
professional services	home services	135	50	95	0.0233	0.0162	2.7000	1.4211	0.5263	1.4341
professional services	religious organizations	9	9	8	0.1111	0.1250	1.0000	1.1250	1.1250	0.8889
public services & government	arts & entertainment	284	70	238	0.0199	0.0206	4.0571	1.1933	0.2941	0.9665
public services & government	education	64	47	42	0.0356	0.0316	1.3617	1.5238	1.1190	1.1249
public services & government	event planning & services	224	69	214	0.0208	0.0137	3.2464	1.0467	0.3224	1.5154
public services & government	financial services	26	26	24	0.0577	0.0497	1.0000	1.0833	1.0833	1.1613
public services & government	hotels & travel	258	68	153	0.0209	0.0159	3.7941	1.6863	0.4444	1.3170
public services & government	local flavor	107	51	40	0.0313	0.0416	2.0980	2.6750	1.2750	0.7535
public services & government	mass media	18	18	13	0.0864	0.1581	1.0000	1.3846	1.3846	0.5465
religious organizations	education	19	12	15	0.0965	0.0772	1.5833	1.2667	0.8000	1.2500
religious organiza- tions	professional services	9	8	9	0.1250	0.1111	1.1250	1.0000	0.8889	1.1250
restaurants	food	10383	4435	1614	0.0022	0.0017	2.3411	6.4331	2.7478	1.2788
restaurants	nightlife	11013	4396	640	0.0021	0.0039	2.5052	17.2078	6.8688	0.5360
shopping	arts & entertainment	1729	1510	292	0.0030	0.0094	1.1450	5.9212	5.1712	0.3176

source	target	user size	source item size	target item size	source density	target density	user to source item ratio	user to target item ratio	source to target item ratio	source to target density ratio
shopping	food	3253	1619	1568	0.0020	0.0035	2.0093	2.0746	1.0325	0.5735
shopping	nightlife	2657	1597	627	0.0022	0.0085	1.6637	4.2376	2.5470	0.2595

Table 44: Domain ratings central tendency and dispersion statistics for the Yelp dataset

active life	arts & entertainment	3.9993	3.8701	4	4	4	4	1.1116	1.0776
active life	automotive	3.9902	3.7613	4	4	4	5	1.1254	1.8332
active life	beauty & spas	4.0450	4.0302	4	4	5	5	1.1098	1.3207
active life	event planning & services	4.0380	3.8652	4	4	5	4	1.0574	1.1496
active life	food	4.0079	3.9149	4	4	5	4	1.1644	1.0691
active life	health & medical	4.0184	4.1609	4	5	5	5	1.0837	1.5750
active life	home services	4.0026	3.7405	4	4	5	5	1.1400	2.0711
active life	hotels & travel	4.0414	3.7515	4	4	4	4	1.0359	1.2647
active life	local services	4.0173	3.9755	4	4	5	5	1.1085	1.5722
active life	nightlife	3.9900	3.6950	4	4	5	4	1.1866	1.1100
active life	pets	4.0094	4.3068	4	5	4	5	1.0617	1.0574
arts & entertainment	active life	3.8701	3.9993	4	4	4	4	1.0776	1.1116
arts & entertain- ment	automotive	3.8592	3.7469	4	4	4	5	1.0393	1.8526
arts & entertain- ment	beauty & spas	3.8685	3.9976	4	4	4	5	1.0753	1.2976
arts & entertain- ment	education	3.9233	4.0630	4	4	4	5	0.9865	1.3241
arts & entertain- ment	event planning & services	3.8782	3.8447	4	4	4	4	1.0284	1.1009
arts & entertain- ment	food	3.8724	3.9061	4	4	4	4	1.1205	1.0856
arts & entertainment	health & medical	3.8484	4.1005	4	5	4	5	1.0731	1.6075
arts & entertain- ment	home services	3.8495	3.6609	4	4	4	5	1.0513	2.1026
arts & entertain- ment	hotels & travel	3.8788	3.7227	4	4	4	4	1.0294	1.2784
arts & entertain- ment	local flavor	3.8463	4.0132	4	4	4	5	1.0136	1.4259
arts & entertainment	local services	3.8592	3.9717	4	4	4	5	1.0646	1.6072
arts & entertain- ment	nightlife	3.8650	3.7023	4	4	4	4	1.1625	1.1538
arts & entertain- ment	pets	3.8701	4.2888	4	5	4	5	1.0502	1.0956
arts & entertain- ment	public services & government	3.8938	3.8510	4	4	4	4	0.9830	1.3676
arts & entertain- ment	shopping	3.8935	3.8416	4	4	4	4	1.0853	1.2394
automotive	active life	3.7613	3.9902	4	4	5	4	1.8332	1.1254
automotive	arts & entertainment	3.7469	3.8592	4	4	5	4	1.8526	1.0393
automotive	beauty & spas	3.7654	4.0097	4	4	5	5	1.8088	1.3558

source	target	source mean rating	target mean rating	source median rating	target median rating	source mode rating	target mode rating	source var. rating	target var. rating
automotive	event planning & services	3.7019	3.8878	4	4	5	4	1.8199	1.0714
automotive	hotels & travel	3.6960	3.7179	4	4	5	4	1.8243	1.3566
automotive	nightlife	3.7251	3.6823	4	4	5	4	2.0401	1.1305
beauty & spas	active life	4.0302	4.0450	4	4	5	5	1.3207	1.1098
beauty & spas	arts & entertain- ment	3.9976	3.8685	4	4	5	4	1.2976	1.0753
beauty & spas	automotive	4.0097	3.7654	4	4	5	5	1.3558	1.8088
beauty & spas	event planning & services	4.0121	3.9007	4	4	5	4	1.2963	1.1893
beauty & spas	food	3.9985	3.8960	4	4	5	4	1.4671	1.1154
beauty & spas	health & medical	3.9588	4.1055	4	5	5	5	1.5713	1.8046
beauty & spas	hotels & travel	4.0086	3.8142	4	4	5	4	1.2611	1.2851
beauty & spas	nightlife	3.9996	3.6975	4	4	5	4	1.4311	1.1055
education	arts & entertain- ment	4.0630	3.9233	4	4	5	4	1.3241	0.9865
education	event planning & services	4.0683	3.9015	4	4	5	4	1.2600	1.1025
education	hotels & travel	4.0265	3.8075	4	4	5	4	1.3238	1.2052
education	local flavor	4.1444	4.1387	4	5	5	5	0.9789	1.1203
education	local services	3.8480	3.7322	4	4	5	5	1.8238	1.8524
education	public services & government	4.1882	3.9346	4	4	5	5	0.7261	1.2504
education	religious organiza- tions	3.6818	4.1364	4	5	5	5	1.9416	2.1234
event planning services	& active life	3.8652	4.0380	4	4	4	5	1.1496	1.0574
event planning services	& arts & entertain- ment	3.8447	3.8782	4	4	4	4	1.1009	1.0284
event planning services	& automotive	3.8878	3.7019	4	4	4	5	1.0714	1.8199
event planning services	& beauty & spas	3.9007	4.0121	4	4	4	5	1.1893	1.2963
event planning services	& education	3.9015	4.0683	4	4	4	5	1.1025	1.2600
event planning services	& food	3.8305	3.9021	4	4	4	4	1.2339	1.0697
event planning services	& health & medical	3.8935	4.0717	4	5	4	5	1.0902	1.6621
event planning services	& home services	3.8188	3.7550	4	4	4	5	1.2055	1.9479
event planning services	& hotels & travel	3.6913	3.6245	4	4	4	4	1.4393	1.5001

source		target	source mean rating	target mean rating	source median rating	target median rating	source mode rating	target mode rating	source var. rating	target var. rating
event planning services	&	local flavor	3.8971	4.0776	4	4	4	5	0.9561	1.2440
event planning services	&	local services	3.8987	3.9981	4	4	4	5	1.1636	1.6229
event planning services	&	nightlife	3.7981	3.6884	4	4	4	4	1.2178	1.0985
event planning services	&	pets	3.9007	4.3484	4	5	4	5	1.1680	1.0680
event planning services	&	public services & government	3.9439	3.8602	4	4	4	5	1.0531	1.4415
financial services		professional services	4.4667	4.4643	5	5	5	5	1.3909	1.4896
financial services		public services & government	3.9355	3.7436	4	4	5	4	1.3957	1.2483
food		active life	3.9149	4.0079	4	4	4	5	1.0691	1.1644
food		arts & entertainment	3.9061	3.8724	4	4	4	4	1.0856	1.1205
food		beauty & spas	3.8960	3.9985	4	4	4	5	1.1154	1.4671
food		event planning & services	3.9021	3.8305	4	4	4	4	1.0697	1.2339
food		hotels & travel	3.8938	3.6797	4	4	4	4	1.0434	1.3221
food		nightlife	3.9330	3.7179	4	4	4	4	1.1308	1.1948
food		restaurants	3.9416	3.7288	4	4	5	4	1.2375	1.2592
food		shopping	3.8978	3.8003	4	4	4	4	1.1573	1.4224
health & medical		active life	4.1609	4.0184	5	4	5	5	1.5750	1.0837
health & medical		arts & entertainment	4.1005	3.8484	5	4	5	4	1.6075	1.0731
health & medical		beauty & spas	4.1055	3.9588	5	4	5	5	1.8046	1.5713
health & medical		event planning & services	4.0717	3.8935	5	4	5	4	1.6621	1.0902
health & medical		home services	4.0693	3.7486	5	4	5	5	1.8348	2.0018
health & medical		hotels & travel	4.1432	3.7348	5	4	5	4	1.5086	1.3248
health & medical		local services	4.2102	4.0383	5	4	5	5	1.4908	1.4999
health & medical		nightlife	4.0892	3.6929	5	4	5	4	1.7888	1.1338
home services		active life	3.7405	4.0026	4	4	5	5	2.0711	1.1400
home services		arts & entertainment	3.6609	3.8495	4	4	5	4	2.1026	1.0513
home services		event planning & services	3.7550	3.8188	4	4	5	4	1.9479	1.2055
home services		health & medical	3.7486	4.0693	4	5	5	5	2.0018	1.8348
home services		hotels & travel	3.7352	3.6981	4	4	5	4	1.8936	1.3698
home services		local services	3.8683	3.9302	4	4	5	5	1.9826	1.8040
home services		nightlife	3.6726	3.6672	4	4	5	4	2.2799	1.1371

source	target	mean rating	target mean rating	source median rating	target median rating	mode rating	mode rating	source var. rating	target var. rating
home services	pets	3.7372	4.2778	4	5	5	5	2.1259	1.1587
home services	professional services	3.2548	3.2484	4	4	5	5	2.7705	3.1366
hotels & travel	active life	3.7515	4.0414	4	4	4	4	1.2647	1.0359
hotels & travel	arts & entertain- ment	3.7227	3.8788	4	4	4	4	1.2784	1.0294
hotels & travel	automotive	3.7179	3.6960	4	4	4	5	1.3566	1.8243
hotels & travel	beauty & spas	3.8142	4.0086	4	4	4	5	1.2851	1.2611
hotels & travel	education	3.8075	4.0265	4	4	4	5	1.2052	1.3238
hotels & travel	event planning & services	3.6245	3.6913	4	4	4	4	1.5001	1.4393
hotels & travel	food	3.6797	3.8938	4	4	4	4	1.3221	1.0434
hotels & travel	health & medical	3.7348	4.1432	4	5	4	5	1.3248	1.5086
hotels & travel	home services	3.6981	3.7352	4	4	4	5	1.3698	1.8936
hotels & travel	local flavor	3.7860	4.0567	4	4	4	5	1.0845	1.3150
hotels & travel	local services	3.7589	3.9817	4	4	4	5	1.3636	1.5446
hotels & travel	nightlife	3.6550	3.6691	4	4	4	4	1.3341	1.0996
hotels & travel	pets	3.7596	4.2922	4	5	4	5	1.2964	1.1787
hotels & travel	public services & government	3.7448	3.8229	4	4	4	5	1.2670	1.4467
local flavor	arts & entertain- ment	4.0132	3.8463	4	4	5	4	1.4259	1.0136
local flavor	education	4.1387	4.1444	5	4	5	5	1.1203	0.9789
local flavor	event planning & services	4.0776	3.8971	4	4	5	4	1.2440	0.9561
local flavor	hotels & travel	4.0567	3.7860	4	4	5	4	1.3150	1.0845
local flavor	mass media	4.2979	3.7436	5	4	5	5	1.0833	1.8799
local flavor	pets	4.0785	4.3533	4	5	5	5	1.2201	0.9947
local flavor	public services & government	4.1404	3.8772	4	4	5	4	1.0367	1.2025
local services	active life	3.9755	4.0173	4	4	5	5	1.5722	1.1085
local services	arts & entertain- ment	3.9717	3.8592	4	4	5	4	1.6072	1.0646
local services	education	3.7322	3.8480	4	4	5	5	1.8524	1.8238
local services	event planning & services	3.9981	3.8987	4	4	5	4	1.6229	1.1636
local services	health & medical	4.0383	4.2102	4	5	5	5	1.4999	1.4908
local services	home services	3.9302	3.8683	4	4	5	5	1.8040	1.9826
local services	hotels & travel	3.9817	3.7589	4	4	5	4	1.5446	1.3636
local services	nightlife	3.9771	3.6912	5	4	5	4	1.7827	1.0947
local services	pets	4.0554	4.3759	4	5	5	5	1.4969	1.0105
mass media	local flavor	3.7436	4.2979	4	5	5	5	1.8799	1.0833

source	target	source mean rating	target mean rating	source median rating	target median rating	source mode rating	target mode rating	source var. rating	target var. rating
mass media	public services & government	3.6486	4.1786	4	5	5	5	1.6231	1.1892
nightlife	active life	3.6950	3.9900	4	4	4	5	1.1100	1.1866
nightlife	arts & entertainment	3.7023	3.8650	4	4	4	4	1.1538	1.1625
nightlife	automotive	3.6823	3.7251	4	4	4	5	1.1305	2.0401
nightlife	beauty & spas	3.6975	3.9996	4	4	4	5	1.1055	1.4311
nightlife	event planning & services	3.6884	3.7981	4	4	4	4	1.0985	1.2178
nightlife	food	3.7179	3.9330	4	4	4	4	1.1948	1.1308
nightlife	health & medical	3.6929	4.0892	4	5	4	5	1.1338	1.7888
nightlife	home services	3.6672	3.6726	4	4	4	5	1.1371	2.2799
nightlife	hotels & travel	3.6691	3.6550	4	4	4	4	1.0996	1.334
nightlife	local services	3.6912	3.9771	4	5	4	5	1.0947	1.782
nightlife	pets	3.7004	4.3291	4	5	4	5	1.0889	1.1980
nightlife	restaurants	3.7118	3.7193	4	4	4	4	1.3226	1.260
nightlife	shopping	3.6950	3.8352	4	4	4	4	1.1530	1.345
pets	active life	4.3068	4.0094	5	4	5	4	1.0574	1.061
pets	arts & entertain- ment	4.2888	3.8701	5	4	5	4	1.0956	1.0502
pets	event planning & services	4.3484	3.9007	5	4	5	4	1.0680	1.1680
pets	home services	4.2778	3.7372	5	4	5	5	1.1587	2.1259
pets	hotels & travel	4.2922	3.7596	5	4	5	4	1.1787	1.296
pets	local flavor	4.3533	4.0785	5	4	5	5	0.9947	1.220
pets	local services	4.3759	4.0554	5	4	5	5	1.0105	1.4969
pets	nightlife	4.3291	3.7004	5	4	5	4	1.1980	1.0889
professional services	financial services	4.4643	4.4667	5	5	5	5	1.4896	1.390
professional services	home services	3.2484	3.2548	4	4	5	5	3.1366	2.770
professional services	religious organiza- tions	3.5556	3.8889	4	4	4	5	2.2778	1.861
public services & government	arts & entertain- ment	3.8510	3.8938	4	4	4	4	1.3676	0.9830
public services & government	education	3.9346	4.1882	4	4	5	5	1.2504	0.726
public services & government	event planning & services	3.8602	3.9439	4	4	5	4	1.4415	1.053
public services & government	financial services	3.7436	3.9355	4	4	4	5	1.2483	1.395
public services & government	hotels & travel	3.8229	3.7448	4	4	5	4	1.4467	1.2670
public services & government	local flavor	3.8772	4.1404	4	4	4	5	1.2025	1.036

source	target	source mean rating	target mean rating	source median rating	target median rating	source mode rating	target mode rating	source var. rating	target var. rating
public services & government	mass media	4.1786	3.6486	5	4	5	5	1.1892	1.6231
religious organiza- tions	education	4.1364	3.6818	5	4	5	5	2.1234	1.9416
religious organiza- tions	professional services	3.8889	3.5556	4	4	5	4	1.8611	2.2778
restaurants	food	3.7288	3.9416	4	4	4	5	1.2592	1.2375
restaurants	nightlife	3.7193	3.7118	4	4	4	4	1.2607	1.3226
shopping	arts & entertain- ment	3.8416	3.8935	4	4	4	4	1.2394	1.0853
shopping	food	3.8003	3.8978	4	4	4	4	1.4224	1.1573
shopping	nightlife	3.8352	3.6950	4	4	4	4	1.3455	1.1530

