

DEVICE-INDUCED ERYTHROCYTE DEFORMATION USING M-FLOW  
VISUALIZATION

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# DEVICE-INDUCED ERYTHROCYTE DEFORMATION USING M-FLOW VISUALIZATION

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Implantable cardiovascular devices are commonly used in clinical treatment for end stage cardiovascular devices. However, they may cause device-induced blood damage which can cause serious complications such as hemolysis and thrombosis. Blood damage often occurs within small passages or journals of the flow path. These regions may be associated with hot-spots in which shear stress is excessive and cells may be irreversibly strained. The successful design of these devices relies on efficiently minimizing supra-physiologic shear fields through computational modeling. However the fundamental blood mechanics under these conditions are not yet fully characterized.

This study was therefore conducted to elucidate the microscopic mechanics of cellular deformation that underlie shear-induced hemolysis. A micro fluid system was developed to emulate flow environments at hot-spots and provide optical access for microscopic visualization. The flow of red blood cells (RBCs) within micro channels was illuminated by a pair of stroboscopes resulting in a rapid succession of images -- recorded by double-exposure digital CCD camera. Red blood cell motion and deformation dynamics, as well as the surrounding fluid velocity field under various conditions of hematocrit, flow rate were quantitatively measured using particle image velocimetry (PIV) technique.

The results show that cells deform rapidly as they approach the inlet, bear the largest deformation at inlet, keep large deformation inside channel and recover as soon as flowing out of exit. Inside channel, cell deformation will reach to a threshold that the cells will not be elongated as shear stress increases. We concluded that the largest possibility for blood damage occurs at the inlet of gaps or clearance in cardiovascular devices, due to the combined effect of extensional stress and shear stress. The combined effect is great on blood mechanical damage in that it can deform the cell to a maximal value in a transient time. The sublethal damage is more likely to happen than the visible rupture of red cells in our experimental situation.

Our findings show basic mechanism underlining device-induced blood damage. The methods are proved to be effective and ready to be applied in further design and investigations.

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## **1.0 INTRODUCTION**

### **1.1 BLOOD AND BLOOD DAMAGE**

#### **1.1.1 Blood and blood rheology**

Blood is a suspension of formed cellular elements in an aqueous solution called plasma [1]. Plasma occupies 55-60% of total blood volume. The main content of plasma is water, which is about 90% by weight. Plasma also contains of 7% plasma protein, 1% inorganic substances and 1% organic substances. The cellular elements occupy the remaining 40-45% of blood volume. There are three kinds of cellular contents, erythrocytes, or red blood cells (RBCs); leukocytes, or white blood cells (WBCs); and platelets. Red blood cells are the most numerous cells, which account for 95%of cellular contents by volume. They conduct the important role of delivering oxygen to the tissue and removing waste from it. Though white blood cells and platelets only contain 5% by volume, they have important roles in immunity and hemostasis, respectively.

##### **1.1.1.1 Macroscopic RBC rheology**

Blood rheology has been studied for many years. In a bulk flow, blood shows a non-Newtonian behavior in a low shear rate ( $<100 \text{ s}^{-1}$ ), with a decreasing viscosity as shear rate increases [2].

The blood converts to show a Newtonian behavior as the shear rate exceeds  $100 \text{ s}^{-1}$ . In a near zero shear rate, Cokelet et al. [3] and Merrill et al. [4] showed a finite yield stress, which made blood behave like an elastic solid. Cokelet et al. also showed that the experimental data was able to fit into Casson's equation [5] when the hematocrit is below 33%. Chien et al. [6] illustrated the effects of red blood cell aggregation and deformation on the non-Newtonian behavior of blood flow. They showed that red blood cell aggregation is responsible for the viscosity increase at low shear rate. As the shear rate increased, the disaggregation and the cells deformation causes a decrease in viscosity.

#### **1.1.1.2 Microscopic observation of RBC rheology**

In microcirculation, since the diameter of a blood vessel is comparable to the diameter of red blood cells, the blood needs to be considered as a two-phase fluid instead of a homogeneous one. Many studies have been performed to investigate the microscopic behavior of blood flow and blood cells under shear stress in glass capillary and isolated vessels. For cell aggregation, Reinke et al. reported a formation of a cell free plasma layer near the tube wall due to the cell aggregation in a vertically oriented small tube [7] and cell sedimentation on the bottom of the tube when it was horizontally oriented [8]. Bishop et al. reported the same situation happen in vivo [9]. Chien et al. observed the cell behavior in shear disaggregation [10]. They concluded that cells separated from each other by rolling rather than sliding.

For cell deformation, Fischer et al. illustrated the cell deformation from biconcave shape to ellipsoid under an increasing shear rate up to  $500 \text{ s}^{-1}$  using a cone and plate viscometer [11].

They also observed that the orientation of elongation was parallel to the flow direction. They believed there was a membrane rotation, which they described as tank tread, during deformation. Sutura et al. also observed the ellipsoid deformation using a concentric cylinder viscometer [12]. They reported that the cell began to lose the biconcave shape at about 500 dynes/cm<sup>2</sup> and became an ellipsoid when the shear stress exceeded 1500 dynes/cm<sup>2</sup>. The cell would be elongated more with continuous increasing of shear stress, with more pointed tips on its two ends. They also reported that the cell would recover to its original shape one minute after the termination of shear stress loading. Those observations illustrated the fluid drop-like deformations of red blood cells in the flow media. The cells can be deformed without changing the surface area and volume under low shear stress conditions.

However, most of the previous microscopic studies are conducted in low shear stress conditions or high-uniform shear stress conditions. None of them are related to the characteristic conditions which red blood cell encounter in cardiovascular devices.

### **1.1.2 Blood cell damage**

Blood cell damage, also called blood trauma, means the pathological changes of cellular elements in blood, including morphologic changes, shortened life span, biochemical functional alterations and complete rupture. Red blood cells can be mechanically destructed due to extremely high shear stress and release hemoglobin. This is defined as “hemolysis”. Platelets can also be stimulated by stress. The platelet aggregation results in thrombosis. Our research stressed on the mechanical damage of red blood cells.



### **1.1.2.1 Previous studies for RBCs damage**

Over the last forty years, many investigations have been performed on flow induced blood trauma. Many of them were conducted to study the shear induced hemolysis in well defined flow conditions. Conventional shear devices, such as cone-and-plate viscometers, concentric cylinder viscometers and capillary tubes, were applied to provide such flow conditions [13] [14] [15]. Blood suspensions were subjected to shear stress for prescribed times and plasma free hemoglobin (fHb) concentration was measured as an index for hemolysis. Those studies showed that there were two primary factors on shear induced hemolysis: shear stress amplitude and loading time. The threshold of shear stress for long exposure times, which is from seconds to minutes, was reported by numerous investigators [14] [16]. Those experiments could not be conducted for a short exposure time on the order of micro seconds. A few investigators also designed novel experimental methods to find the hemolysis status under short exposure times [17]. However, the threshold values in those studies are inconsistent and being debated and revised [18].

These historical studies have provided a general guideline for red blood cell hemolysis. However, the precise mechanisms of blood damage and flow behavior under high shear stress and low exposure time conditions remain unclear.

## **1.2 DEVICE INDUCED BLOOD DAMAGE**

### **1.2.1 Cardiovascular devices**

Cardiovascular disease (CVD) is the No. 1 killer in United States. Over 2,600 people die from CVD every single day. The high mortality of heart diseases urged the development of cardiovascular devices, which could be substituted for part or whole function of the impaired organ. Since 1950s', cardiovascular devices have been developed rapidly. As far as today, prosthetic heart valves replacement has been proved to be a successful treatment to heart valve diseases. Ventricular assist devices (VAD) of varied designing principles have been used either as a temporary bridge for keeping patient alive until later transplantation or as a recovery method for postcardiotomy [19]. Cardiovascular bypass and oxygenator have been used as a standard during the operation through out the world [20]. As a whole, cardiovascular devices are commonly used as a clinical treatment for end stage cardiovascular diseases and improving the survival rate and life qualities for many patients.