Table 45: Domain and domain-pair ratings dispersion statistics for the Yelp dataset

active life	arts & entertainment	0.0152	16.1565	13.4672	236.1682	3.7809	3.3882	-1.1092	-0.8987
active life	automotive	0.0658	19.2769	18.9300	274.5583	3.8610	2.5329	-1.1399	-0.8762
active life	beauty & spas	0.0132	15.5345	10.0235	263.4350	4.0319	3.5866	-1.2016	-1.1863
active life	event planning & services	0.0161	14.0212	1.3863	251.4691	3.8780	3.3261	-1.1255	-0.9247
active life	food	0.0151	18.5949	17.6753	189.7263	3.7882	3.3993	-1.1510	-0.9297
active life	health & medical	0.1289	14.9855	1.0986	288.1325	3.7984	4.0242	-1.1094	-1.4858
active life	home services	0.1171	16.4696	8.6643	286.6001	3.6460	2.2552	-1.0968	-0.8324
active life	hotels & travel	0.0390	15.8673	11.3780	265.3335	3.9831	3.1197	-1.1479	-0.8762
active life	local services	0.0435	16.6326	11.7639	286.5140	3.8040	3.1804	-1.1326	-1.1353
active life	nightlife	0.0708	19.4230	18.4273	191.6564	3.7462	3.0750	-1.1399	-0.7370
active life	pets	0.0918	15.0528	1.2040	282.6181	3.8263	5.5328	-1.1130	-1.7356
arts & entertainment	active life	0.0154	14.7327	6.0073	253.2545	3.3882	3.7809	-0.8987	-1.1092
arts & entertain- ment	automotive	0.1269	17.9118	17.3287	276.2130	3.2953	2.5456	-0.8415	-0.8849
arts & entertain- ment	beauty & spas	0.0419	16.4756	12.0712	266.4649	3.3399	3.4867	-0.8834	-1.1264
arts & entertain- ment	education	0.0780	12.9264	1.0986	285.6175	3.1947	3.8168	-0.7985	-1.2616
arts & entertainment	event planning & services	0.0012	14.5521	1.3863	263.7732	3.3800	3.3257	-0.8694	-0.8817
arts & entertain- ment	food	0.0009	16.6015	17.0104	192.8078	3.3423	3.3803	-0.9130	-0.9288
arts & entertainment	health & medical	0.2030	17.9341	17.3287	301.9238	3.3321	3.6804	-0.8611	-1.3702
arts & entertain- ment	home services	0.1909	17.6490	13.0267	289.9907	3.2936	2.1198	-0.8362	-0.7416
arts & entertainment	hotels & travel	0.0179	16.3186	12.0146	265.6131	3.3381	3.0719	-0.8539	-0.8507
arts & entertainment	local flavor	0.1077	10.2886	0.9163	230.4512	3.2627	3.3245	-0.7973	-1.1235
arts & entertainment	local services	0.1136	15.5878	1.3863	291.2517	3.3375	3.2013	-0.8586	-1.1459
arts & entertain- ment	nightlife	0.0174	11.8152	8.6219	161.1118	3.3751	3.0724	-0.9471	-0.7661
arts & entertainment	pets	0.1758	14.7571	1.6094	275.7562	3.4343	5.2751	-0.8943	-1.6796
arts & entertainment	public services & government	0.0415	15.6307	1.6094	283.3873	3.3265	3.3731	-0.8128	-1.0401
arts & entertainment	shopping	0.0043	15.1347	11.9281	215.6628	3.3628	3.1713	-0.9091	-0.9131
automotive	active life	0.0563	20.9979	23.3926	236.3300	2.5329	3.8610	-0.8762	-1.1399
automotive	$\begin{array}{ccc} \operatorname{arts} & \& & \operatorname{entertain-} \\ \operatorname{ment} & & \end{array}$	0.1003	21.3632	22.9305	213.5785	2.5456	3.2953	-0.8849	-0.8415
automotive	beauty & spas	0.0244	18.9409	18.0807	255.8627	2.6056	3.4492	-0.9031	-1.1477

source	target	total KL- divergence			variance user KL- divergence	${\rm Kurtosis}$	target Kurtosis rating	source skewness rating	target skewness rating
automotive	event planning & services	z 0.0736	22.0413	30.9317	239.7236	2.4665	3.5112	-0.8178	-0.9544
automotive	hotels & travel	0.0515	20.2143	22.9305	248.7309	2.4529	3.0372	-0.8078	-0.8947
automotive	nightlife	0.1816	22.9264	25.4902	168.2070	2.3487	3.0412	-0.8547	-0.7307
beauty & spas	active life	0.0128	16.9937	17.3287	247.6592	3.5866	4.0319	-1.1863	-1.2016
beauty & spas	arts & entertain ment	- 0.0412	19.5163	18.6737	221.5675	3.4867	3.3399	-1.1264	-0.8834
beauty & spas	automotive	0.0298	18.5620	17.6753	259.6304	3.4492	2.6056	-1.1477	-0.9031
beauty & spas	event planning & services	z 0.0189	11.1916	0.4055	217.6943	3.5301	3.2710	-1.1437	-0.9464
beauty & spas	food	0.0583	19.3782	18.5931	185.4296	3.3849	3.3452	-1.1701	-0.9312
beauty & spas	health & medical	0.0566	11.5541	0.6931	252.0274	3.1546	3.5436	-1.1094	-1.3908
beauty & spas	hotels & travel	0.0239	10.9762	0.3466	210.6334	3.5021	3.0313	-1.1163	-0.8736
beauty & spas	nightlife	0.1349	21.2422	22.7459	183.9480	3.4183	3.0779	-1.1682	-0.7427
education	arts & entertain ment	- 0.0730	19.6352	19.8058	202.1654	3.8168	3.1947	-1.2616	-0.7985
education	event planning & services	z 0.0477	23.6094	26.5129	183.0362	3.7562	3.4474	-1.2185	-0.9670
education	hotels & travel	0.0667	21.5271	23.3926	214.1862	3.7994	3.2858	-1.2282	-0.9386
education	local flavor	0.0332	22.1399	35.1761	239.9429	4.0502	3.2817	-1.2019	-1.0627
education	local services	0.0079	11.7629	0.0000	223.2304	2.7110	2.4909	-0.9724	-0.8505
education	public services & government	z 5.6969	20.3068	31.9864	284.9464	2.2458	3.3293	-0.6002	-1.0098
education	religious organiza tions	- 0.2824	14.2856	0.6931	306.5837	2.4914	3.5285	-0.8174	-1.4696
event planning services	& active life	0.0161	14.8659	8.6351	246.6920	3.3261	3.8780	-0.9247	-1.1255
event planning services	& arts & entertain ment	- 0.0011	17.0194	17.3287	236.6391	3.3257	3.3800	-0.8817	-0.8694
event planning services	& automotive	0.0900	21.2425	28.7067	259.8635	3.5112	2.4665	-0.9544	-0.8178
event planning services	& beauty & spas	0.0191	10.2032	0.3662	217.0283	3.2710	3.5301	-0.9464	-1.1437
event planning services	& education	0.0490	17.4596	1.7918	312.5803	3.4474	3.7562	-0.9670	-1.2185
event planning services	& food	0.0046	18.4615	17.6753	197.3122	3.1514	3.3826	-0.8903	-0.9144
event planning services	& health & medical	0.1660	20.2700	35.3505	292.3892	3.4032	3.5030	-0.9178	-1.3150
event planning services	& home services	0.1145	18.5833	17.6753	291.2655	3.3556	2.3086	-0.9529	-0.8247
event planning services	& hotels & travel	0.0015	1.8845	0.0000	40.7132	2.7269	2.5759	-0.7773	-0.7143

source	target	total KL- divergence			variance user KL- divergence	${\rm Kurtosis}$	target Kurtosis rating	source skewness rating	target skewness rating
event planning & services	z local flavor	0.0876	17.6478	17.3287	279.2561	3.2829	3.7287	-0.8054	-1.1997
event planning & services	z local services	0.0876	17.8281	17.5020	287.7133	3.4911	3.1969	-1.0053	-1.1628
event planning & services	z nightlife	0.0165	19.6571	19.7888	204.4376	3.0832	3.0659	-0.8441	-0.7244
event planning & services	z pets	0.1697	16.8326	11.3780	287.8458	3.4311	5.7889	-1.0013	-1.8249
event planning & services	z public services & government	0.0256	17.4523	17.3287	284.0684	3.6481	3.2124	-1.0023	-1.0279
financial services	professional services	1.9592	5.4405	0.0000	155.8866	7.0330	5.8000	-2.3154	-2.0961
financial services	public services & government	0.0639	29.5836	36.0437	178.2565	3.4489	3.6884	-1.1074	-1.0867
food	active life	0.0153	12.3180	1.0986	254.4170	3.3993	3.7882	-0.9297	-1.1510
food	arts & entertain- ment	0.0010	11.2891	0.9163	235.2941	3.3803	3.3423	-0.9288	-0.9130
food	beauty & spas	0.0599	12.6098	1.0986	259.9170	3.3452	3.3849	-0.9312	-1.1701
food	event planning & services	0.0051	12.2012	1.0986	256.7831	3.3826	3.1514	-0.9144	-0.8903
food	hotels & travel	0.0263	15.5777	1.7918	279.3756	3.3474	2.9343	-0.8863	-0.8064
food	nightlife	0.0252	13.7636	7.5602	221.9204	3.4238	3.0258	-0.9865	-0.7833
food	restaurants	0.0271	13.0855	11.6091	140.9268	3.4003	2.9082	-1.0425	-0.7785
food	shopping	0.0113	10.9036	0.9163	219.2576	3.2974	2.9588	-0.9413	-0.9092
health & medical	active life	0.1314	18.2738	17.6753	242.9194	4.0242	3.7984	-1.4858	-1.1094
health & medical	arts & entertain- ment	0.2122	23.6098	27.6414	188.1433	3.6804	3.3321	-1.3702	-0.8611
health & medical	beauty & spas	0.0624	14.4089	11.3780	234.8590	3.5436	3.1546	-1.3908	-1.1094
health & medical	event planning & services	0.1684	23.1405	35.2192	227.2406	3.5030	3.4032	-1.3150	-0.9178
health & medical	home services	0.0572	20.0403	23.6236	278.9314	3.3848	2.2705	-1.3282	-0.8178
health & medical	hotels & travel	0.1820	23.0971	34.9450	219.6363	3.8944	3.0310	-1.4153	-0.8755
health & medical	local services	0.0339	15.7537	11.3780	270.8026	4.4567	3.4694	-1.6018	-1.2289
health & medical	nightlife	0.3696	23.5183	25.9930	156.6763	3.5124	3.0177	-1.3691	-0.7193
home services	active life	0.0969	20.6191	22.9305	224.4585	2.2552	3.6460	-0.8324	-1.0968
home services	arts & entertain- ment	0.1631	23.2382	26.4704	187.9973	2.1198	3.2936	-0.7416	-0.8362
home services	event planning & services	0.1147	21.5849	25.9930	238.3209	2.3086	3.3556	-0.8247	-0.9529
home services	health & medical	0.0511	19.3770	22.9305	292.3334	2.2705	3.3848	-0.8178	-1.3282
home services	hotels & travel	0.0754	21.3677	23.3926	234.7059	2.3427	2.8987	-0.8186	-0.8436
home services	local services	0.0037	14.7965	1.0986	273.8873	2.5516	2.7959	-0.9810	-1.0459
home services	nightlife	0.2763	24.3710	27.3668	156.6582	2.0237	3.0186	-0.7453	-0.7202

source	target	total KL- divergenc			variance user KL- divergence	${\rm Kurtosis}$	target Kurtosis rating	source skewness rating	target skewness rating
home services	pets	0.0847	16.4521	14.5266	276.1422	2.2082	5.0859	-0.8193	-1.6590
home services	professional services	0.0316	2.0158	0.0000	65.1544	1.4162	1.2720	-0.3138	-0.2686
hotels & travel	active life	0.0383	16.9877	17.3287	252.3528	3.1197	3.9831	-0.8762	-1.1479
hotels & travel	arts & entertainment	0.0147	18.6178	17.6753	231.4209	3.0719	3.3381	-0.8507	-0.8539
hotels & travel	automotive	0.0517	19.3896	18.2670	263.9217	3.0372	2.4529	-0.8947	-0.8078
hotels & travel	beauty & spas	0.0247	9.7326	0.2877	211.5293	3.0313	3.5021	-0.8736	-1.1163
hotels & travel	education	0.0667	17.1626	1.6094	309.0994	3.2858	3.7994	-0.9386	-1.2282
hotels & travel	event planning & services	0.0015	1.6047	0.0000	36.6861	2.5759	2.7269	-0.7143	-0.7773
hotels & travel	food	0.0218	21.1512	22.9305	192.8912	2.9343	3.3474	-0.8064	-0.8863
hotels & travel	health & medical	0.1884	20.3504	35.3505	288.5156	3.0310	3.8944	-0.8755	-1.4153
hotels & travel	home services	0.0751	18.7845	18.0807	285.7877	2.8987	2.3427	-0.8436	-0.8186
hotels & travel	local flavor	0.1228	19.8497	18.7150	281.5169	3.4412	3.5307	-0.8958	-1.1636
hotels & travel	local services	0.0744	18.6095	18.0218	277.4827	3.0104	3.1434	-0.9000	-1.1083
hotels & travel	nightlife	0.0120	20.2786	21.3691	203.5635	2.8102	3.0307	-0.7519	-0.7073
hotels & travel	pets	0.2148	18.5573	18.0218	287.8745	3.1371	5.3546	-0.9115	-1.7387
hotels & travel	public services & government	0.0213	14.2976	1.3863	271.4928	3.0233	3.0492	-0.8389	-0.9491
local flavor	arts & entertainment	0.1030	17.9789	17.3287	172.8263	3.3245	3.2627	-1.1235	-0.7973
local flavor	education	0.0351	19.6478	36.0437	307.4457	3.2817	4.0502	-1.0627	-1.2019
local flavor	event planning & services	0.0829	21.1874	23.3926	217.8478	3.7287	3.2829	-1.1997	-0.8054
local flavor	hotels & travel	0.1156	22.6334	27.1636	217.8553	3.5307	3.4412	-1.1636	-0.8958
local flavor	mass media	0.1710	12.4552	7.1007	212.1137	4.2211	2.3783	-1.4378	-0.8315
local flavor	pets	0.0597	18.0972	17.3287	291.8155	3.5969	5.0360	-1.1422	-1.6460
local flavor	public services & government	0.0512	16.7442	17.3287	268.0685	3.9401	3.6412	-1.1852	-1.0441
local services	active life	0.0417	20.2114	20.7622	223.7674	3.1804	3.8040	-1.1353	-1.1326
local services	arts & entertainment	0.1102	21.3030	21.5530	193.6949	3.2013	3.3375	-1.1459	-0.8586
local services	education	0.0080	9.1866	0.0000	229.1951	2.4909	2.7110	-0.8505	-0.9724
local services	event planning & services	0.0879	21.2249	23.6236	231.2368	3.1969	3.4911	-1.1628	-1.0053
local services	health & medical	0.0312	14.9776	1.0986	279.5438	3.4694	4.4567	-1.2289	-1.6018
local services	home services	0.0038	15.2654	7.3551	268.7982	2.7959	2.5516	-1.0459	-0.9810
local services	hotels & travel	0.0721	20.7716	22.9305	238.1435	3.1434	3.0104	-1.1083	-0.9000
local services	nightlife	0.2591	22.4416	24.6197	153.4333	3.0581	3.1309	-1.1616	-0.7460
local services	pets	0.0476	14.4732	0.9364	260.7341	3.4832	6.3152	-1.2424	-1.9099