### **1.2.2 Hemolysis induced by implantation, clinical reports**

Though enormous amount of research has been done to improve the design and performances of cardiovascular devices over the last two decades, it is still impossible to mimic an exact physiological environment for the blood contacting those devices. The non physiological condition induced by implantation of cardiovascular devices within circulation system acts as a source for multiple complications such as hemolysis and thrombosis. Several clinical researchers have reported the hemolysis complication associated with the implantation of artificial organs in the past two years. Burda et al reported the extracorporeal membrane oxygenation (ECMO)

related hemolysis[21]. Okumiya et al investigated the hemolysis caused by the replacement of cardiac valve prostheses [22]. Allman et al reported an uncommon hemolytic anemia case after the implantation of heart valves [23].

### **1.2.3 Sublethal blood damage**

In addition to hemolysis, cardiovascular devices may also cause sublethal mechanical damage to red blood cells, which cannot be measured through plasma free hemoglobin concentration. Compared to hemolysis studies, very few papers address sublethal blood damage. Artificial organs are found to decrease the deformability of red blood cells [24]. Red blood cells with a low deformability may be prevented from going through the microvessels and may be removed from circulation by spleen. Mechanical stresses have also been reported to change the blood rheology and shorten the life span of RBCs [25].

### **1.2.4 Previous attempts on design and optimization**

Compared to the historical blood damage studies, which were conducted in well defined flow conditions, the flow status in cardiovascular devices is much more complex. A number of in vitro and in vivo studies have been conducted on realistic cardiovascular devices for getting deep knowledge of the characteristic flow pattern, stress-strain conditions, and the blood damage index under specific device working status, for the purpose of optimizing the design to decrease complication rate.

For prosthetic heart valves, researcher stressed on valve closure behavior and pressure-flow conditions. Rebound [26] and squeeze flow [27] phenomena have been found. The regurgitant back flow has been reported to contribute significantly to overall hemolysis in heart valve [28]. In the more complex case of ventricular assistant pump, more criteria need to be considered and a medium needs to be made between the reduction of hemolysis and the adequacy of pump working efficiency. Factors such as rotary speed, geometry design, materials choice and surface quality were precisely studied [29] [30] [31] [32]. Flow visualization has been used to directly illustrate the flow conditions around pumps [33]. There are also hemolytic studies being conducted in other implantable devices. For example, Umezu et al. tested the hemolysis level in stent connectors of different geometries[34]. Sharp et al. reported the hemolysis status in needles and catheters [35].

Most recently, research began to combine numerical simulation and experimental results to seek the correlations between blood stress conditions and damage. Mathematical models for the relationship of stress and hemolysis were established based on experimental data[36] [37]. Computational Fluid Dynamics (CFD) provided a way to estimate and optimize the complicated fluid dynamic situation in multiple cardiovascular devices [38] [39] and predict hemolysis status [40] [41] [42].

The fluid dynamic studies showed that cardiovascular devices induced a non-physiological shear stress, which is much higher than normal, and a quite dynamic flow condition to blood through them. The shear stress distribution is not a uniform one. The highest and most damaging shear stresses are often located in specific regions, which have been referred to as “hot-spots” [43] [44]

[45]. Sharp edges, steps, narrow gaps are the usual “hot-spots” in cardiovascular devices. For instance, in the *StreamLiner* ventricular assist device, an axial blood pump developed by our group [44], the maximum shear stresses are localized in the blade tip region and the leading edge of the stator blades. To achieve the highest pump hydraulic efficiency, blood needs to be moved through a blade tip gap about 50 $\mu$ m wide. The “hot-spots” are regions most likely to cause hemolysis, though only a few individual blood cells in the pump will be subjected to the highest shear stress. The contacting time for the blood through those regions is also very short, which is on the order of micro seconds.

The main contribution of the previous studies is the illustration of the high shear stress, low exposure time conditions faced by surface contacting blood in “hot-spots”. A lot of effort was put into optimizing the design of those regions to reduce blood damage. However, most of the designs are conducted in a trial and error fashion, which is a result of the unclear fundamental mechanism of blood deformation and rupture dynamics under the specific environment caused by the implantation of cardiovascular devices. Neither experimental nor CFD modeling research has been conducted in a micro-scale environment with blood considered as a two phase flow. A mathematical model based on a single-continuum, homogenized fluid may lead to the wrong design prediction.

### **1.3 MOTIVATION**

With the increasing use of artificial organs, the blood trauma problem has become an important clinical issue. To overcome blood trauma is a major challenge in the development of implantable cardiovascular devices. However, the fundamental understanding of blood damage associated with characteristic features of cardiovascular devices still remains unclear. Previous fundamental studies are focused on microcirculation, with a low shear stress and a long exposure time. The blood damage studies associated with cardiovascular devices are superficial due to the lack of cell deformation and rupture dynamics under high shear stress, low exposure time conditions. The CFD model was established regardless the two phase nature of blood. All of those issues will slow the development of cardiovascular devices.

The motivation of this project is to resolve the issues risen above. We believe the understanding of device-induced blood damage at a micro-scale level is critical to the long-term success and advancement of cardiovascular device technology.

### **1.4 AIM OF THESIS**

The aim of this project is to find a novel experimental method to 1.understand the dynamic process of red blood cell deformation under non-uniform high shear stress conditions; 2.study the mechanism underlying device-induced hemolysis; 3.provide mechanistic basis for numerical

prediction of blood damage; 4.provide rigorous engineering principles for designing and improving cardiovascular devices.

## **2.0 METHODS**

### **2.1 SAMPLE PREPARATION**

#### **2.1.1 Low viscosity blood sample**

Fresh bovine blood was collected in the animal facility at the McGowan Institute for Regenerative Medicine (MIRM). Blood was centrifuged at 3000 RPM for 10 minutes. After centrifugation, plasma and buffy coat, which contains white blood cells and platelets, were removed. Red blood cells (RBCs) then were washed for three times for further removing other blood components. PBS solution (Sigma-Aldrich Corp., St. Louis, MO, 0.01 M phosphate buffer, 0.0027 M potassium chloride and 0.137 M sodium chloride, pH 7.4 at 25 °C) was used as resuspended media in the first two washes and for the third time, 1% bovine albumin (Sigma-Aldrich Corp., St. Louis, MO) was added in PBS solution to prevent RBCs from sticking together.

After washing, the sample hematocrit was measured by capillary centrifuge (IEC Micro MB, IEC Co., Needham Heights, MA). RBCs were resuspended to a needed hematocrit before experiment by adding specified amount of PBS with 1% albumin solution.



The sample hematocrit and viscosity were measured before each experiment, using capillary centrifuge and glass viscometer (Cannon U-tube, Cannon Instrument Co., State College, PA). Temperature was also recorded. For our experiments, hematocrit is  $(20\pm 2)\%$  and viscosity is  $(1.8\pm 0.1)\text{cp}$  at ambient temperature ( $25^\circ\text{C}$ ).

### **2.1.2 High viscosity blood sample**

Dextran 40 (Sigma-Aldrich Corp., St. Louis, MO, MW=37,500) was used for making high viscosity RBC suspension. Several preliminary trials had been done to determine the molecular weight (MW) and the concentration of the dextran for experimental using, which is needed to simulate the sample. Low MW dextran was preferred to reduce the possibility of coagulation. The concentration of dextran solution used in the experiment was 30%, with 6g dextran being added to 20g 0.9% sodium chloride solution (Baxter International Inc., Deerfield, IL). The solution was stirred until the dextran was solved completely.