source		target	total KL- divergenc			variance user KL- divergence	${\rm Kurtosis}$	target Kurtosis rating	source skewness rating	target skewness rating
mass media		local flavor	0.1387	12.5339	5.5567	217.0714		4.2211	-0.8315	-1.4378
mass media		public services & government		21.4680	26.3257	263.8726		3.8321	-0.5421	-1.2321
nightlife		active life	0.0741	13.2852	1.3083	262.1594	3.0750	3.7462	-0.7370	-1.1399
nightlife		arts & entertainment	0.0180	6.4847	0.5233	153.0407	3.0724	3.3751	-0.7661	-0.9471
nightlife		automotive	0.1983	15.6377	1.7918	288.0214	3.0412	2.3487	-0.7307	-0.8547
nightlife		beauty & spas	0.1422	14.9697	1.6094	277.9625	3.0779	3.4183	-0.7427	-1.1682
nightlife		event planning & services	0.0174	14.0930	1.3863	273.4589	3.0659	3.0832	-0.7244	-0.8441
nightlife		food	0.0260	13.7288	7.6144	220.7040	3.0258	3.4238	-0.7833	-0.9865
nightlife		health & medical	0.3548	14.7964	1.6094	292.3288	3.0177	3.5124	-0.7193	-1.3691
nightlife		home services	0.2859	16.2536	1.9459	298.0849	3.0186	2.0237	-0.7202	-0.7453
nightlife		hotels & travel	0.0128	15.0443	1.7047	272.9551	3.0307	2.8102	-0.7073	-0.7519
nightlife		local services	0.2669	12.9002	1.3863	271.1494	3.1309	3.0581	-0.7460	-1.1616
nightlife		pets	0.3940	12.7763	1.3863	268.6771	3.1359	5.5664	-0.7474	-1.8289
nightlife		restaurants	0.0012	10.2608	8.4486	111.2599	2.9164	2.9072	-0.8100	-0.7753
nightlife		shopping	0.0337	14.2092	4.6575	241.7667	3.0274	3.0938	-0.7455	-0.9356
pets		active life	0.0951	18.9861	17.6753	225.0063	5.5328	3.8263	-1.7356	-1.1130
pets		arts & entertain- ment	0.1780	21.8856	22.9305	171.9909	5.2751	3.4343	-1.6796	-0.8943
pets		event planning & services	0.1706	19.9114	19.4444	233.8959	5.7889	3.4311	-1.8249	-1.0013
pets		home services	0.1091	16.7041	14.8155	274.5974	5.0859	2.2082	-1.6590	-0.8193
pets		hotels & travel	0.2091	21.7151	24.5246	224.5803	5.3546	3.1371	-1.7387	-0.9115
pets		local flavor	0.0702	19.3500	17.6753	268.4746	5.0360	3.5969	-1.6460	-1.1422
pets		local services	0.0608	14.7480	5.1836	258.6983	6.3152	3.4832	-1.9099	-1.2424
pets		nightlife	0.3926	22.3406	23.5163	155.9775	5.5664	3.1359	-1.8289	-0.7474
professional se	er-	financial services	0.0993	5.9782	0.0000	158.6266	5.8000	7.0330	-2.0961	-2.3154
professional se vices	er-	home services	0.0350	4.8200	0.0000	102.0316	1.2720	1.4162	-0.2686	-0.3138
professional se vices	er-	religious organiza- tions	8.2015	24.0291	36.0437	324.7862	1.8306	3.1260	-0.5752	-1.0457
public services government	&	arts & entertain- ment	0.0325	21.6146	23.3207	187.6150	3.3731	3.3265	-1.0401	-0.8128
public services government	&	education	0.2489	19.9075	27.4909	294.6180	3.3293	2.2458	-1.0098	-0.6002
public services government		event planning & services	0.0213	21.8168	23.3926	205.9713	3.2124	3.6481	-1.0279	-1.0023
public services government	&	financial services	0.0685	28.5679	36.0437	208.8340	3.6884	3.4489	-1.0867	-1.1074

source	target	total KL- divergence			variance user KL- divergence	Kurtosis	target Kurtosis rating	source skewness rating	target skewness rating
public services & government	hotels & travel	0.0208	18.2281	17.3287	229.4528	3.0492	3.0233	-0.9491	-0.8389
public services & government	local flavor	0.0508	15.5181	1.3863	280.8956	3.6412	3.9401	-1.0441	-1.1852
public services & government	mass media	0.2347	22.2018	26.4708	235.5339	3.8321	2.0721	-1.2321	-0.5421
religious organiza- tions	education	6.7125	15.4954	0.6931	301.6879	3.5285	2.4914	-1.4696	-0.8174
religious organiza- tions	professional services	8.2030	24.0291	36.0437	324.7862	3.1260	1.8306	-1.0457	-0.5752
restaurants	food	0.0277	5.3245	0.5952	128.6955	2.9082	3.4003	-0.7785	-1.0425
restaurants	nightlife	0.0013	2.2455	0.3964	52.2595	2.9072	2.9164	-0.7753	-0.8100
shopping	arts & entertainment	0.0039	13.0087	1.4469	232.0976	3.1713	3.3628	-0.9131	-0.9091
shopping	food	0.0096	14.5273	11.3969	199.4479	2.9588	3.2974	-0.9092	-0.9413
shopping	nightlife	0.0324	17.0565	17.3287	211.1177	3.0938	3.0274	-0.9356	-0.7455

Table 46: Domain-pair CCA statistics for the Yelp dataset

active life	arts & entertainment	0.1315	0.0319	0.0000	0.4294	0.9476	0.9321	251	125
active life	automotive	0.1018	0.0265	0.0000	0.3907	0.9395	0.9225	226	113
active life	beauty & spas	0.0810	0.0211	0.0000	0.3508	0.9286	0.9161	284	143
active life	event planning & services	0.0992	0.0165	0.0000	0.3779	0.9385	0.9182	242	124
active life	food	0.2401	0.0932	0.0210	0.5351	0.9754	0.9661	429	321
active life	health & medical	0.0966	0.0138	0.0000	0.3806	0.9297	0.8931	145	69
active life	home services	0.0949	0.0146	0.0000	0.4035	0.9409	0.8984	137	66
active life	hotels & travel	0.0796	0.0100	0.0000	0.3559	0.9201	0.8925	201	105
active life	local services	0.1029	0.0147	0.0000	0.3800	0.9241	0.8985	136	66
active life	nightlife	0.1408	0.0453	0.0048	0.4154	0.9637	0.9477	419	222
active life	pets	0.1313	0.0404	0.0000	0.4007	0.9235	0.9102	99	48
arts & entertainment	active life	0.0784	0.0157	0.0000	0.3874	0.9443	0.9214	255	139
arts & entertainment	automotive	0.0682	0.0000	0.0000	0.3640	0.8936	0.8782	220	112
arts & entertainment	beauty & spas	0.0542	0.0042	0.0000	0.3565	0.9072	0.8862	240	134
arts & entertainment	education	0.1458	0.0000	0.0000	0.4812	0.8988	0.8626	48	25
arts & entertainment	event planning & services	0.0474	0.0000	0.0000	0.3037	0.8954	0.8753	253	115
arts & entertainment	food	0.2125	0.0513	0.0037	0.6021	0.9555	0.9452	273	250
arts & entertainment	health & medical	0.0556	0.0000	0.0000	0.2976	0.8994	0.8714	162	73
arts & entertainment	home services	0.0719	0.0000	0.0000	0.3637	0.8968	0.8767	153	75
arts & entertainment	hotels & travel	0.0267	0.0000	0.0000	0.2809	0.8782	0.8371	225	104
arts & entertainment	local flavor	0.2250	0.0500	0.0000	0.5569	0.9221	0.8826	40	22
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	local services	0.0714	0.0065	0.0000	0.3604	0.9063	0.8828	154	75
arts & entertainment	nightlife	0.1455	0.0291	0.0036	0.4970	0.9523	0.9326	275	190
arts & entertainment	pets	0.0943	0.0189	0.0000	0.3700	0.9260	0.8963	106	52
arts & entertainment	public services & government	0.1343	0.0149	0.0000	0.4996	0.9116	0.8785	67	38
arts & entertainment	shopping	0.2169	0.0625	0.0074	0.5776	0.9630	0.9485	272	229
automotive	active life	0.1266	0.0306	0.0000	0.4068	0.9439	0.9242	229	114
automotive	arts & entertainment	0.1493	0.0362	0.0000	0.4109	0.9383	0.9249	221	100
automotive	beauty & spas	0.1128	0.0205	0.0000	0.4042	0.9466	0.9166	195	106

$ \geq 0.80 \geq 0.90 \geq 0.95 \text{correlation} \text{ponent components tion} \text{ponent correlation} \text{ponents correlation} \text$	# significant correlations 85 194 139 112
services automotive hotels & travel 0.1259 0.0296 0.0000 0.4339 0.9316 0.9134 135 6 automotive nightlife 0.1831 0.0710 0.0109 0.4395 0.9619 0.9551 366 1 beauty & spas active life 0.1025 0.0247 0.0000 0.3693 0.9408 0.9271 283 1 beauty & spas arts & entertain- 0.1345 0.0336 0.0000 0.4037 0.9373 0.9266 238 1	55 194 139 112
automotive nightlife 0.1831 0.0710 0.0109 0.4395 0.9619 0.9551 366 1 beauty & spas active life 0.1025 0.0247 0.0000 0.3693 0.9408 0.9271 283 1 beauty & spas arts & entertain- 0.1345 0.0336 0.0000 0.4037 0.9373 0.9266 238 1	194 139 112
beauty & spas active life 0.1025 0.0247 0.0000 0.3693 0.9408 0.9271 283 1 beauty & spas arts & entertain- 0.1345 0.0336 0.0000 0.4037 0.9373 0.9266 238 1	139 112 101
beauty & spas arts & entertain- 0.1345 0.0336 0.0000 0.4037 0.9373 0.9266 238 1	112
·	101
beauty & spas automotive 0.1379 0.0197 0.0000 0.3979 0.9285 0.9084 203 1	
beauty & spas event planning & 0.0977 0.0140 0.0000 0.3694 0.9246 0.9079 215 services	109
beauty & spas food 0.2364 0.0970 0.0263 0.4964 0.9777 0.9714 495 3	332
beauty & spas	71
beauty & spas hotels & travel 0.0898 0.0120 0.0000 0.3620 0.9137 0.8926 167 8	37
beauty & spas $$ nightlife $$ 0.1263 $$ 0.0450 $$ 0.0064 $$ 0.3626 $$ 0.9707 $$ 0.9551 $$ 467	215
education arts & entertain- 0.1837 0.0408 0.0000 0.5303 0.9422 0.8918 49 ment	37
education event planning & 0.1163 0.0465 0.0000 0.4580 0.9184 0.8650 43 services	28
education hotels & travel 0.0513 0.0000 0.0000 0.4165 0.8930 0.7884 39	24
education local flavor 0.0690 0.0000 0.0000 0.3288 0.8365 0.7577 29	13
education local services 0.0606 0.0000 0.0000 0.4365 0.8823 0.8015 33	19
education public services & 0.0714 0.0000 0.0000 0.3544 0.8605 0.7756 28 government	13
education religious organiza- 0.2500 0.1250 0.1250 0.4531 0.9655 0.6675 8 tions	3
event planning & active life $0.0816 0.0122 0.0000 0.3703 0.9349 0.9073 245 1$ services	133
event planning & arts & entertain- 0.0723 0.0080 0.0000 0.3412 0.9109 0.8925 249 services ment	117
event planning & automotive $0.0726 - 0.0056 - 0.0000 - 0.3936 - 0.9071 - 0.8821 - 179$ services	96
event planning & beauty & spas 0.0594 0.0046 0.0000 0.3436 0.9178 0.8842 219 services	122
event planning & education $0.0714 0.0000 0.0000 0.4241 0.8595 0.8189 42$ services	22
event planning & food 0.1831 0.0640 0.0145 0.5036 0.9684 0.9598 344 2 services	261
event planning & health & medical 0.0873 0.0079 0.0000 0.3643 0.9031 0.8760 126 services	63
event planning & home services 0.0732 0.0163 0.0000 0.3728 0.9439 0.8870 123 services	52
event planning & hotels & travel 0.2931 0.0977 0.0086 0.5694 0.9668 0.9550 348 1 services	183

source	target	CCA ≥ 0.80	CCA ≥ 0.90	CCA ≥ 0.95	average correla- tion	first component correlation	first 5 compo- nents correla- tion	# components	# signifi- cant cor- relations
event planning & services	c local flavor	0.1750	0.0250	0.0000	0.4942	0.9104	0.8651	40	21
event planning & services	c local services	0.1157	0.0248	0.0000	0.4114	0.9292	0.9015	121	65
event planning & services	nightlife	0.0912	0.0147	0.0000	0.3786	0.9423	0.9201	340	194
event planning & services	pets	0.1222	0.0222	0.0000	0.3790	0.9405	0.9010	90	43
event planning & services	public services & government	0.1270	0.0317	0.0000	0.4558	0.9205	0.8932	63	33
financial services	professional services	0.3000	0.1000	0.0000	0.4328	0.9397	0.7414	10	2
financial services	public services & government	0.0714	0.0000	0.0000	0.3494	0.8242	0.6419	14	7
food	active life	0.2278	0.0839	0.0096	0.5062	0.9656	0.9564	417	222
food	arts & entertainment	0.3223	0.1136	0.0110	0.6227	0.9593	0.9518	273	145
food	beauty & spas	0.1777	0.0661	0.0083	0.4565	0.9629	0.9543	484	259
food	event planning & services	0.1780	0.0475	0.0030	0.4824	0.9600	0.9444	337	185
food	hotels & travel	0.1877	0.0578	0.0108	0.4961	0.9596	0.9505	277	145
food	nightlife	0.1922	0.0549	0.0048	0.5150	0.9633	0.9540	619	357
food	restaurants	0.3481	0.1753	0.0627	0.6302	0.9890	0.9855	1580	1291
food	shopping	0.2013	0.0939	0.0294	0.4377	0.9812	0.9770	1257	625
health & medical	active life	0.1074	0.0201	0.0000	0.4239	0.9378	0.9136	149	79
health & medical	arts & entertainment	0.1098	0.0305	0.0000	0.3783	0.9403	0.9206	164	75
health & medical	beauty & spas	0.1484	0.0516	0.0000	0.4345	0.9404	0.9298	155	86
health & medical	event planning & services	0.0880	0.0160	0.0000	0.3911	0.9144	0.8928	125	63
health & medical	home services	0.1149	0.0230	0.0000	0.4424	0.9421	0.8983	87	40
health & medical	hotels & travel	0.0808	0.0101	0.0000	0.4024	0.9053	0.8698	99	48
health & medical	local services	0.1014	0.0145	0.0000	0.3936	0.9225	0.8743	69	27
health & medical	nightlife	0.1842	0.0746	0.0175	0.4655	0.9793	0.9642	228	134
home services	active life	0.1216	0.0203	0.0000	0.4075	0.9407	0.9103	148	77
home services	arts & entertainment	0.1203	0.0253	0.0000	0.3899	0.9308	0.9107	158	76
home services	event planning & services	0.0952	0.0159	0.0000	0.3876	0.9183	0.8847	126	61
home services	health & medical	0.1222	0.0222	0.0000	0.4195	0.9155	0.8948	90	43
home services	hotels & travel	0.0982	0.0179	0.0000	0.3961	0.9143	0.8940	112	53

source	target	CCA ≥ 0.80	CCA ≥ 0.90	CCA ≥ 0.95	average correla- tion	first component correlation	first 5 compo- nents correla- tion	# components	# signifi- cant cor- relations
home services	local services	0.1667	0.0444	0.0000	0.4380	0.9435	0.9172	90	40
home services	nightlife	0.2192	0.0959	0.0183	0.4789	0.9768	0.9594	219	130
home services	pets	0.1127	0.0141	0.0000	0.3773	0.9078	0.8841	71	30
home services	professional ser- vices	0.3226	0.1290	0.0323	0.5927	0.9536	0.9210	31	10
hotels & travel	active life	0.0686	0.0049	0.0000	0.3470	0.9089	0.8894	204	114
hotels & travel	arts & entertain- ment	0.0437	0.0044	0.0000	0.3023	0.9083	0.8715	229	107
hotels & travel	automotive	0.0685	0.0000	0.0000	0.3812	0.8870	0.8681	146	79
hotels & travel	beauty & spas	0.0359	0.0000	0.0000	0.3342	0.8863	0.8388	167	100
hotels & travel	education	0.0256	0.0000	0.0000	0.3944	0.8334	0.7773	39	18
hotels & travel	event planning & services	0.2849	0.0940	0.0114	0.5591	0.9703	0.9573	351	198
hotels & travel	food	0.1748	0.0629	0.0070	0.4970	0.9614	0.9477	286	221
hotels & travel	health & medical	0.0891	0.0099	0.0000	0.3626	0.9063	0.8718	101	51
hotels & travel	home services	0.0531	0.0088	0.0000	0.3463	0.9073	0.8573	113	57
hotels & travel	local flavor	0.0789	0.0000	0.0000	0.4279	0.8705	0.8083	38	22
hotels & travel	local services	0.0796	0.0000	0.0000	0.3576	0.8848	0.8588	113	55
hotels & travel	nightlife	0.0821	0.0107	0.0000	0.3755	0.9371	0.9138	280	170
hotels & travel	pets	0.0976	0.0244	0.0000	0.3410	0.9359	0.8930	82	38
hotels & travel	public services & government	0.0615	0.0000	0.0000	0.4032	0.8856	0.8318	65	34
local flavor	arts & entertain- ment	0.1500	0.0250	0.0000	0.5438	0.9182	0.8595	40	35
local flavor	education	0.0370	0.0000	0.0000	0.2965	0.8172	0.6948	27	12
local flavor	event planning & services	0.0250	0.0000	0.0000	0.4432	0.8149	0.7551	40	31
local flavor	hotels & travel	0.0270	0.0000	0.0000	0.3946	0.8142	0.7368	37	27
local flavor	mass media	0.1818	0.0909	0.0000	0.4271	0.9323	0.7481	11	4
local flavor	pets	0.0909	0.0000	0.0000	0.3698	0.8654	0.8105	33	17
local flavor	public services & government	0.0333	0.0000	0.0000	0.4136	0.8316	0.7625	30	17
local services	active life	0.0922	0.0142	0.0000	0.3661	0.9205	0.8953	141	76
local services	arts & entertain- ment	0.1125	0.0188	0.0000	0.3724	0.9202	0.9043	160	77
local services	education	0.1471	0.0294	0.0000	0.4143	0.9101	0.8588	34	12
local services	event planning & services	0.1066	0.0164	0.0000	0.3914	0.9225	0.8973	122	63
local services	health & medical	0.0704	0.0141	0.0000	0.3566	0.9239	0.8605	71	34
local services	home services	0.1398	0.0538	0.0108	0.4116	0.9577	0.9285	93	44

source		target	CCA ≥ 0.80	CCA ≥ 0.90	CCA ≥ 0.95	average correla- tion	first component correlation	first 5 compo- nents correla- tion	# components	# signifi- cant cor- relations
local services		hotels & travel	0.0893	0.0000	0.0000	0.3568	0.8989	0.8788	112	52
local services		nightlife	0.2188	0.1042	0.0260	0.5171	0.9705	0.9600	192	130
local services		pets	0.0833	0.0167	0.0000	0.3528	0.9039	0.8573	60	26
mass media		local flavor	0.1818	0.0909	0.0000	0.4186	0.9151	0.7011	11	5
mass media		public services & government	0.2222	0.1111	0.0000	0.4604	0.9485	0.7399	9	4
nightlife		active life	0.0909	0.0172	0.0000	0.3730	0.9339	0.9222	407	206
nightlife		arts & entertainment	0.1397	0.0331	0.0000	0.4785	0.9423	0.9303	272	157
nightlife		automotive	0.1121	0.0259	0.0000	0.3947	0.9391	0.9283	348	177
nightlife		beauty & spas	0.0632	0.0087	0.0000	0.3154	0.9277	0.9110	459	214
nightlife		event planning & services	0.0640	0.0061	0.0000	0.3497	0.9173	0.8988	328	176
nightlife		food	0.1234	0.0321	0.0000	0.4727	0.9441	0.9371	624	427
nightlife		health & medical	0.1075	0.0187	0.0000	0.3950	0.9480	0.9157	214	116
nightlife		home services	0.1553	0.0388	0.0097	0.4559	0.9595	0.9414	206	108
nightlife		hotels & travel	0.0693	0.0073	0.0000	0.3522	0.9238	0.8996	274	149
nightlife		local services	0.1514	0.0432	0.0000	0.4629	0.9376	0.9250	185	91
nightlife		pets	0.1832	0.0611	0.0076	0.4652	0.9582	0.9330	131	68
nightlife		restaurants	0.4535	0.1953	0.0488	0.7280	0.9821	0.9748	635	634
nightlife		shopping	0.1442	0.0373	0.0049	0.4490	0.9602	0.9523	617	386
pets		active life	0.1132	0.0189	0.0000	0.4266	0.9260	0.8876	106	65
pets		arts & entertainment	0.1261	0.0360	0.0000	0.4327	0.9402	0.9139	111	62
pets		event planning & services	0.0851	0.0000	0.0000	0.3939	0.8913	0.8642	94	50
pets		home services	0.0986	0.0141	0.0000	0.3984	0.9134	0.8731	71	36
pets		hotels & travel	0.0805	0.0000	0.0000	0.3455	0.8870	0.8601	87	41
pets		local flavor	0.0606	0.0000	0.0000	0.3945	0.8866	0.8006	33	13
pets		local services	0.1563	0.0156	0.0000	0.3770	0.9161	0.8886	64	29
pets		nightlife	0.2500	0.0956	0.0221	0.5590	0.9639	0.9503	136	101
professional vices	ser-	financial services	0.3000	0.1000	0.1000	0.4052	0.9791	0.7552	10	1
professional vices	ser-	home services	0.2581	0.0645	0.0000	0.5810	0.9284	0.8919	31	19
professional vices	ser-	religious organiza- tions	0.1667	0.1667	0.1667	0.4368	0.9718	0.5210	6	1
public services government	s &	arts & entertainment	0.1493	0.0149	0.0000	0.5248	0.9089	0.8865	67	51
public services government	s &	education	0.0370	0.0000	0.0000	0.3266	0.8449	0.7494	27	11

Domain-pair CCA statistics for the Yelp dataset contd.

source	target	CCA ≥ 0.80	CCA ≥ 0.90	CCA ≥ 0.95	average correla- tion	first component correlation	first 5 compo- nents correla- tion	# components	# significant correlations
public services & government	event planning & services	0.0462	0.0000	0.0000	0.4290	0.8748	0.8200	65	44
public services & government	financial services	0.1429	0.0000	0.0000	0.3886	0.8983	0.7530	14	5
public services & government	hotels & travel	0.0462	0.0000	0.0000	0.3842	0.8473	0.8075	65	38
public services & government	local flavor	0.1333	0.0333	0.0000	0.4135	0.9136	0.8443	30	16
public services & government	mass media	0.1111	0.0000	0.0000	0.4486	0.8498	0.6603	9	4
religious organizations	education	0.1429	0.0000	0.0000	0.3985	0.8799	0.5090	7	3
religious organiza- tions	professional services	0.2000	0.0000	0.0000	0.4982	0.8488	0.4982	5	0
restaurants	food	0.3178	0.1544	0.0491	0.5860	0.9843	0.9803	1548	876
restaurants	nightlife	0.5039	0.2512	0.0742	0.7248	0.9823	0.9790	633	325
shopping	arts & entertainment	0.3371	0.1386	0.0262	0.6204	0.9653	0.9602	267	105
shopping	food	0.2309	0.1136	0.0373	0.4540	0.9829	0.9791	1312	641
shopping	nightlife	0.2579	0.1157	0.0298	0.5245	0.9759	0.9715	605	292

B.2 ERROR OF ALGORITHMS ON DOMAIN PAIRS IN YELP DATASET

Table 47: RMSE and MAE for domain-pairs in the Yelp dataset

active life	arts & entertainment	0.9597	1.1231	1.1006	1.2369	1.3288	0.3359	0.8487	0.8707	0.9501	0.8584
active life	automotive	1.3184	1.4675	1.4657	1.6373	2.4854	0.4628	1.1178	1.1234	1.4491	0.9882
active life	beauty $\&$ spas	1.1563	1.2795	1.2789	1.6409	1.1135	0.3920	2.0695	1.5714	1.4531	0.8540
active life	event planning & services	1.0464	1.1831	1.1786	1.5126	1.1153	0.3629	0.9300	0.9346	1.2976	0.8448
active life	food	1.0078	1.0937	1.1056	0.9600	0.8794	0.3441	0.8473	0.8446	0.6695	0.6778
active life	health & medical	1.2836	1.3276	1.3572	1.8555	1.2761	0.4222	0.8891	0.8811	1.7216	1.0075
active life	home services	1.3080	1.6100	1.5434	1.6926	1.2301	0.4724	1.2287	1.1909	1.5255	0.8620
active life	hotels & travel	1.1138	1.2294	1.1881	1.5058	1.4115	0.3819	0.9250	0.9416	1.3104	0.7453
active life	local services	1.3236	1.3931	1.3777	1.6966	1.8572	0.4470	1.0037	0.9841	1.5260	0.9790
active life	nightlife	0.9928	1.1116	1.0973	0.9297	0.9357	0.3451	0.8779	0.8723	0.6580	0.7257
active life	pets	1.0687	1.0441	1.0674	1.8683	1.2105	0.3389	0.7185	0.6934	1.7405	0.8441
arts & entertainment	active life	0.9728	1.0788	1.1296	1.4353	0.9757	0.3390	0.8296	0.8738	1.1784	0.7429
arts & entertainment	automotive	1.3198	1.4290	1.4036	1.6033	1.1628	0.4585	1.0684	1.0796	1.4048	0.9231
arts & entertainment	beauty & spas	1.1532	1.2839	1.2879	1.6605	1.1543	0.3884	1.1631	0.9329	1.4802	0.8927
arts & entertainment	education	1.2148	1.3480	1.2943	1.8419	0.9880	0.4322	0.9147	0.8962	1.7459	0.6462
arts & entertainment	event planning & services	1.0155	1.1087	1.1430	1.5024	1.8565	0.3494	0.8463	0.9171	1.2916	0.6768
arts & entertainment	food	1.0077	1.0872	1.1010	0.9701	0.9516	0.3439	0.8365	0.8628	0.6797	0.7345
arts & entertainment	health & medical	1.3595	1.3723	1.4337	1.8318	1.3540	0.4530	1.0052	0.9564	1.6956	0.9711
arts & entertainment	home services	1.4175	1.5835	1.5711	1.6272	1.2427	0.5175	1.2359	1.2388	1.4470	0.9120
arts & entertainment	hotels & travel	1.0863	1.1968	1.2052	1.4732	1.3889	0.3781	0.9093	0.9331	1.2626	0.7530
arts & entertain- ment	local flavor	0.8945	1.1951	1.2583	1.6829	0.5908	0.3197	0.9287	0.9279	1.4986	0.4332
arts & entertainment	local services	1.3193	1.3097	1.3792	1.7231	1.0994	0.4480	0.9821	0.9721	1.5541	0.8223
arts & entertainment	nightlife	0.9952	1.1372	1.1399	0.9860	0.9949	0.3445	1.9882	1.9217	0.7064	0.7561
arts & entertainment	pets	1.0932	1.1035	1.1543	1.8441	1.0401	0.3491	0.9999	0.7794	1.7186	0.7898
arts & entertainment	public services & government	1.1259	1.3190	1.3217	1.6354	0.8619	0.3799	0.9744	0.9464	1.4800	0.6069
arts & entertainment	shopping	1.0680	1.1460	1.1803	1.1220	1.2663	0.3610	0.8949	0.9107	0.8352	0.7875

 RMSE and MAE for domain-pairs in the Yelp dataset contd.

source	target	CCA RMSE	CD- SVD RMSE	SD- SVD RMSE	RMGM RMSE	CMF RMSE	CCA MAE	CD- SVD MAE	SD- SVD MAE	RMGM MAE	CMF MAE
automotive	active life	0.9996	1.1571	1.1885	1.4168	0.8863	0.3441	0.8878	0.9050	1.1592	0.6605
automotive	arts & entertain- ment	0.9818	1.1114	1.1149	1.1966	0.7677	0.3431	0.8763	0.8783	0.9179	0.5951
automotive	beauty & spas	1.2485	1.2239	1.2801	1.6929	1.9018	0.4162	0.9225	0.9203	1.5297	1.0101
automotive	event planning & services	0.9906	1.0752	1.1551	1.4164	1.5786	0.3412	0.8438	0.8737	1.1805	0.8015
automotive	hotels & travel	1.1315	1.3655	1.3842	1.4018	1.1693	0.3901	0.9671	1.0023	1.1756	0.9071
automotive	nightlife	1.0242	1.1533	1.1596	0.9156	0.8698	0.3561	1.9969	1.9969	0.6471	0.6715
beauty & spas	active life	1.0253	1.1809	1.1751	1.4339	1.0114	0.3508	1.9758	1.7631	1.1683	0.7726
beauty & spas	arts & entertain- ment	0.9882	1.2183	1.2092	1.2233	0.8260	0.3424	0.9216	0.9178	0.9389	0.6191
beauty & spas	automotive	1.3401	1.4506	1.4450	1.5971	2.1354	0.4648	1.1115	1.1093	1.4035	1.0305
beauty & spas	event planning & services	1.0803	1.1622	1.1666	1.5713	1.3069	0.3703	0.9011	0.9201	1.3743	0.7306
beauty & spas	food	1.0237	1.1211	1.1247	0.9808	0.8094	0.3499	0.8738	0.8799	0.6921	0.6233
beauty & spas	health & medical	1.3647	1.4518	1.4659	1.8508	1.5539	0.4636	0.9640	0.9591	1.7126	0.9962
beauty & spas	hotels & travel	1.0709	1.1799	1.1827	1.5831	1.3405	0.3713	0.9046	0.9192	1.4028	0.6019
beauty & spas	nightlife	0.9995	1.2656	1.2504	0.9418	0.8776	0.3454	0.9430	0.9321	0.6721	0.6799
education	arts & entertain- ment	0.9522	1.1460	1.1650	1.1095	0.8209	0.3251	0.9121	0.9139	0.8244	0.6201
education	event planning & services	1.0348	1.1010	1.0778	1.4302	1.4236	0.3546	0.8858	0.8786	1.2074	0.9884
education	hotels & travel	1.0487	1.1869	1.1336	1.4902	1.0684	0.3698	0.9152	0.9079	1.2820	0.8124
education	local flavor	0.8850	1.1634	1.1654	1.6383	0.6630	0.3190	0.8211	0.8554	1.4711	0.5265
education	local services	1.3724	1.5285	1.5040	1.6624	2.2257	0.4995	1.1898	1.2092	1.5194	1.2536
education	public services & government	1.1954	1.4926	1.4492	1.5820	1.1611	0.4215	1.0251	1.0277	1.3915	0.9176
education	religious organiza- tions	1.0699	0.7701	0.7680	2.0679	1.2557	0.4098	0.6705	0.6135	2.0065	1.0890
event planning services	& active life	0.9357	1.0721	1.1312	1.4507	0.9875	0.3257	0.8376	0.8507	1.2009	0.7460
event planning services	& arts & entertain- ment	0.9304	1.0566	1.0751	1.2368	0.9527	0.3191	0.8175	0.8275	0.9518	0.6997
event planning services	& automotive	1.3165	1.4113	1.4262	1.5234	8.0580	0.4666	1.0985	1.1174	1.3181	1.9342
event planning services	& beauty & spas	1.1378	1.1782	1.2166	1.6743	1.0954	0.3891	0.9093	0.9258	1.5055	0.8018
event planning services	& education	1.1115	1.2287	1.2475	1.7908	1.0777	0.3921	0.8578	0.9421	1.6730	0.8289
event planning services	& food	1.0024	1.0895	1.1083	0.9723	0.9266	0.3417	0.8403	0.8502	0.6820	0.7137
event planning services	& health & medical	1.3762	1.3025	1.3511	1.7959	1.1360	0.4576	0.9651	0.9363	1.6528	0.9165

 RMSE and MAE for domain-pairs in the Yelp dataset contd.

source	target	CCA RMSE	CD- SVD RMSE	SD- SVD RMSE	RMGM RMSE	CMF RMSE	CCA MAE	CD- SVD MAE	SD- SVD MAE	RMGM MAE	CMF MAE
event planning d	& home services	1.3984	1.6203	1.6012	1.6774	2.1187	0.5038	2.1060	1.4656	1.5157	1.1500
event planning a services	& hotels & travel	1.1037	1.2480	1.2681	1.5874	1.0394	0.3916	0.9848	0.9911	1.4298	0.7247
event planning a services	& local flavor	0.8565	1.1704	1.2161	1.6782	0.8818	0.3007	0.9029	0.9399	1.5063	0.5103
event planning of services	& local services	1.2664	1.2694	1.2943	1.7359	1.2399	0.4369	2.0979	1.5720	1.5624	0.9150
event planning of services	& nightlife	0.9899	1.0998	1.1147	0.9538	1.0406	0.3434	0.8597	0.8698	0.6786	0.8181
event planning of services	& pets	1.0151	1.0471	1.0991	1.8254	1.0593	0.3249	0.7300	0.6470	1.6696	0.7791
event planning of services	& public services & government	1.1623	1.3601	1.3871	1.6277	0.9349	0.3839	0.9527	1.0119	1.4531	0.6975
financial services	professional services	0.9415	0.8848	0.8888	2.0885	1.0712	0.3225	0.5372	0.5257	2.0268	0.7155
financial services	public services & government	nan	1.6876	1.6554	nan	nan	nan	0.9791	0.9047	nan	nan
food	active life	0.9906	1.1035	1.1493	1.5095	0.9797	0.3412	0.8376	0.8774	1.2667	0.7502
food	arts & entertain- ment	0.9550	1.0437	1.0893	1.3808	1.1854	0.3349	0.8202	0.8454	1.1175	0.6539
food	beauty & spas	1.2189	1.2276	1.3159	1.6846	0.9998	0.4132	0.9342	0.9526	1.5079	0.7666
food	event planning & services	1.0420	1.1497	1.1830	1.5642	1.3116	0.3618	0.8841	0.9236	1.3784	0.6785
food	hotels & travel	1.0849	1.2175	1.2226	1.5144	1.3180	0.3755	1.5607	0.9761	1.3320	0.6764
food	nightlife	1.0104	1.2556	1.2489	1.1407	3.2806	0.3502	2.0056	2.0056	0.8562	0.8894
food	restaurants	1.0740	1.1647	1.1635	0.8048	1.3621	0.3703	0.9146	0.9153	0.5598	0.8172
food	shopping	1.1405	1.2257	1.2485	1.2262	1.0591	0.3897	0.9387	0.9662	0.9389	0.8329
health & medical	active life	1.0203	1.1825	1.1565	1.4163	0.9302	0.3504	0.8957	0.8836	1.1538	0.6826
health & medical	arts & entertain- ment	0.9822	1.2633	1.2151	1.2021	0.7332	0.3424	0.8894	0.8934	0.9205	0.5596
health & medical	beauty & spas	1.3063	1.3298	1.3365	1.6416	1.1730	0.4411	0.9745	0.9749	1.4418	0.9011
health & medical	event planning & services	1.0649	1.1822	1.2052	1.5025	0.9656	0.3688	0.9206	0.9137	1.2860	0.7029
health & medical	home services	1.3740	1.5394	1.4995	1.6978	1.3562	0.5064	1.1355	1.2148	1.5394	1.1272
health & medical	hotels & travel	1.1238	1.2756	1.1767	1.5249	1.8405	0.3880	0.9887	0.9459	1.3406	0.8000
health & medical	local services	1.2814	1.3454	1.3898	1.8110	1.3223	0.4253	0.9428	0.9465	1.6796	1.0612
health & medical	nightlife	1.0411	1.1630	1.1631	0.9345	0.8119	0.3621	0.9730	0.9811	0.6623	0.6330
home services	active life	1.0277	1.1443	1.1663	1.3820	0.9898	0.3538	0.8729	0.9118	1.1136	0.7253
home services	arts & entertain- ment	0.9692	1.0846	1.1060	1.2233	0.7805	0.3338	0.8783	0.8867	0.9412	0.6050
home services	event planning & services	1.0830	1.2416	1.3295	1.4366	1.2280	0.3726	1.8063	1.5279	1.2117	0.7195