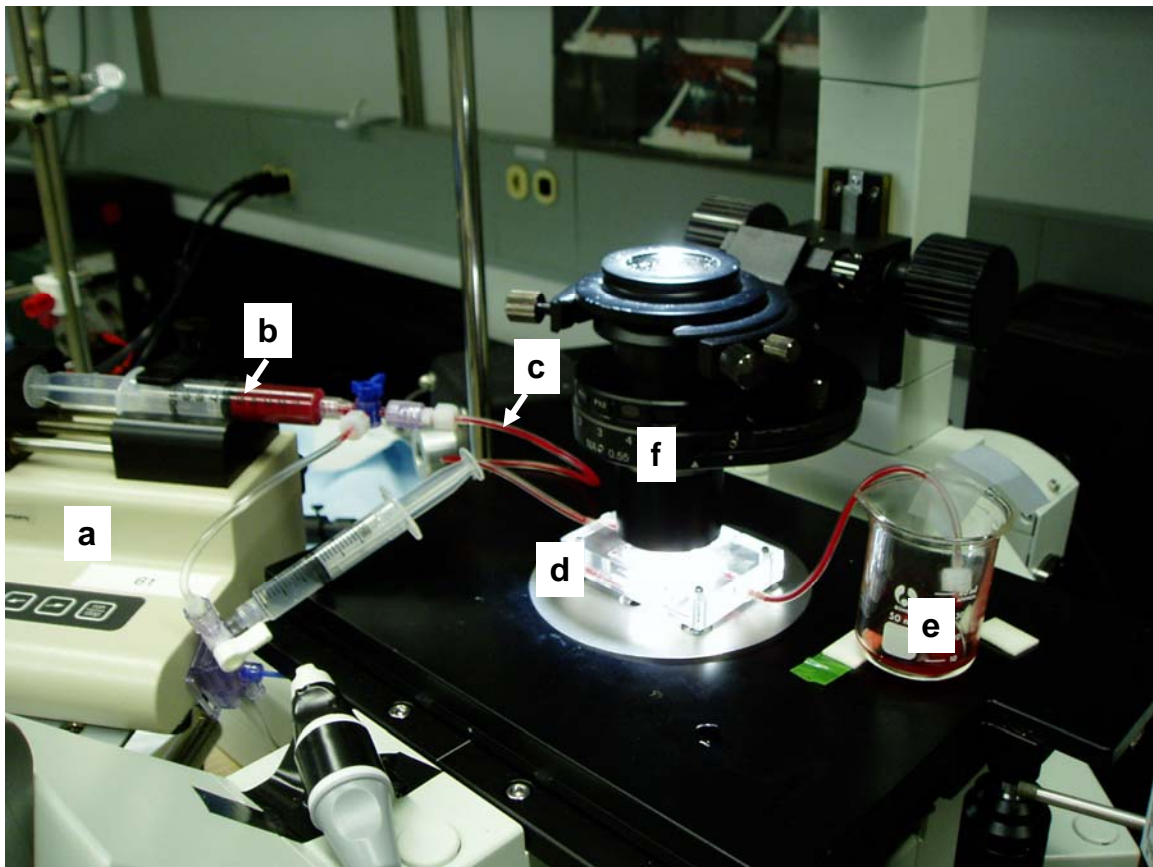
The blood sample was washed using the procedure described in 1.1. Hematocrit was measured after washing. Dextran solution was added to resuspend RBCs to achieve hematocrit of  $(5\pm 0.2)\%$ . Viscosity was also measured. The resulting viscosity was  $(30\pm 2)\text{cp}$ .

## **2.2 MICRO-FLUID SYSTEM**

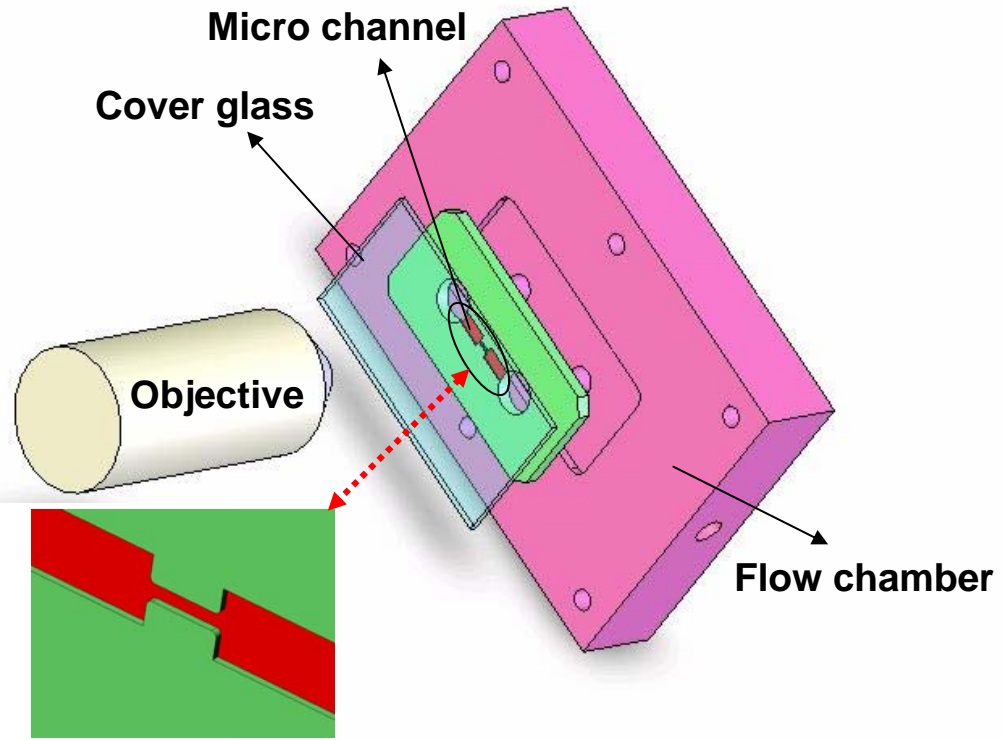
The micro-fluidics system (fig.1) includes a 10ml plastic syringe which was put on a syringe pump (KDS100, KD Scientific Inc., Holliston, MA), a transparent flow chamber with

poly(dimethylsiloxane) (PDMS) micro channel underneath, a reservoir and PVC tubing. A piece of PDMS micro channel was adhered to the bottom of a custom chamber using silicon glue. The channel side faced the bottom and was sealed with a glass slide (fig.2). In the experiment, blood was driven by syringe pump at desired flow rates and forced through micro channel.

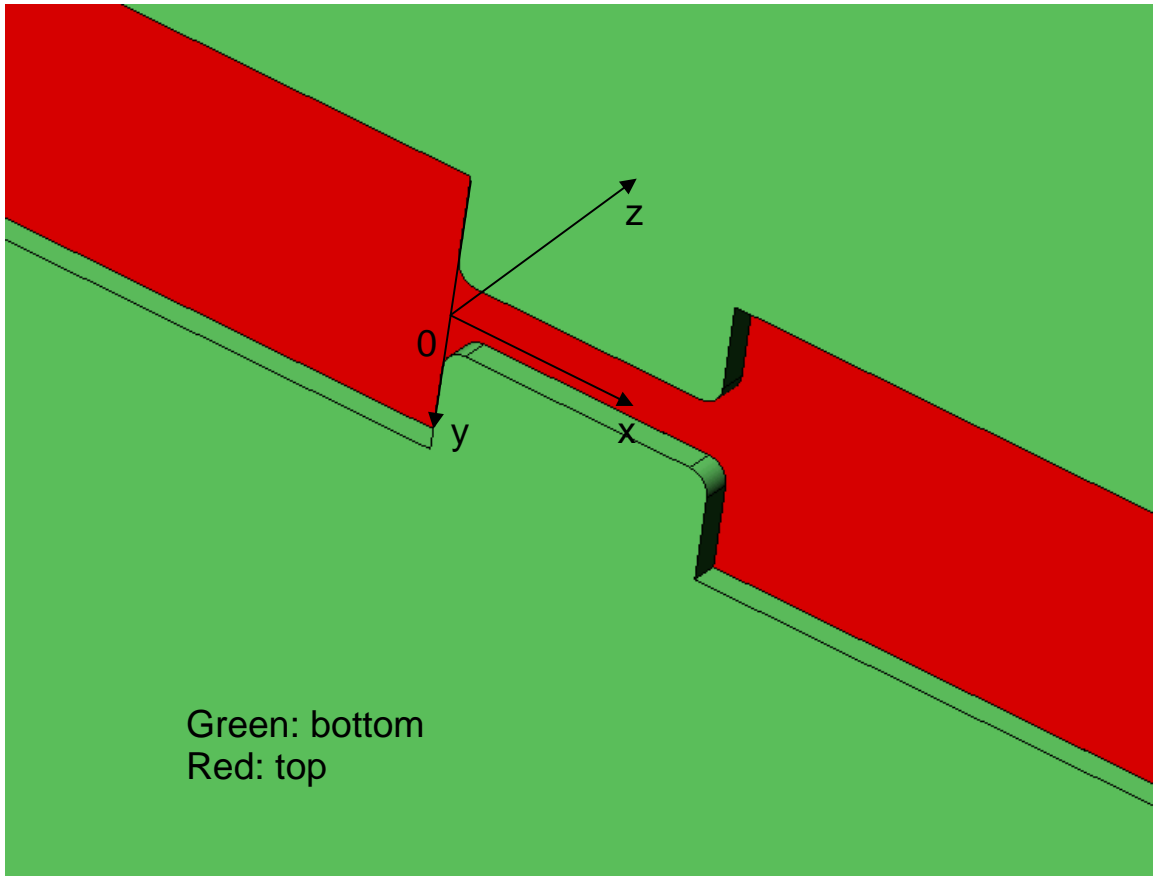
The PDMS channel is the crucial component of micro fluid system. The cross section of channel is rectangular to give a good optical access. The edge of channel is smooth and the inlet and outlet have a radius of 15 $\mu$ m.



**Fig. 1** Micro-fluidics system, a: syringe pump, b: syringe, c: PVC tubing, d: flow chamber and micro channel, e: reservoir, f: inverted microscope



**Fig. 2** Channel and chamber assembly



**Fig. 3** Micro channel coordinate system

## **2.2.1 Micro channel design and fabrication**

### **2.2.1.1 Coordinate system**

A right-handed Cartesian coordinate system was used to define the micro channel dimensions (fig.3). The x coordinate is parallel to blood flow. The y and z coordinates are aligned to the channel width and depth, respectively. The origin of coordinate is at the intersection of centerline and the line across channel inlet ( $x=0, y=0$ ) on the bottom plane of the channel ( $z=0$ ). The x

coordinate increases in the downstream direction. The z coordinate increases as the plane moving from bottom to top.

### 2.2.1.2 Channel dimension design

The solution for fully developed flow through a duct with rectangular cross section [46] was used as a theoretical guideline for designing channel dimensions, in order to maintain a high shear stress and a short exposure time. Blood was assumed as an incompressible Newtonian fluid to simplify the problem.

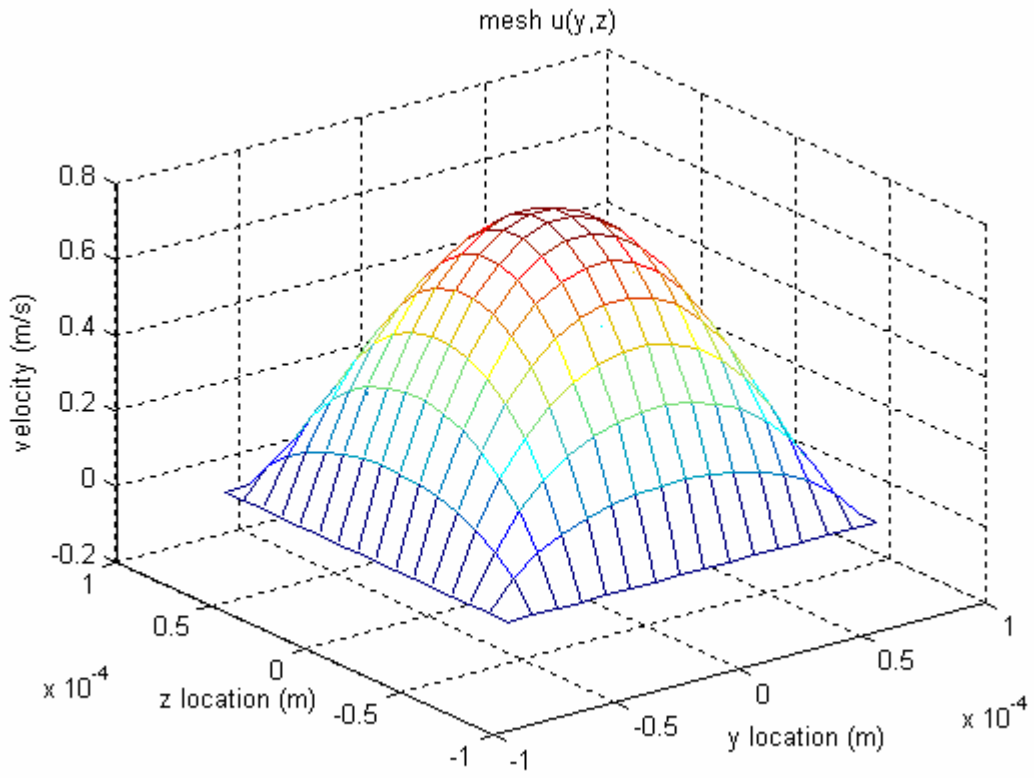
$$u(y, z) = \frac{16a^2}{\mu\pi^3} \left( -\frac{d\hat{p}}{dx} \right) \sum_{i=1,3,5,\dots}^{\infty} (-1)^{(i-1)/2} \left[ 1 - \frac{\cosh(i\pi z / 2a)}{\cosh(i\pi b / 2a)} \right] \times \frac{\cos(i\pi y / 2a)}{i^3} \quad (1)$$

$$Q = \frac{4ba^3}{3\mu} \left( -\frac{d\hat{p}}{dx} \right) \left[ 1 - \frac{192a}{\pi^5 b} \sum_{i=1,3,5,\dots}^{\infty} \frac{\tanh(i\pi b / 2a)}{i^5} \right] \quad (2)$$