 RMSE and MAE for domain-pairs in the Yelp dataset contd.

source	target	CCA RMSE	CD- SVD RMSE	SD- SVD RMSE	RMGM RMSE	CMF RMSE	CCA MAE	CD- SVD MAE	SD- SVD MAE	RMGM MAE	CMF MAE
home services	health & medical	1.4840	1.4120	1.5547	1.7915	1.4781	0.5105	1.0289	1.0437	1.6400	1.2528
home services	hotels & travel	1.1398	1.2246	1.2311	1.4717	1.2088	0.3903	0.9801	0.9547	1.2713	0.7916
home services	local services	1.2935	1.4292	1.4325	1.7531	1.3400	0.4558	1.0268	1.0024	1.6058	1.0669
home services	nightlife	1.0663	1.2618	1.2695	0.8826	0.8670	0.3700	1.9864	1.9864	0.6277	0.6764
home services	pets	1.3037	1.2323	1.2445	1.7856	1.1222	0.4231	0.8051	0.8455	1.6413	0.8447
home services	professional services	1.6791	1.8771	1.8859	1.6276	0.9716	0.6612	1.5792	1.6054	1.4349	0.7811
hotels & travel	active life	0.9886	1.0815	1.1608	1.4026	1.8883	0.3394	0.8497	0.8746	1.1386	0.7242
hotels & travel	arts & entertain- ment	0.9386	1.0506	1.1052	1.2375	0.9457	0.3288	0.8366	0.8651	0.9514	0.7177
hotels & travel	automotive	1.3212	1.5675	1.5734	1.5820	1.6153	0.4677	1.1411	1.1465	1.4065	1.1032
hotels & travel	beauty & spas	1.1305	1.1480	1.2324	1.6805	1.7435	0.3813	0.8874	0.9249	1.5143	0.8541
hotels & travel	education	1.1876	1.2162	1.2739	1.7652	0.8588	0.4042	0.9402	0.9660	1.6323	0.6072
hotels & travel	event planning & services	1.0998	1.2240	1.2563	1.5823	1.0875	0.3896	0.9632	0.9971	1.4172	0.7549
hotels & travel	food	0.9999	1.0888	1.1162	0.9703	0.8995	0.3411	1.5087	0.9003	0.6838	0.7049
hotels & travel	health & medical	1.3278	1.3261	1.4130	1.7767	1.3141	0.4494	0.9663	0.9129	1.6211	0.9531
hotels & travel	home services	1.3209	1.4280	1.4987	1.6620	1.1125	0.4770	1.1381	1.1182	1.5023	0.9059
hotels & travel	local flavor	0.9177	1.2108	1.2359	1.6659	0.8704	0.3219	0.9094	0.9218	1.4946	0.6184
hotels & travel	local services	1.2533	1.2744	1.3401	1.6809	1.6728	0.4171	0.9617	0.9795	1.5075	0.9263
hotels & travel	nightlife	0.9870	1.0796	1.0942	0.9378	1.0745	0.3428	0.8468	0.8753	0.6681	0.8456
hotels & travel	pets	1.1931	1.1974	1.2243	1.8269	1.1148	0.3846	0.9249	0.7960	1.6776	0.8225
hotels & travel	public services & government	1.1799	1.2765	1.2888	1.6328	0.8503	0.4097	1.1699	1.0968	1.4700	0.6573
local flavor	arts & entertain- ment	0.9485	1.1059	1.0835	1.0405	0.8045	0.3303	0.8427	0.8604	0.7526	0.6184
local flavor	education	1.0328	1.1061	1.0632	1.8235	0.8217	0.3592	0.7563	0.7247	1.7131	0.6400
local flavor	event planning & services	0.9466	1.1056	1.1101	1.4569	1.0293	0.3246	0.9087	0.8748	1.2408	0.7584
local flavor	hotels & travel	1.0298	1.1692	1.1343	1.4457	1.0220	0.3510	0.8900	0.9495	1.2527	0.7683
local flavor	mass media	1.2381	1.2613	1.4176	1.5768	1.2267	0.4481	0.9703	0.9910	1.3894	1.0937
local flavor	pets	0.9813	1.0773	1.0875	1.8641	1.6895	0.3351	0.6566	0.6965	1.7263	0.8933
local flavor	public services & government	1.0544	1.2767	1.2206	1.6984	1.7611	0.3504	0.9610	0.9283	1.5803	0.9958
local services	active life	1.0148	1.1265	1.1729	1.3740	0.9769	0.3514	0.8711	0.8966	1.1060	0.7229
local services	arts & entertain- ment	0.9910	1.1075	1.1108	1.1786	0.7913	0.3410	0.8929	0.8903	0.8923	0.6088
local services	education	1.3073	1.3845	1.3757	1.7335	0.8844	0.4726	1.0261	1.0194	1.5851	0.6842
local services	event planning & services	1.0842	1.2030	1.1857	1.4705	0.8957	0.3697	1.9847	1.9816	1.2379	0.6633
local services	health & medical	1.2779	1.2585	1.2985	1.8968	1.0867	0.4244	0.7883	0.8142	1.7758	0.8823

 RMSE and MAE for domain-pairs in the Yelp dataset contd.

source	target	CCA RMSE	CD- SVD RMSE	SD- SVD RMSE	RMGM RMSE	CMF RMSE	CCA MAE	CD- SVD MAE	SD- SVD MAE	RMGM MAE	CMF MAE
local services	home services	1.3550	1.5605	1.5737	1.7302	2.9252	0.4758	1.2003	1.1822	1.5659	1.3186
local services	hotels & travel	1.1527	1.3120	1.2582	1.5036	7.0090	0.3987	1.0110	0.9963	1.3063	1.3024
local services	nightlife	1.0143	1.1292	1.1093	0.8861	0.8213	0.3533	0.8781	0.8788	0.6235	0.6432
local services	pets	1.0954	1.1223	1.1672	1.8203	1.5735	0.3623	0.7068	0.6961	1.6562	0.9083
mass media	local flavor	1.0835	1.0144	1.0363	1.6173	1.1060	0.4069	0.8843	0.7022	1.3986	0.9527
mass media	public services & government	0.9660	1.2034	1.4046	1.8621	1.0068	0.3469	1.2600	1.0851	1.8125	0.8803
nightlife	active life	0.9911	1.0878	1.1610	1.4749	0.9275	0.3435	0.8417	0.8970	1.2333	0.6990
nightlife	arts & entertainment	0.9894	1.1139	1.1453	1.3915	1.1792	0.3452	2.0129	1.8353	1.1329	0.5548
nightlife	automotive	1.3588	1.4917	1.5197	1.6415	1.0218	0.4698	2.0137	1.7052	1.4543	0.7873
nightlife	beauty & spas	1.2058	1.3708	1.3363	1.6860	1.0331	0.4084	1.0049	0.9539	1.5083	0.7810
nightlife	event planning & services	1.0489	1.1270	1.1893	1.5610	1.6780	0.3656	0.8700	0.9332	1.3831	0.5992
nightlife	food	1.0124	1.1921	1.2323	1.1348	1.2246	0.3475	2.0324	2.0312	0.8314	0.8717
nightlife	health & medical	1.3849	1.4264	1.4528	1.8264	1.1645	0.4610	1.1259	0.9828	1.6796	0.8691
nightlife	home services	1.4286	1.7171	1.6776	1.6989	1.5219	0.5163	2.1176	1.6466	1.5328	1.0140
nightlife	hotels & travel	1.0775	1.1701	1.1969	1.5088	3.9908	0.3747	0.9096	0.9678	1.3275	0.7230
nightlife	local services	1.3294	1.3387	1.4111	1.7464	1.4236	0.4489	1.0453	1.0317	1.5909	0.7823
nightlife	pets	1.0737	1.1745	1.1546	1.8809	0.9330	0.3479	0.8909	0.6839	1.7501	0.6781
nightlife	restaurants	1.0707	1.1444	1.1612	0.7992	1.2232	0.3724	0.8991	0.9125	0.5578	0.7780
nightlife	shopping	1.1062	1.1649	1.2185	1.2009	1.1053	0.3747	0.9112	0.9457	0.9156	0.8565
pets	active life	1.0193	1.1510	1.1466	1.3749	1.2093	0.3478	0.8810	0.8927	1.1103	0.8471
pets	arts & entertainment	0.9369	1.1790	1.1361	1.0823	0.7266	0.3271	0.8947	0.9211	0.7920	0.5544
pets	event planning & services	1.0691	1.2750	1.1880	1.3965	1.0543	0.3677	0.9565	0.9612	1.1415	0.7731
pets	home services	1.5615	1.7300	1.6722	1.6607	1.3713	0.5748	1.2943	1.2846	1.4827	1.0487
pets	hotels & travel	1.1082	1.3098	1.2074	1.4217	0.9515	0.3809	1.0013	1.0124	1.2002	0.6958
pets	local flavor	0.8504	1.1893	1.1327	1.7307	0.7924	0.3150	0.8693	0.8546	1.5836	0.6068
pets	local services	1.2527	1.4258	1.4034	1.7608	1.2150	0.4267	0.9876	0.9861	1.6138	1.0097
pets	nightlife	1.0189	1.1281	1.0948	0.9407	0.8372	0.3498	0.8952	0.8504	0.6711	0.6511
professional services	financial services	0.9745	0.9269	0.9719	2.1008	0.7411	0.3194	0.4849	0.4889	2.0500	0.5196
professional services	home services	1.6797	1.7640	1.8521	1.5645	2.2404	0.6522	1.5261	1.5653	1.3707	1.3153
professional services	religious organizations	nan	0.8873	0.6747	nan	nan	nan	0.9792	1.1618	nan	nan
public services & government	arts & entertainment	0.9512	1.1804	1.1912	1.0547	0.9123	0.3373	0.9074	0.9191	0.7603	0.6983
public services & government	education	0.8932	1.0645	0.9430	1.9223	1.0481	0.3179	0.6890	0.6459	1.8739	0.8670

 RMSE and MAE for domain-pairs in the Yelp dataset contd.

source	target	CCA RMSE	CD- SVD RMSE	SD- SVD RMSE	RMGM RMSE	CMF RMSE	CCA MAE	CD- SVD MAE	SD- SVD MAE	RMGM MAE	CMF MAE
public services & government	event planning & services	1.0835	1.2594	1.3068	1.4268	1.0866	0.3757	0.9109	0.9542	1.1906	0.8351
public services & government	financial services	1.2015	1.0398	1.2670	1.7537	1.2650	0.4502	0.9116	0.9084	1.6658	1.1557
public services & government	hotels & travel	1.0867	1.1848	1.2052	1.4248	1.1364	0.3853	1.1436	1.0917	1.2197	0.8611
public services & government	local flavor	0.9090	1.1286	1.2048	1.6823	0.8675	0.3230	0.8247	0.8795	1.5260	0.6772
public services & government	mass media	nan	1.5091	1.5893	nan	nan	nan	1.1619	1.2104	nan	nan
religious organiza- tions	education	1.3924	1.6810	1.5882	1.7111	5.0885	0.5074	1.1963	1.4445	1.6025	3.3215
religious organiza- tions	professional services	1.4449	0.8288	0.6279	1.8179	1.4915	0.6115	0.8975	0.9419	1.7590	1.4793
restaurants	food	1.0543	1.1137	1.1616	1.2997	1.0723	0.3625	0.8636	0.8846	1.0073	0.7643
restaurants	nightlife	1.0697	1.1484	1.1733	1.2975	1.8423	0.3748	0.8990	0.9188	1.0301	0.7662
shopping	arts & entertainment	0.9643	1.0702	1.1035	1.3083	1.2578	0.3343	0.8422	0.8427	1.0333	0.7224
shopping	food	1.0369	1.1108	1.1405	1.0342	0.8487	0.3577	0.8667	0.8917	0.7397	0.6453
shopping	nightlife	1.0084	1.1100	1.1122	0.9749	1.0953	0.3506	0.8724	0.8920	0.7002	0.7376

B.3 COLD-START ANALYSIS OF DOMAIN PAIRS FOR YELP DATASET

B.3.1 MAEs for Target User Profiles

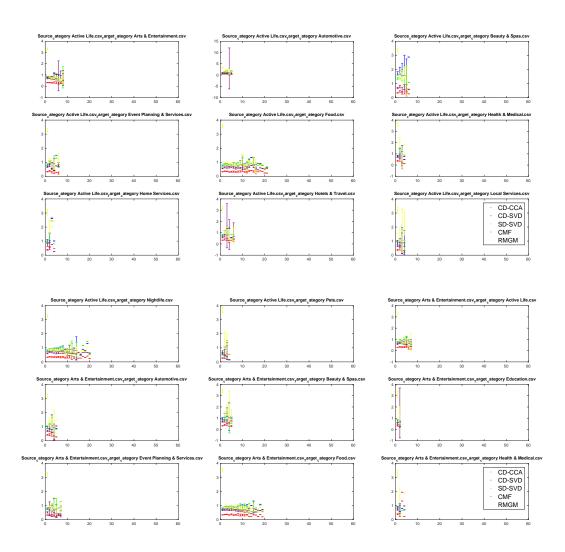


Figure 74: User-based MAE of algorithms in the Yelp dataset, averaged on each domain-pair and sorted based on the users' target domain profile size

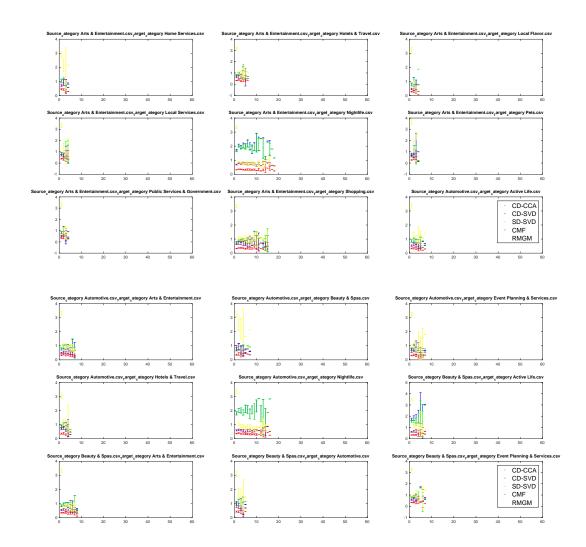


Figure 74: User-based MAE of algorithms in the Yelp dataset, averaged on each domain-pair and sorted based on the users' target domain profile size for domain pairs 19 to 36

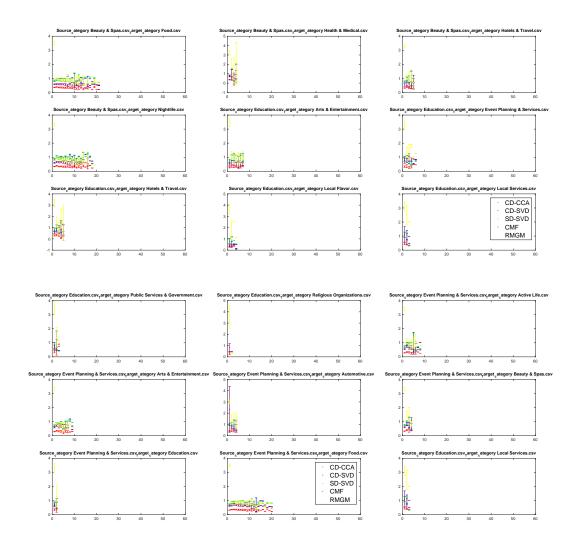


Figure 74: User-based MAE of algorithms in the Yelp dataset, averaged on each domain-pair and sorted based on the users' target domain profile size for domain pairs 37 to 53

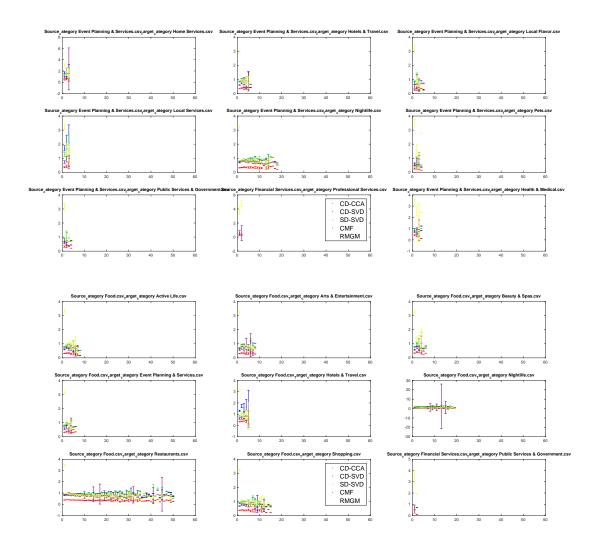


Figure 74: User-based MAE of algorithms in the Yelp dataset, averaged on each domain-pair and sorted based on the users' target domain profile size for domain pairs 54 to 71