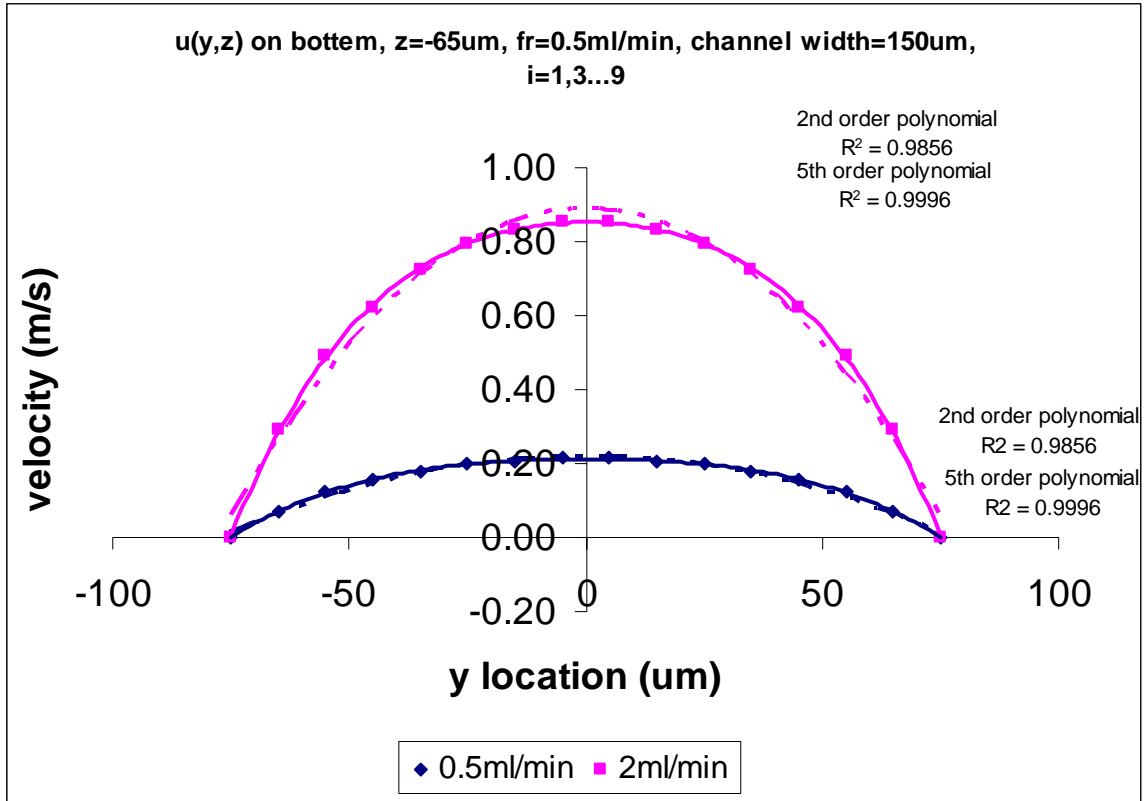
$$(-a \leq y \leq a, -b \leq z \leq b)$$

The terms in equation 1 are defined in table 1.

The 3-D velocity profile is shown in figure 4a. At specified x-y plane, the velocity curve is a near parabolic. The cross section geometry causes a small bluntness as shown in figure 4b.



(a)



**(b)**

**Fig. 4** Theoretical velocity curve in a micro channel with a rectangular cross section, channel width=150μm, depth=150μm, a: 3D velocity curve, b: bluntness of the curve, solid lines indicate 5<sup>th</sup> order polynomial regression, dash lines indicate quadratic regression, the difference of solid line and dash line in each flow rate indicates the bluntness

Hydraulic diameter of cross section was introduced to compute Reynolds number of flow in non-circular duct,

$$D_h = \frac{4 \times \text{cross area}}{\text{wetted perimeter}} \quad (3)$$

The equation for calculating Reynolds number is

$$\text{Re}_{d_h} = \frac{\rho \bar{u} D_h}{\mu} \quad (4)$$

The terms in equation 6 are defined in table 1.

**Table 1** Symbol definition in equation 1-6

<b>Symbol</b>	<b>Definition</b>
$a$	Half of channel width
$b$	Half of channel depth
$u$	Velocity
$\mu$	Viscosity
$\hat{p}$	Pressure
$Q$	Flow rate
$D_h$	Hydraulic diameter
$\text{Re}_{D_h}$	Reynolds number
$\rho$	Density
$\bar{u}$	mean velocity

Table 2 shows the theoretical value for the two kinds of channels used in our experiment, which have the same length of 2000 $\mu\text{m}$  and depth of 150 $\mu\text{m}$ , but have different widths of 50 $\mu\text{m}$  and 150 $\mu\text{m}$ , for both high viscosity flow (30cp) and low viscosity flow (1.75cp). Because the microscope objective was focused on the plane near bottom, the z plane was assumed as 10 $\mu\text{m}$  above the bottom. We can see that the blood inside the channel can be undergoing sufficiently high shear stress and short exposure time, both for a high and low viscosity sample. The Reynolds number is low enough for maintaining a laminar flow.



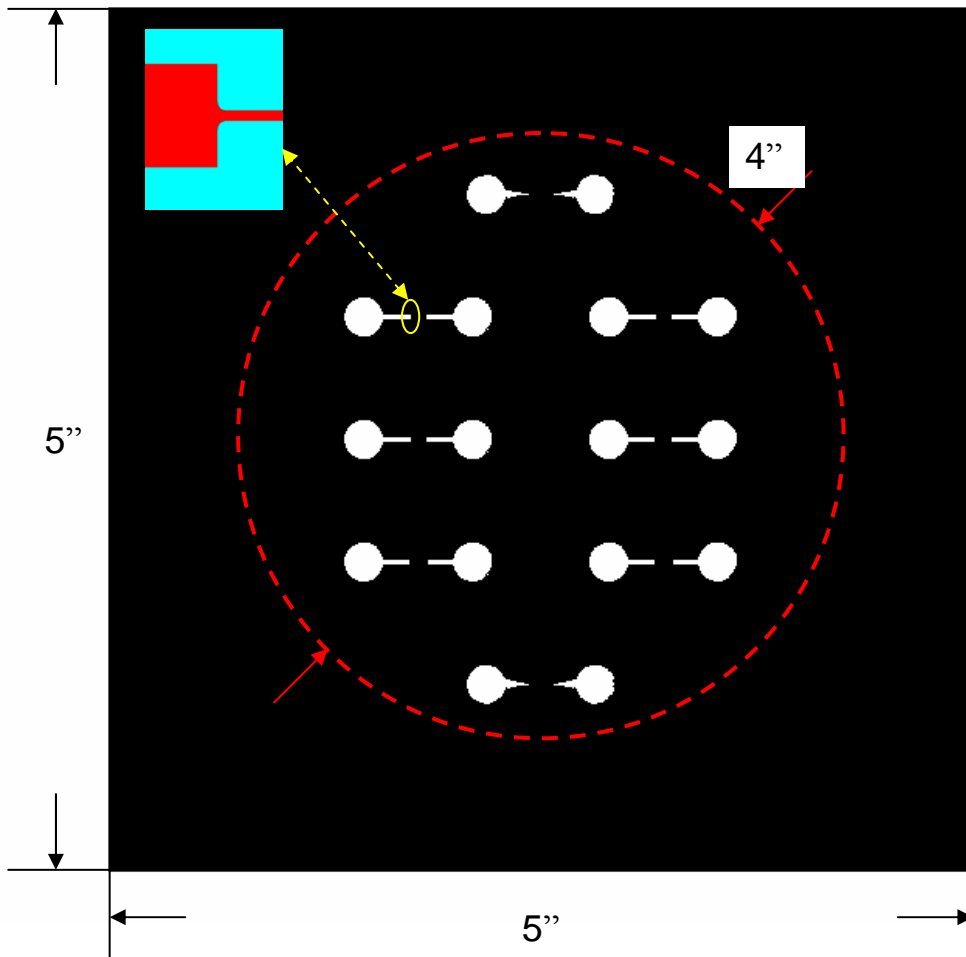
**Table 2** Theoretical value for micro channels

$2a = 50\mu m$				
$\mu$ (cp)	1.8	1.8	30	30
$Q$ (ml/min)	0.5	0.1	0.5	0.1
Max $\gamma$ ( $s^{-1}$ )	20000	4000	20000	4000
$Re_{D_h}$	0.1	0.02	$6*10^{-3}$	$1*10^{-3}$
$t$ (ms)	2	9	2	9
$2a = 150\mu m$				
$\mu$ (cp)	1.75	1.75	30	30
$Q$ (ml/min)	0.5	0.1	0.5	0.1
Max $\gamma$ ( $s^{-1}$ )	10000	2000	10000	2000
$Re_{D_h}$	0.06	0.01	$4*10^{-3}$	$0.7*10^{-3}$
$t$ (ms)	6	30	6	30

### 2.2.1.3 Mask design

CorelDRAW (CorelDRAW Graphics Suite 12, Corel Corp., Ottawa, ON) was used to draw the computer drafting file of the mask (fig.5). The size of the mask depends on the characteristic size of the mask holder in the photolithography equipment. In this case, it is a 5×5 inch square. The pattern also needs to be inside a circle, which is homocentric with the mask and whose size is as the same as the silicon wafer. The wafer used in this experiment has a diameter of 4 inches.

The computer file was sent to Magna Graphics Inc. (Pittsburgh, PA), a local company, to be printed out on a transparency using a 3400 DPI high resolution commercial printer. In this case, because we choose SU-8 (SU-8 2075, MicroChem Corp., Newton, MA), a negative tone photoresist, the transparency needs to be printed out positively, which means white area on CorelDRAW file should be clear on the transparency.



**Fig. 5** Channel pattern on mask

#### 2.2.1.4 Mold fabrication

A 5×5 inch square glass plate was used to hold the transparency, which is otherwise too soft to be put on the mask holder in the etching equipment. Margins were justified and the two parts were fixed by placing tape on the edges. Before the transparency and the glass plate were arranged together, both of them were cleaned to remove dust.

Mechanical grade silicon wafers (University Wafer Inc., South Boston, MA) were etched in the clean room of University of Pittsburgh. Since any dust or dirt on the surface of wafer may cause serious problem on SU-8 coating thus causing the whole process to fail, wafer needs to be extremely clean before being put on the spin coater. A process called piranha etch was used to completely clean the wafer. A clean solution was made by mixing sulphuric acid (Mallinckrodt Baker, Inc., Phillipsburg NJ) and hydrogen peroxide together by a ratio of 3:1 by volume. The wafer was washed in the mixture for five minutes and rinsed by deionized (DI) water for ten minutes. The DI water on the surface was blown off by air duster. Then, the wafer was placed on hot plate for five minutes at a temperature of 200°C.

**a) Spin coat**

After pretreating, the wafer was put on the spin coater (Karl Suss RC8, Suss MicroTec Inc., Waterbury Center, VT). About 5ml of SU-8 was poured at the center of wafer, using caution to avoid inducing air bubbles. The spin coater was set to 1600rpm for 30 seconds, after which the SU-8 was distributed evenly and became a thin film on the surface.

**b) Soft bake**

The SU-8 on the wafer surface was soft baked before exposure to UV light. Initially, the wafer was baked for 5 minutes on the hot plate with a temperature of 65°C. Then, the temperature of the hot plate was increased to 95°C at an increasing rate of 2°C/min. The wafer was continuously baked at 95°C for 40 minutes.

**c) Exposure**

The mask and the soft baked silicon wafer were placed at proper locations with respect to the UV lamp (Karl Suss MA6, Suss MicroTec Inc., Waterbury Center, VT). The UV light was turned on and the wafer was exposed for 30 seconds.

**d) Post expose bake**

After being exposed, the wafer underwent a post expose bake on the hot place for 1 minute at 65°C and for 15 minutes at 95°C.

**e) Develop**

About 20ml SU-8 developer (MicroChem Corp., Newton, MA) was poured into a glass tray and placed in the developer for ten minutes. The SU-8 in non-exposed areas was washed out during this process, while the SU-8 in exposed areas remained on the surface and became hard. After being developed, the wafer was washed in Isopropyl Alcohol to remove SU-8 developer. After washing, the wafer surface should be bright and clean. If there is a white film on the surface, it means some SU-8 has not been fully developed and still remained on the wafer surface. In that case, the wafer needs to be developed again in a new SU-8 developer. After being washed in IPA solution, the wafer was washed by DI water to get rid of IPA on surface.

**f) Hard bake**

Finally, the mold was put on the hot plate and baked for 30 minutes at 200°C. The purpose of this process is to harden the pattern on the mold.

### **2.2.1.5 PDMS curing**

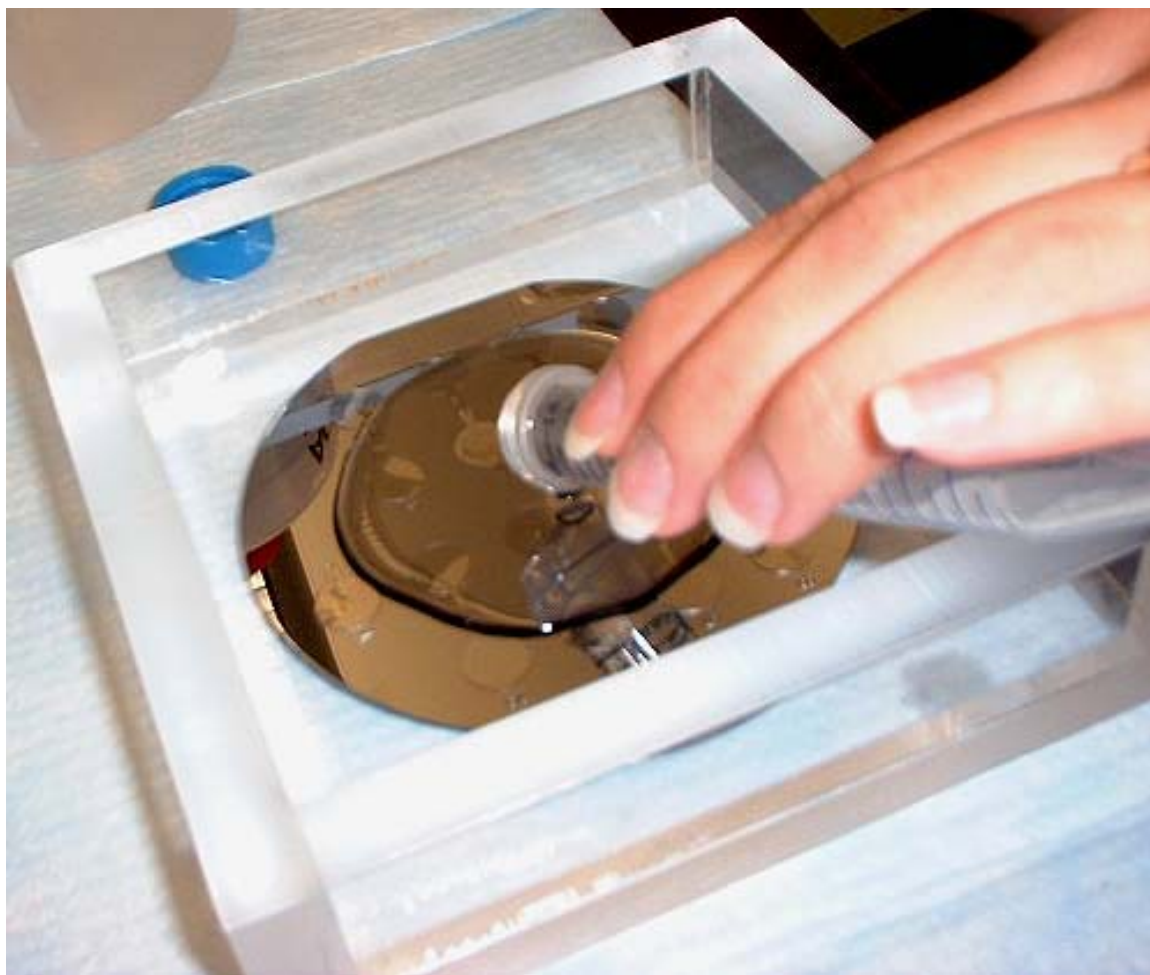
PDMS (Sylgard 184, Dow Corning Corp., Midland, MI) was made by mixing silicon elastomer base and curing agent in a 10:1 ratio by weight. The mixture was then centrifuged for about 20 seconds to remove air bubbles due to the reaction during mixing. Silicon mold was placed in the center of a container. PDMS was poured over the mold in the center slowly, to avoid inducing more bubbles (fig.6a).