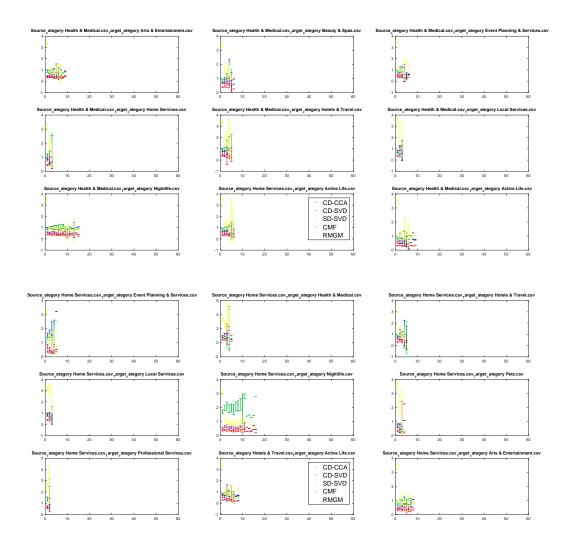


Figure 74: User-based MAE of algorithms in the Yelp dataset, averaged on each domain-pair and sorted based on the users' target domain profile size for domain pairs 72 to 89

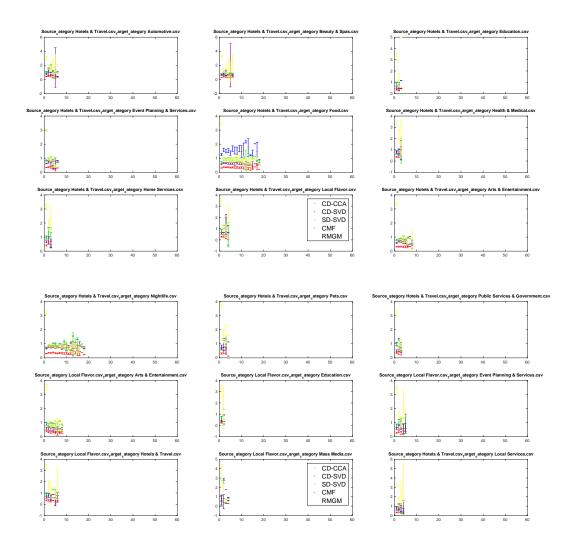


Figure 74: User-based MAE of algorithms in the Yelp dataset, averaged on each domain-pair and sorted based on the users' target domain profile size for domain pairs 90 to 107

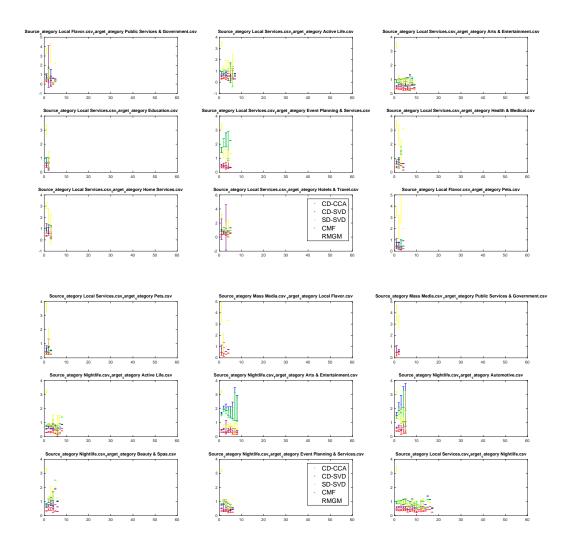


Figure 74: User-based MAE of algorithms in the Yelp dataset, averaged on each domain-pair and sorted based on the users' target domain profile size for domain pairs 108 to 125

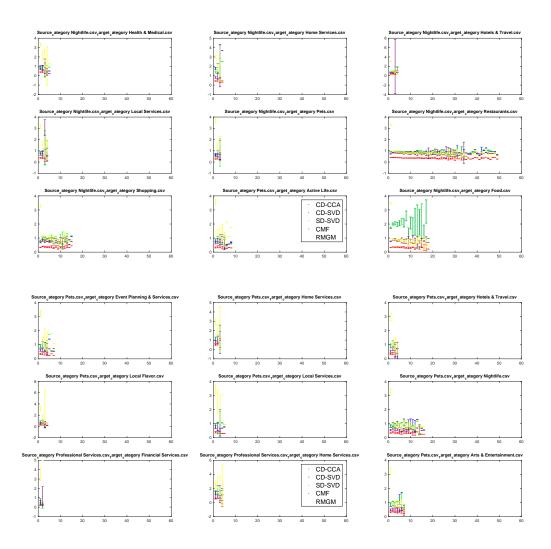


Figure 74: User-based MAE of algorithms in the Yelp dataset, averaged on each domain-pair and sorted based on the users' target domain profile size for domain pairs 126 to 143

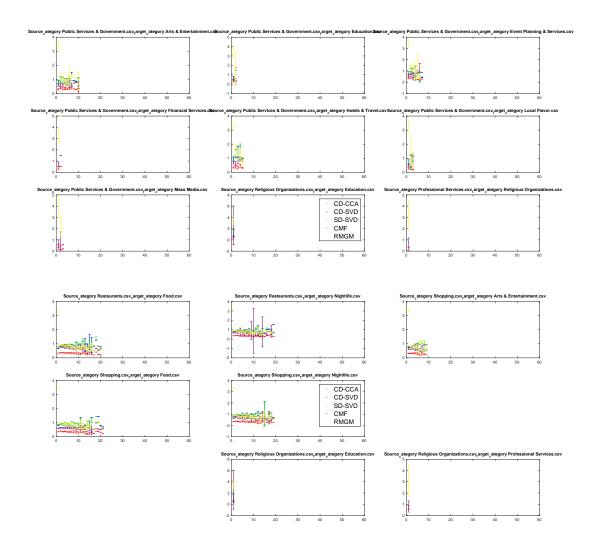


Figure 74: User-based MAE of algorithms in the Yelp dataset, averaged on each domain-pair and sorted based on the users' target domain profile size for domain pairs 144 to 158

B.3.2 MAEs for Source User Profiles

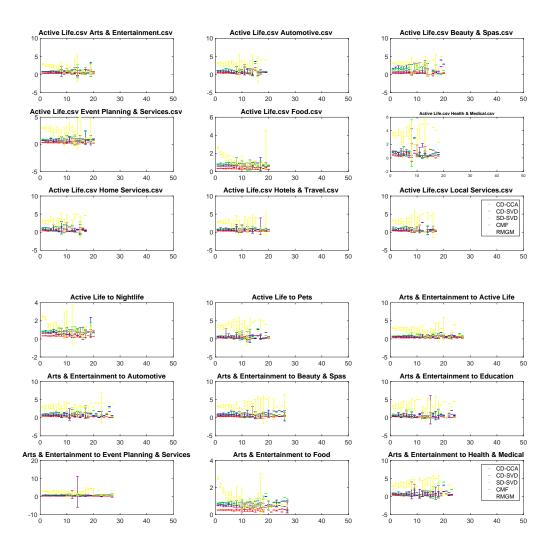


Figure 75: User-based MAE of algorithms in the Yelp dataset, averaged on each domain-pair and sorted based on the users' source domain profile size

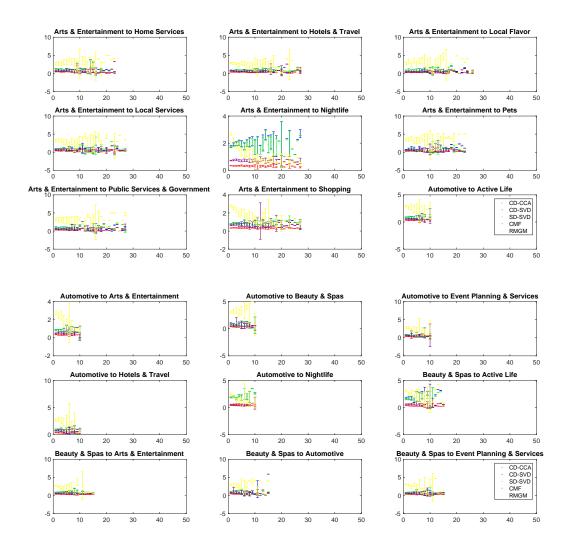


Figure 75: User-based MAE of algorithms in the Yelp dataset, averaged on each domain-pair and sorted based on the users' source domain profile size for domain pairs 19 to 36

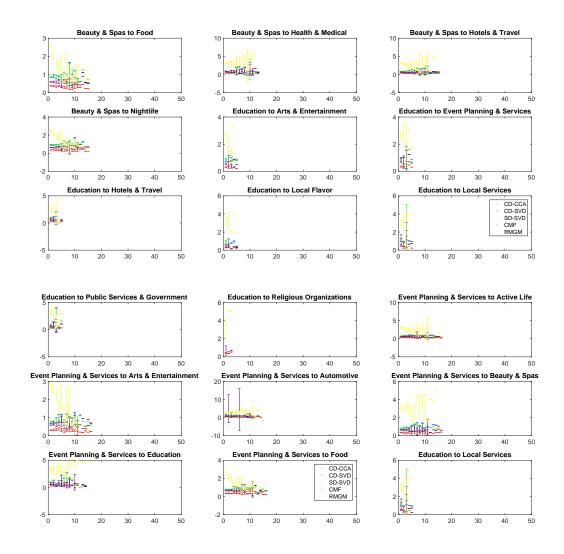


Figure 75: User-based MAE of algorithms in the Yelp dataset, averaged on each domain-pair and sorted based on the users' source domain profile size for domain pairs 37 to 53

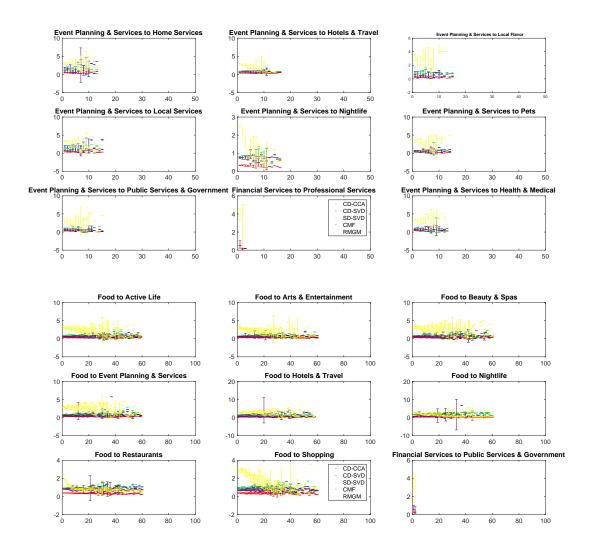


Figure 75: User-based MAE of algorithms in the Yelp dataset, averaged on each domain-pair and sorted based on the users' source domain profile size for domain pairs 54 to 71

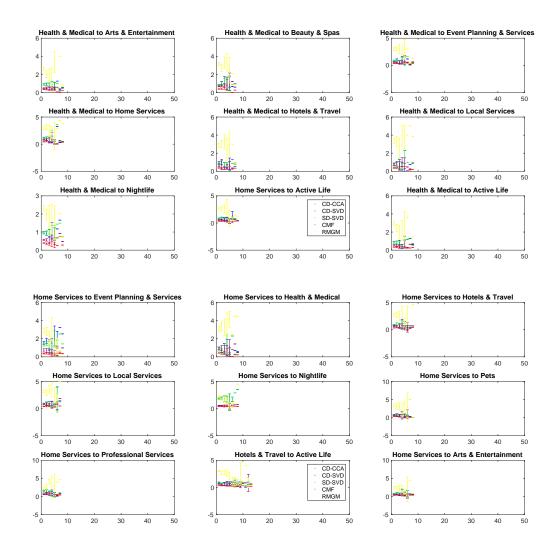


Figure 75: User-based MAE of algorithms in the Yelp dataset, averaged on each domain-pair and sorted based on the users' source domain profile size for domain pairs 72 to 89

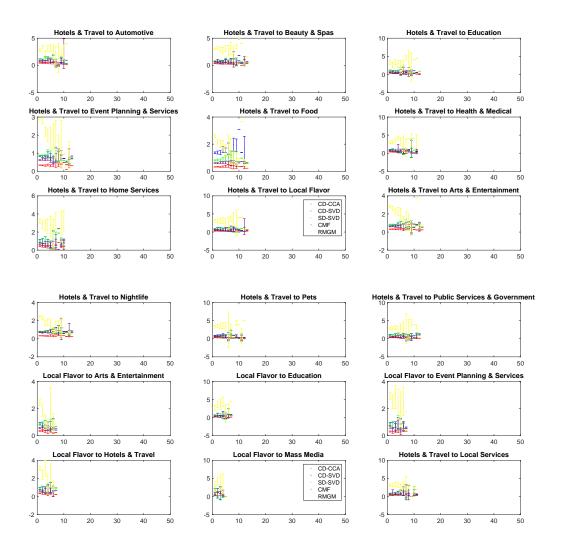


Figure 75: User-based MAE of algorithms in the Yelp dataset, averaged on each domain-pair and sorted based on the users' Source domain profile size for domain pairs 90 to 107

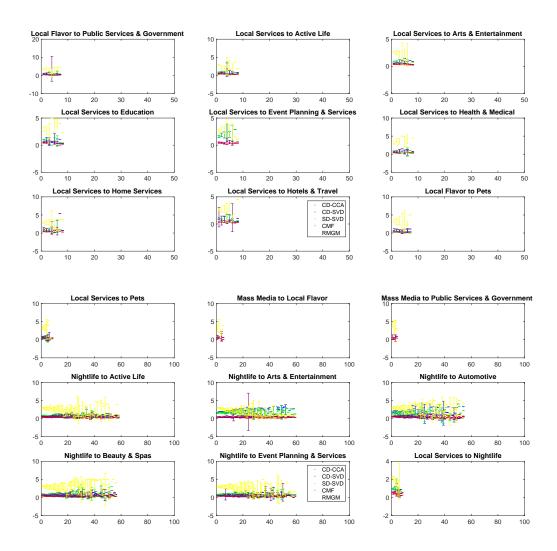


Figure 75: User-based MAE of algorithms in the Yelp dataset, averaged on each domain-pair and sorted based on the users' Source domain profile size for domain pairs 108 to 125

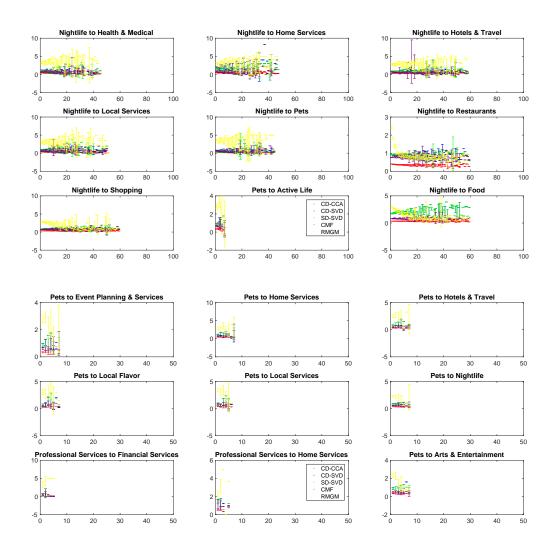


Figure 75: User-based MAE of algorithms in the Yelp dataset, averaged on each domain-pair and sorted based on the users' Source domain profile size for domain pairs 126 to 143

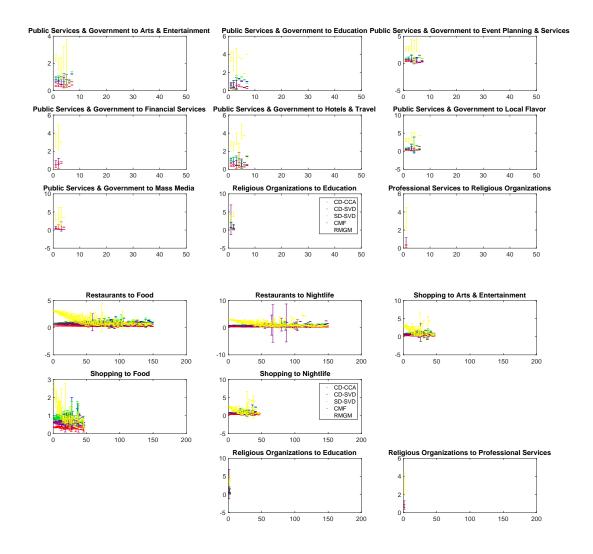


Figure 75: User-based MAE of algorithms in the Yelp dataset, averaged on each domain-pair and sorted based on the users' Source domain profile size for domain pairs 144 to 158