The container was placed in a vacuum oven for further removal of bubbles. The vacuum pump was turned on until the pressure inside decreased to -23 in. Hg. The low pressure remained steady for 2 minutes. During this period, the air bubbles were seen swelling and floating to the surface of PDMS. After 2 minutes, the pressure was increased quickly to pop as many bubbles as possible. The process was repeated several times until the majority of small bubbles had gone. After removing from the container, large air bubbles that were still in the PDMS were popped manually with a small needle. The container was then heated at 60°C for four hours to cure the PDMS. Cured PDMS was removed from container by loosening edges with a scraping tool. This step was done very carefully, avoiding breaking the mold. After the PDMS piece was successfully separated from mold, it was cut to individual channels to fit into the channel shell. Two reservoir holes were punched assuming smooth edges.

### **2.2.1.6 Oxygen plasma treatment**

The channel was sealed with a glass slide by oxygen plasma treatment [47], which was conducted in the laboratory of Dr. Shelley Anna from Department of Chemical Engineering, at

Carnegie Mellon University (CMU). Both glass slide and channel had been completely cleaned with detergent, DI water and acetone before the treatment. Then, they were placed in the plasma cleaner (Harrick PFC-32G, Harrick Scientific Corp., NY) for 1 minute and put together quickly after being taken out (fig.6).



**(a)**



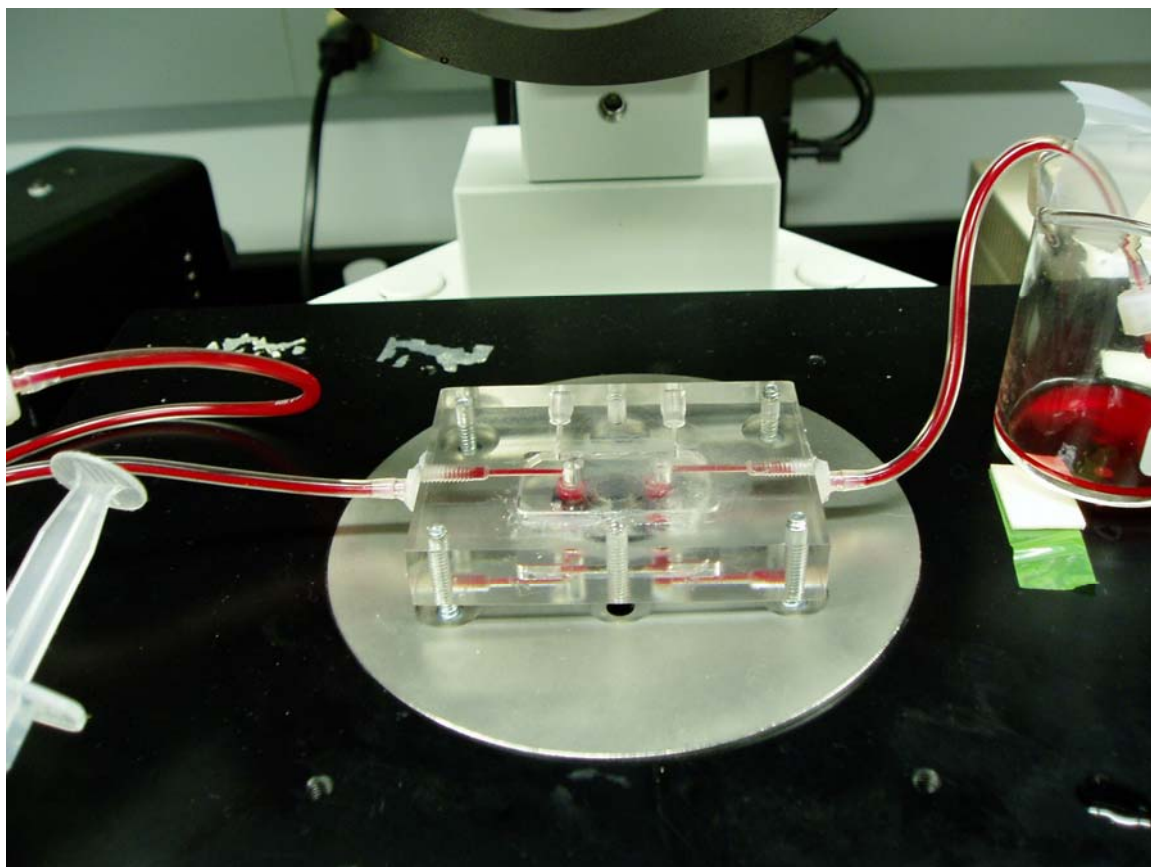
(b)

**Fig. 6** Micro channel fabrication, a: PDMS pouring, b: micro channels after plasma treatment

### 2.2.2 Flow chamber design

A polycarbonate flow chamber (fig.7) was designed to hold the PDMS micro channel and give an easy optical pathway. The back side of PDMS piece was stuck under the chamber by silicon glue. The surfaces of chamber were polished to give a good optical pathway. The flow chamber was fixed on the stainless steel plate, which was specifically designed for the chamber, with four

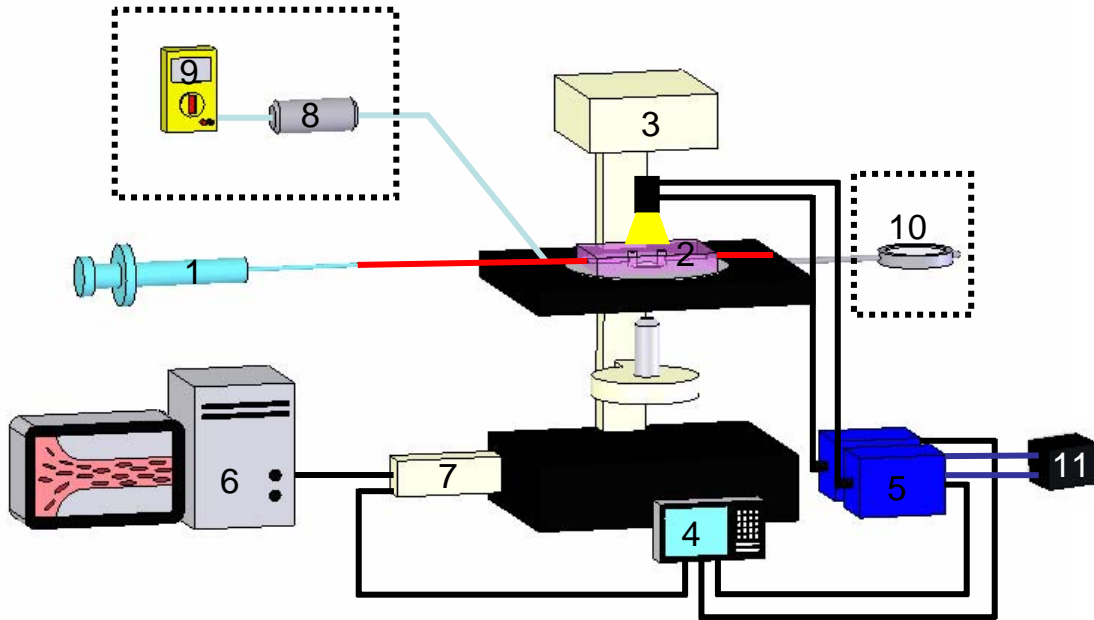
screws. The plate was fitted to the hole on the microscope stage. The channel through camera can be easily adjusted to be parallel to the image frame by circling the plate. The four screws were helpful in making the whole image field focused. Input and output tubing were connected and sealed with silicon glue.