B.4 CORRELATION ANALYSIS FOR YELP DATASET

B.4.1 Correlation Analysis Plots for the RMSE of Algorithms in the Yelp Dataset

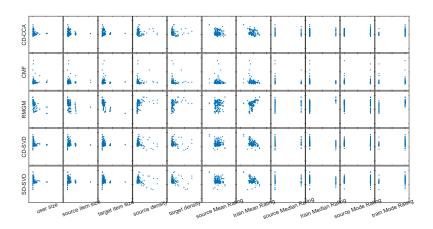


Figure 76: Scatter plot of general and central tendency statistics with the RMSE of algorithms in the Yelp dataset

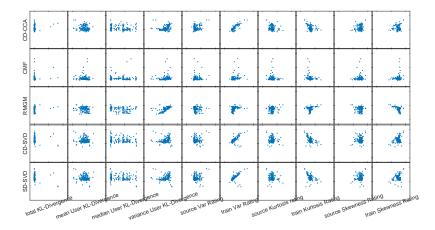


Figure 77: Scatter plot of dispersion statistics with the RMSE of algorithms in the Yelp dataset

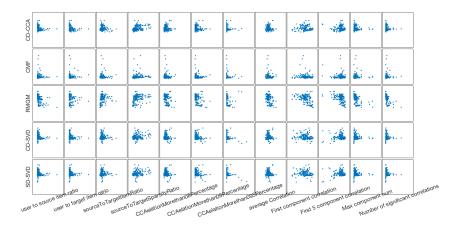


Figure 78: Scatter plot of CCA-related statistics with the RMSE of algorithms in the Yelp dataset

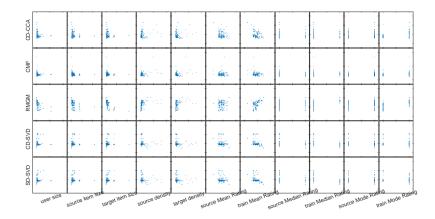


Figure 79: Scatter plot of general and central tendency statistics with the MAE of algorithms in the Yelp dataset

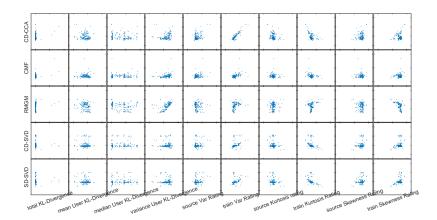


Figure 80: Scatter plot of dispersion statistics with the MAE of algorithms in the Yelp dataset

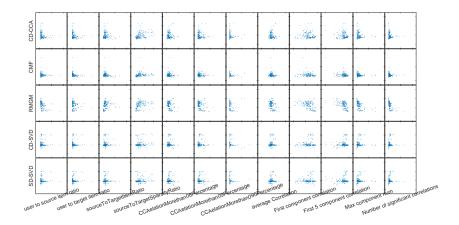


Figure 81: Scatter plot of CCA-related statistics with the MAE of algorithms in the Yelp dataset

B.4.2 Correlation Analysis Plots for the Improvement Ratio of Algorithms in the Yelp Dataset

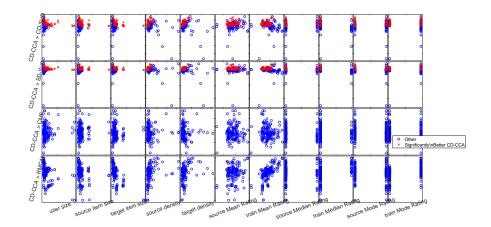


Figure 82: Scatter plot of general and central tendency statistics with the improvement ratio of CD-CCA over other algorithms in the Yelp dataset; red cross shows the cases in which CD-CCA is significantly better than other algorithms

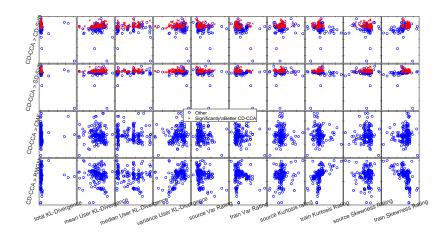


Figure 83: Scatter plot of dispersion statistics with the improvement ratio of CD-CCA over other algorithms in the Yelp dataset; red cross shows the cases in which CD-CCA is significantly better than other algorithms

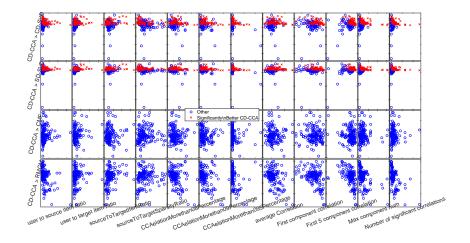


Figure 84: Scatter plot of CCA-related statistics with the improvement ratio of CD-CCA over other algorithms in the Yelp dataset; red cross shows the cases in which CD-CCA is significantly better than other algorithms

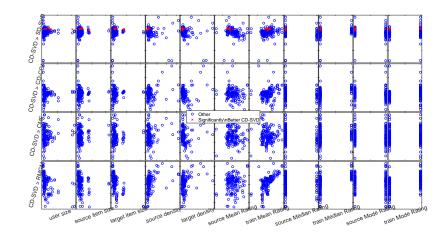


Figure 85: Scatter plot of general and central tendency statistics with the improvement ratio of CD-SVD over other algorithms in the Yelp dataset; red cross shows the cases in which CD-SVD is significantly better than other algorithms

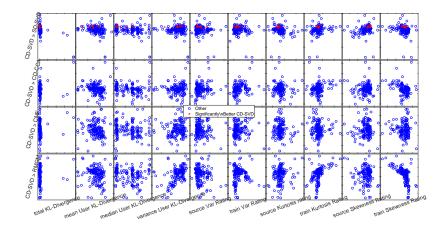


Figure 86: Scatter plot of dispersion statistics with the improvement ratio of CD-SVD over other algorithms in the Yelp dataset; red cross shows the cases in which CD-SVD is significantly better than other algorithms

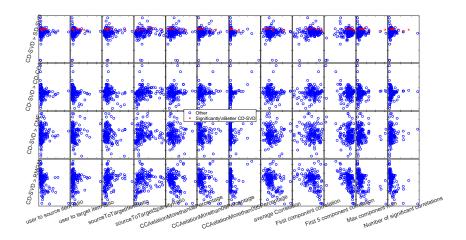


Figure 87: Scatter plot of CCA-related statistics with the improvement ratio of CD-SVD over other algorithms in the Yelp dataset; red cross shows the cases in which CD-SVD is significantly better than other algorithms

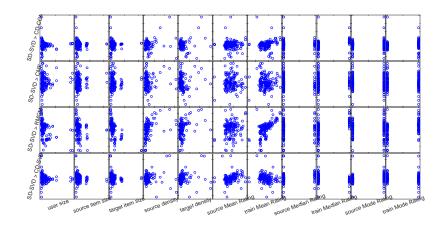


Figure 88: Scatter plot of general and central tendency statistics with the improvement ratio of SD-SVD over other algorithms in the Yelp dataset; red cross shows the cases in which SD-SVD is significantly better than other algorithms

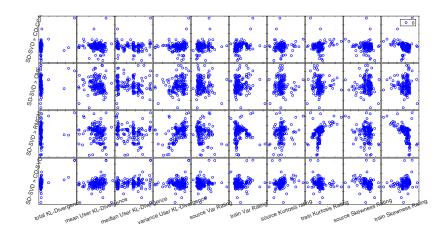


Figure 89: Scatter plot of dispersion statistics with the improvement ratio of SD-SVD over other algorithms in the Yelp dataset; red cross shows the cases in which SD-SVD is significantly better than other algorithms

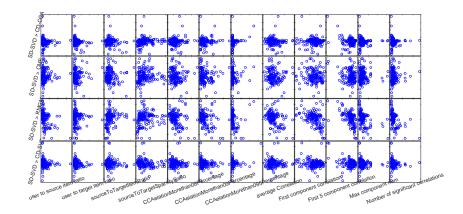


Figure 90: Scatter plot of CCA-related statistics with the improvement ratio of SD-SVD over other algorithms in the Yelp dataset; red cross shows the cases in which SD-SVD is significantly better than other algorithms

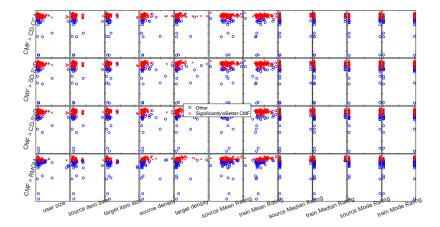


Figure 91: Scatter plot of general and central tendency statistics with the improvement ratio of CMF over other algorithms in the Yelp dataset; red cross shows the cases in which CMF is significantly better than other algorithms

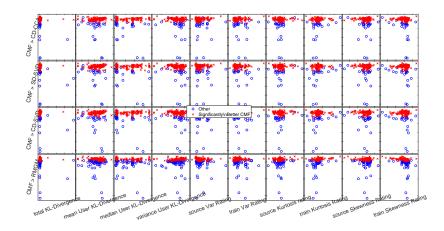


Figure 92: Scatter plot of dispersion statistics with the improvement ratio of CMF over other algorithms in the Yelp dataset; red cross shows the cases in which CMF is significantly better than other algorithms

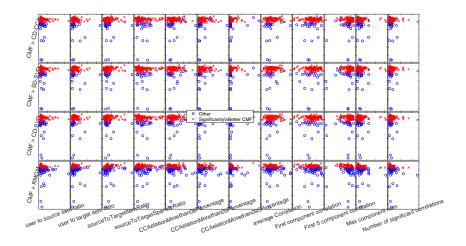


Figure 93: Scatter plot of CCA-related statistics with the improvement ratio of CMF over other algorithms in the Yelp dataset; red cross shows the cases in which CMF is significantly better than other algorithms

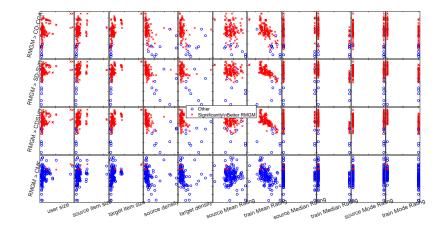


Figure 94: Scatter plot of general and central tendency statistics with the improvement ratio of RMGM over other algorithms in the Yelp dataset; red cross shows the cases in which RMGM is significantly better than other algorithms

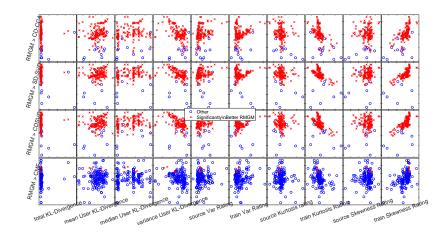


Figure 95: Scatter plot of dispersion statistics with the improvement ratio of RMGM over other algorithms in the Yelp dataset; red cross shows the cases in which RMGM is significantly better than other algorithms

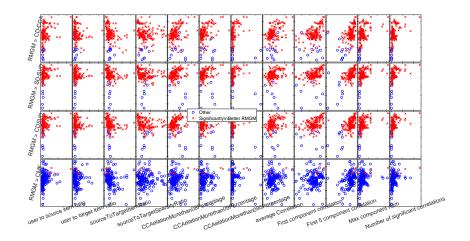


Figure 96: Scatter plot of CCA-related statistics with the improvement ratio of RMGM over other algorithms in the Yelp dataset; red cross shows the cases in which RMGM is significantly better than other algorithms

APPENDIX C

IMHONET DATA FIGURES AND TABLES

C.1 DOMAIN PAIR STATISTICS FOR IMHONET DATASET

Table 48: Domain and domain-pair data size statistics for the Imhonet dataset

source	target	user size	source item size	target item size	source density	target density	user to source item ratio	user to target item ratio	to target item ratio	source to target density ratio
book	game	41756	125688	11407	0.0007	0.0020	0.3322	3.6606	11.0185	0.3574
book	movie	186877	155765	85892	0.0003	0.0014	1.1997	2.1757	1.8135	0.2501
book	perfume	16750	105805	3545	0.0011	0.0037	0.1583	4.7250	29.8463	0.2836
game	book	41756	11407	125688	0.0020	0.0007	3.6606	0.3322	0.0908	2.7977
game	movie	49784	11715	75599	0.0019	0.0028	4.2496	0.6585	0.1550	0.6754
game	perfume	6297	6854	3232	0.0030	0.0041	0.9187	1.9483	2.1207	0.7233
movie	book	186877	85892	155765	0.0014	0.0003	2.1757	1.1997	0.5514	3.9989
movie	game	49784	75599	11715	0.0028	0.0019	0.6585	4.2496	6.4532	1.4806
movie	perfume	17882	63708	3565	0.0041	0.0037	0.2807	5.0160	17.8704	1.1213
perfume	book	16750	3545	105805	0.0037	0.0011	4.7250	0.1583	0.0335	3.5262
perfume	game	6297	3232	6854	0.0041	0.0030	1.9483	0.9187	0.4715	1.3826
perfume	movie	17882	3565	63708	0.0037	0.0041	5.0160	0.2807	0.0560	0.8918

Table 49: Domain ratings central tendency and dispersion statistics for the Imhonet dataset

source	target	source mean rating	target mean rating	source median rating	target median rating	source mode rating	target mode rating	source var. rating	target var. rating
book	game	7.7312	7.5362	8	8	8	8	4.1508	5.0477
book	movie	7.6869	7.2340	8	8	8	8	4.6493	5.0026
book	perfume	7.7453	7.1408	8	8	8	8	4.1754	5.3937
game	book	7.5362	7.7312	8	8	8	8	5.0477	4.1508
game	movie	7.5126	7.2509	8	8	10	8	5.2903	4.5204
game	perfume	7.5926	7.0892	8	8	8	8	4.4979	5.6549
movie	book	7.2340	7.6869	8	8	8	8	5.0026	4.6493
movie	game	7.2509	7.5126	8	8	8	10	4.5204	5.2903
movie	perfume	7.2722	7.1548	8	8	8	8	4.4203	5.4384
perfume	book	7.1408	7.7453	8	8	8	8	5.3937	4.1754
perfume	game	7.0892	7.5926	8	8	8	8	5.6549	4.4979
perfume	movie	7.1548	7.2722	8	8	8	8	5.4384	4.4203

Table 50: Domain and domain-pair ratings dispersion statistics for the Imhonet dataset

source	target	total KL- divergence	user KL-	median user KL- divergence			target Kurtosis rating	source skewness rating	target skewness rating
book	game	6.7790	0.0708	0.0308	0.0139	4.8828	3.7643	-1.2867	-1.1056
book	movie	0.0300	19.0198	17.3032	155.6620	4.2610	3.3225	-1.1816	-0.8741
book	perfume	6.3087	0.1230	0.0664	0.0567	5.1163	3.0342	-1.3706	-0.8117
game	book	1.9261	0.0166	0.0064	0.0014	3.7643	4.8828	-1.1056	-1.2867
game	movie	1.8925	0.0650	0.0200	0.0150	3.6669	3.5379	-1.0931	-0.8978
game	perfume	0.0315	0.0620	0.0143	0.0429	3.8489	3.2307	-1.0844	-0.9086
movie	book	0.0295	17.8306	10.0413	212.1315	3.3225	4.2610	-0.8741	-1.1816
movie	game	7.9774	0.0655	0.0299	0.0113	3.5379	3.6669	-0.8978	-1.0931
movie	perfume	7.7443	0.1199	0.0655	0.0501	3.5520	3.0251	-0.9039	-0.8125
perfume	book	1.5688	0.0265	0.0106	0.0035	3.0342	5.1163	-0.8117	-1.3706
perfume	game	0.0276	0.0476	0.0113	0.0188	3.2307	3.8489	-0.9086	-1.0844
perfume	movie	1.5792	0.1053	0.0349	0.0369	3.0251	3.5520	-0.8125	-0.9039

Table 51: Domain-pair CCA statistics for the Imhonet dataset

source	target	CCA ≥ 0.80	CCA ≥ 0.90	CCA ≥ 0.95	average correla- tion	first com- ponent correla- tion	first compo- nents correla- tion	5 # components	# signifi- cant cor- relations
book	game	1	0.2	0	0.8738	0.9362	0.8738	5	0
book	movie	0.8	0.2	0	0.8547	0.9354	0.8547	5	0
book	perfume	1	1	0.4	0.9454	0.9820	0.9454	5	0
game	book	0.8	0.2	0	0.8639	0.9244	0.8639	5	0
game	movie	0.6	0.2	0	0.8308	0.9132	0.8308	5	0
game	perfume	1	1	0.4	0.9421	0.9649	0.9421	5	0
movie	book	0.8	0.2	0	0.8564	0.9386	0.8564	5	0
movie	game	0.6	0.2	0	0.8354	0.9111	0.8354	5	0
movie	perfume	1	0.8	0.4	0.9362	0.9852	0.9362	5	0
perfume	book	1	1	0.6	0.9472	0.9764	0.9472	5	0
perfume	game	1	1	0.4	0.9459	0.9660	0.9459	5	0
perfume	movie	1	0.8	0.4	0.9350	0.9842	0.9350	5	0

Table 52: RMSE and MAE for domain-pairs in the Imhonet dataset

source	target	CCA RMSE	CD-SVD RMSE	SD-SVD RMSE	CCA MAE	CD-SVD MAE	SD-SVD MAE
book	game	0.2662	0.4262	0.3336	0.2033	0.3276	0.2464
book	movie	0.2319	0.3245	0.3280	0.1778	0.2514	0.2530
book	perfume	0.2336	0.4861	0.4137	0.1875	0.3885	0.3240
game	book	0.2101	0.4118	0.3717	0.1513	0.3147	0.2808
game	movie	0.2204	0.4295	0.4508	0.1688	0.3419	0.3588
game	perfume	0.2314	0.3477	0.3489	0.1863	0.2698	0.2710
movie	book	0.2220	0.3027	0.3017	0.1649	0.2262	0.2226
movie	game	0.2300	0.4388	0.3545	0.1756	0.3333	0.2656
movie	perfume	0.2369	0.4536	0.3667	0.1891	0.3612	0.2859
perfume	book	0.2032	0.4116	0.3726	0.1492	0.3100	0.2753
perfume	game	0.2118	0.3082	0.3070	0.1654	0.2328	0.2296
perfume	movie	0.2131	0.4349	0.4188	0.1641	0.3457	0.3324

C.3 COLD-START ANALYSIS OF DOMAIN PAIRS FOR IMHONET DATASET

C.3.1 MAEs for Target User Profiles

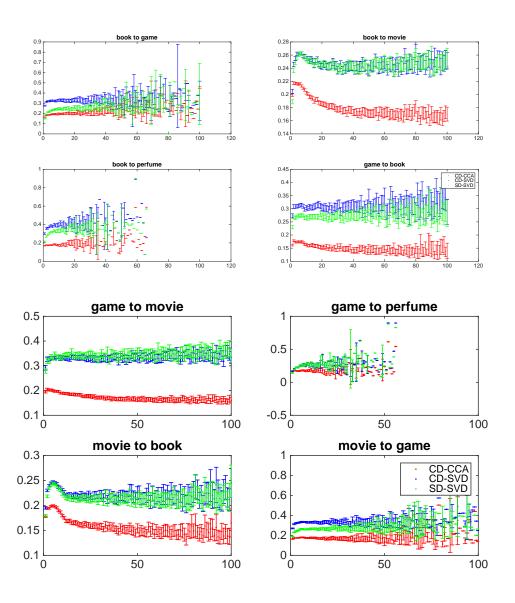


Figure 97: User-based MAE of algorithms in Imhonet dataset, averaged on each domain-pair and sorted based on the users' target domain profile size

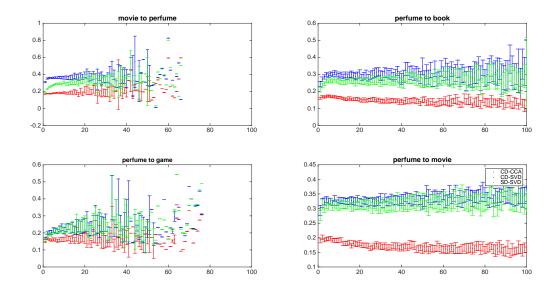


Figure 97: User-based MAE of algorithms in Imhonet dataset, averaged on each domain-pair and sorted based on the users' target domain profile size for domain pairs 9 to 12

C.3.2 RMSEs for Target User Profiles

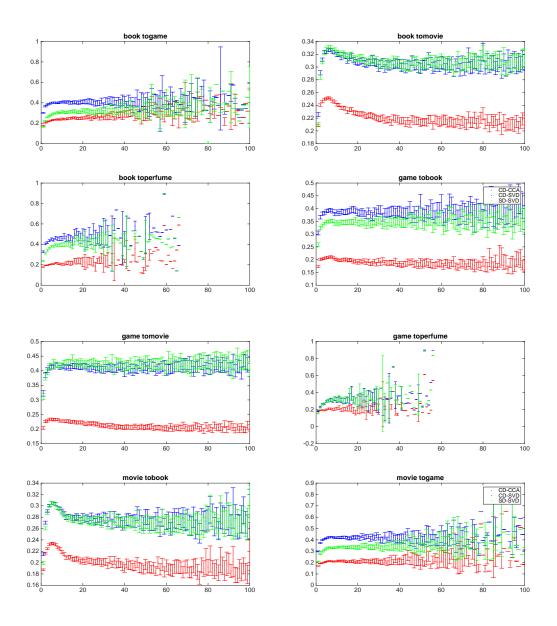


Figure 98: User-based RMSE of algorithms in Imhonet dataset, averaged on each domainpair and sorted based on the users' target domain profile size

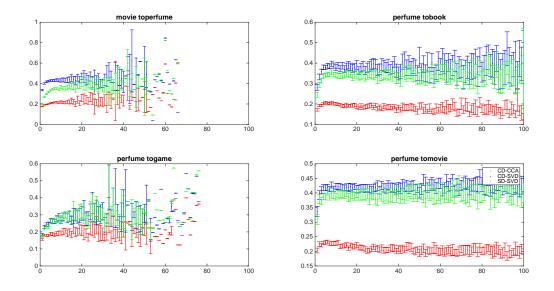


Figure 98: User-based RMSE of algorithms in Imhonet dataset, averaged on each domainpair and sorted based on the users' target domain profile size for domain pairs 9 to 12

C.3.3 MAEs for Source User Profiles

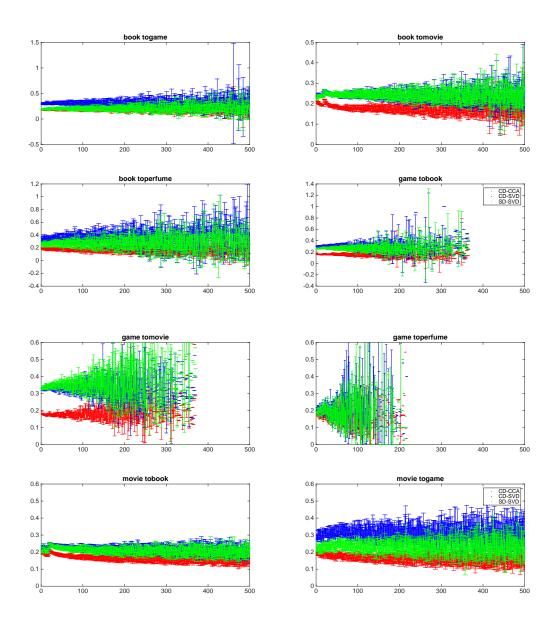


Figure 99: User-based MAE of algorithms in Imhonet dataset, averaged on each domain-pair and sorted based on the users' Source domain profile size

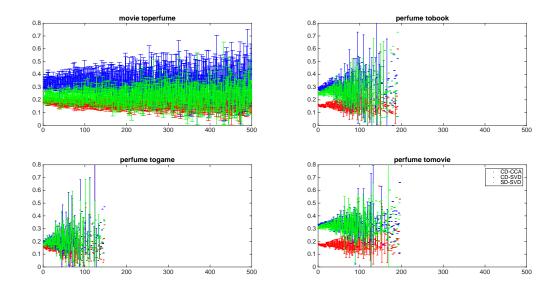


Figure 99: User-based MAE of algorithms in Imhonet dataset, averaged on each domain-pair and sorted based on the users' Source domain profile size for domain pairs 9 to 12

C.3.4 RMSEs for Source User Profiles

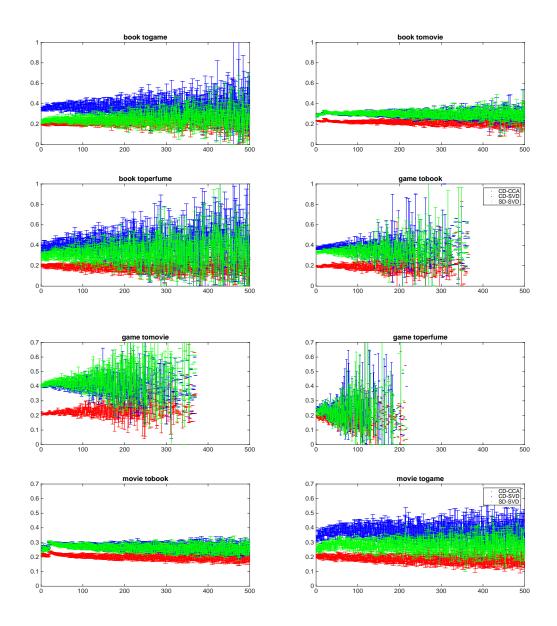


Figure 100: User-based RMSE of algorithms in Imhonet dataset, averaged on each domainpair and sorted based on the users' Source domain profile size

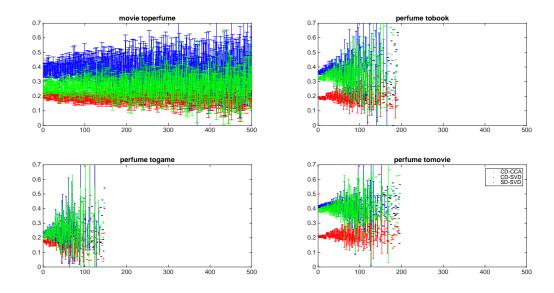


Figure 100: User-based RMSE of algorithms in Imhonet dataset, averaged on each domainpair and sorted based on the users' Source domain profile size for domain pairs 9 to 12

C.4 CORRELATION ANALYSIS FOR IMHONET DATASET

C.4.1 Correlation Analysis Plots for the RMSE of Algorithms in the Imhonet Dataset

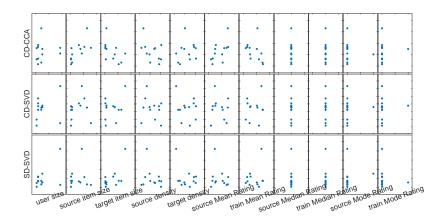


Figure 101: Scatter plot of general and central tendency statistics with the RMSE of algorithms in the Imhonet dataset

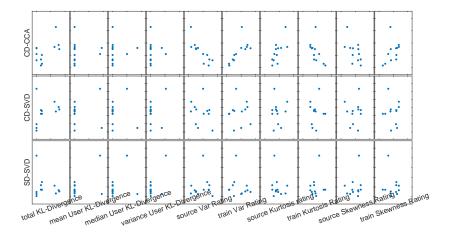


Figure 102: Scatter plot of dispersion statistics with the RMSE of algorithms in the Imhonet dataset

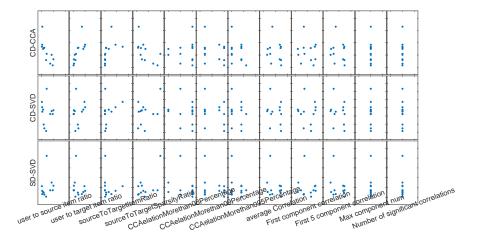


Figure 103: Scatter plot of CCA-related statistics with the RMSE of algorithms in the Imhonet dataset

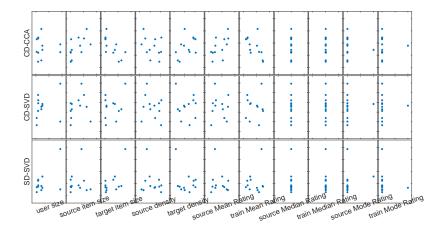


Figure 104: Scatter plot of general and central tendency statistics with the MAE of algorithms in the Imhonet dataset

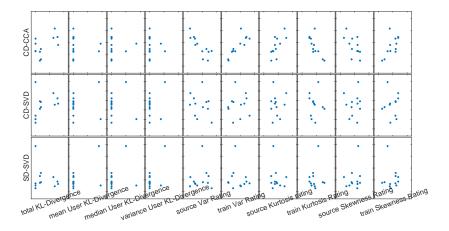
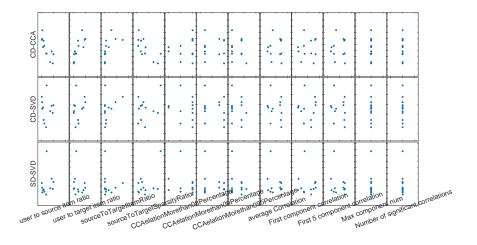


Figure 105: Scatter plot of dispersion statistics with the MAE of algorithms in the Imhonet dataset



 $Figure \ 106: \ Scatter \ plot \ of \ CCA-related \ statistics \ with \ the \ MAE \ of \ algorithms \ in \ the \ Imhonet \ dataset$

C.4.2 Correlation Analysis Plots for the Improvement Ratio of Algorithms in the Imhonet Dataset

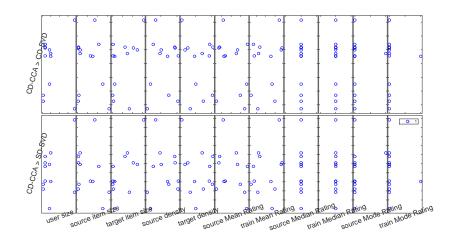


Figure 107: Scatter plot of general and central tendency statistics with the improvement ratio of CD-CCA over other algorithms in the Imhonet dataset; red cross shows the cases in which CD-CCA is significantly better than other algorithms

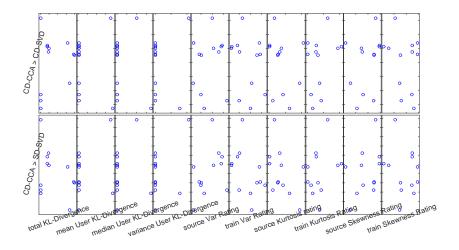


Figure 108: Scatter plot of dispersion statistics with the improvement ratio of CD-CCA over other algorithms in the Imhonet dataset; red cross shows the cases in which CD-CCA is significantly better than other algorithms

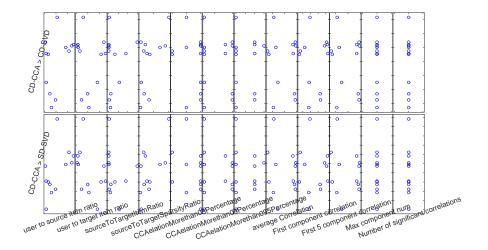


Figure 109: Scatter plot of CCA-related statistics with the improvement ratio of CD-CCA over other algorithms in the Imhonet dataset; red cross shows the cases in which CD-CCA is significantly better than other algorithms

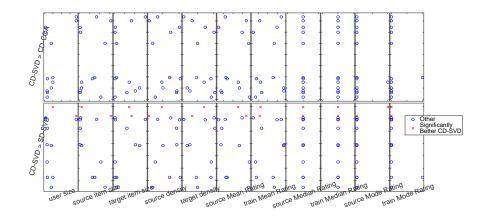


Figure 110: Scatter plot of general and central tendency statistics with the improvement ratio of CD-SVD over other algorithms in the Imhonet dataset; red cross shows the cases in which CD-SVD is significantly better than other algorithms

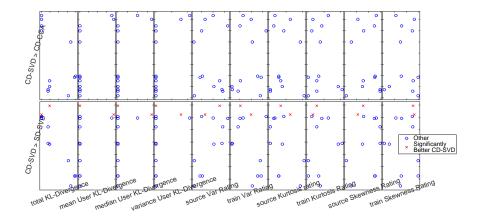


Figure 111: Scatter plot of dispersion statistics with the improvement ratio of CD-SVD over other algorithms in the Imhonet dataset; red cross shows the cases in which CD-SVD is significantly better than other algorithms

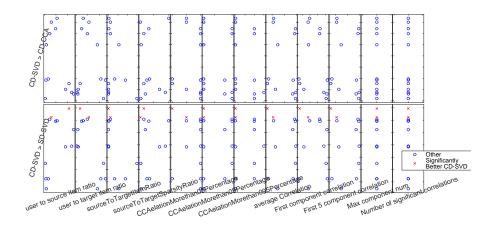


Figure 112: Scatter plot of CCA-related statistics with the improvement ratio of CD-SVD over other algorithms in the Imhonet dataset; red cross shows the cases in which CD-SVD is significantly better than other algorithms

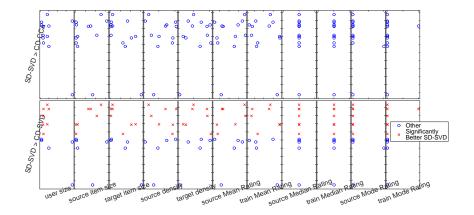


Figure 113: Scatter plot of general and central tendency statistics with the improvement ratio of SD-SVD over other algorithms in the Imhonet dataset; red cross shows the cases in which SD-SVD is significantly better than other algorithms

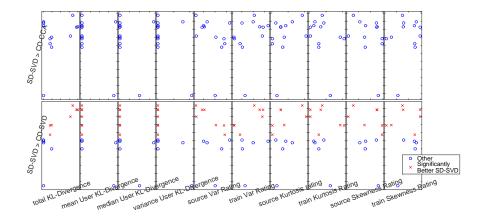


Figure 114: Scatter plot of dispersion statistics with the improvement ratio of SD-SVD over other algorithms in the Imhonet dataset; red cross shows the cases in which SD-SVD is significantly better than other algorithms

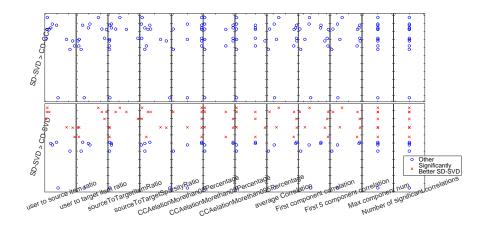


Figure 115: Scatter plot of CCA-related statistics with the improvement ratio of SD-SVD over other algorithms in the Imhonet dataset; red cross shows the cases in which SD-SVD is significantly better than other algorithms

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