**Fig. 7** Flow chamber on microscope stage



### 2.3 EXPERIMENTAL SETUP



**Fig. 8** Experimental set up, 1: plastic syringe, 2: flow chamber and channel, 3: inverted microscope, 4: pulse generator, 5: stroboscope, 6: computer and frame grabber, 7: camera, 8: pressure transducer, 9: multimeter, 10: dial indicator, 11: voltage controller

The overall experimental setup is shown in figure 8. In the experiment, blood was loaded in a 10ml plastic syringe ((1), Becton, Dickinson and Company, Franklin Lakes, NJ), which was driven by a syringe pump. The blood was pushed through the micro channel and collected in a reservoir. The flow chamber (2), with PDMS micro channel underneath, was fixed on the stage of an inverted microscope ((3), Olympus IX70, Olympus, Melville, NY). Both chamber and PDMS piece were transparent to allow sufficient light transmission. A digital camera ((7), Princeton Instruments MicroMax, Roper Scientific Inc., Rochester, NY) was hooked up to the microscope to capture the image from objective to the frame grabber on a computer (6).

Two stroboscopes ((5), X400, PerkinElmer Optoelectronics Inc., Wellesley, MA) were used as illuminators, which were connected in parallel by a two-in-one fiber-optic cable with the output end fixed above the chamber. A voltage controller (11) was connected to both of the stroboscopes in order to make the two output beam intensities approximately equal to each other. Both the stroboscopes and the camera were connected to a pulse generator ((4), BNC500, Berkeley Nucleonics Corp. San Rafael, CA) to be synchronized. A pair of images, with a very short separation time between them, was captured by camera. Each of them was illuminated by one of the two stroboscope beams.

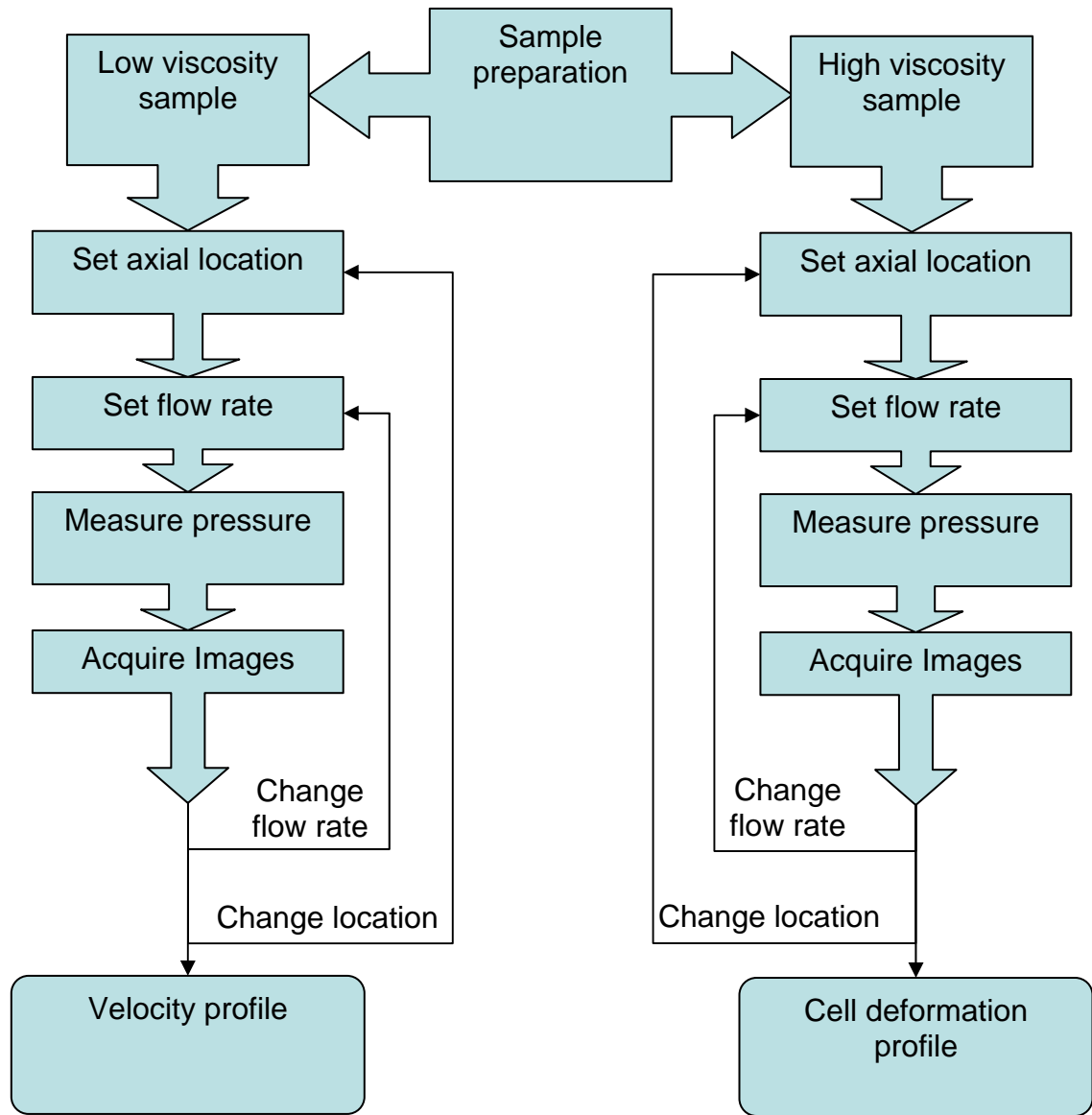
### **2.3.1 Experimental plan**

Figure 9 shows the overall experimental strategy. Low and high viscosity samples were mainly used to obtain velocity profile and cell deformation profile, respectively. A dial indicator (10) was placed on one side of the stage to measure the axial location. The zero point was set as the inlet edge was on the left side of image frame on computer screen. The accuracy of the dial is 0.001 inches, which equal to 25.4 $\mu$ m. After setting the image to a specified location, blood was pushed with different flow rates. In each flow rate, pressure was measured from a port which was close to the tubing-chamber connection by a pressure transducer (8) and 10 pairs of images were acquired.

Both 40 $\times$  and 100 $\times$  magnification objectives were used in the experiments. The 40 $\times$  objective (Olympus UPlanFL, 40 $\times$ , NA=0.75) was mainly used to capture images for calculating velocity profile, while the 100 $\times$  (Olympus UPlanFL, 100 $\times$ , NA=1.30) was used to observe the cell

deformation. In this experiment, because the cover glass was very thin, it was possible to use objective with a relatively short working distance.

Table 3 shows the location and flow rate used in the experiments. For the high viscosity sample at flow rate of 0.05, 0.1 and 2 ml/min, the microscope stage was moved from 2mm before channel inlet to 2 mm after the channel outlet, and images were taken from 30 locations with a distance of 0.008 inches (about 200 $\mu$ m). The protocol allowed us draw a dynamic picture of RBCs from the collector to diffuser.



**Fig. 9** Experimental strategy

**Table 3** Experimental plan

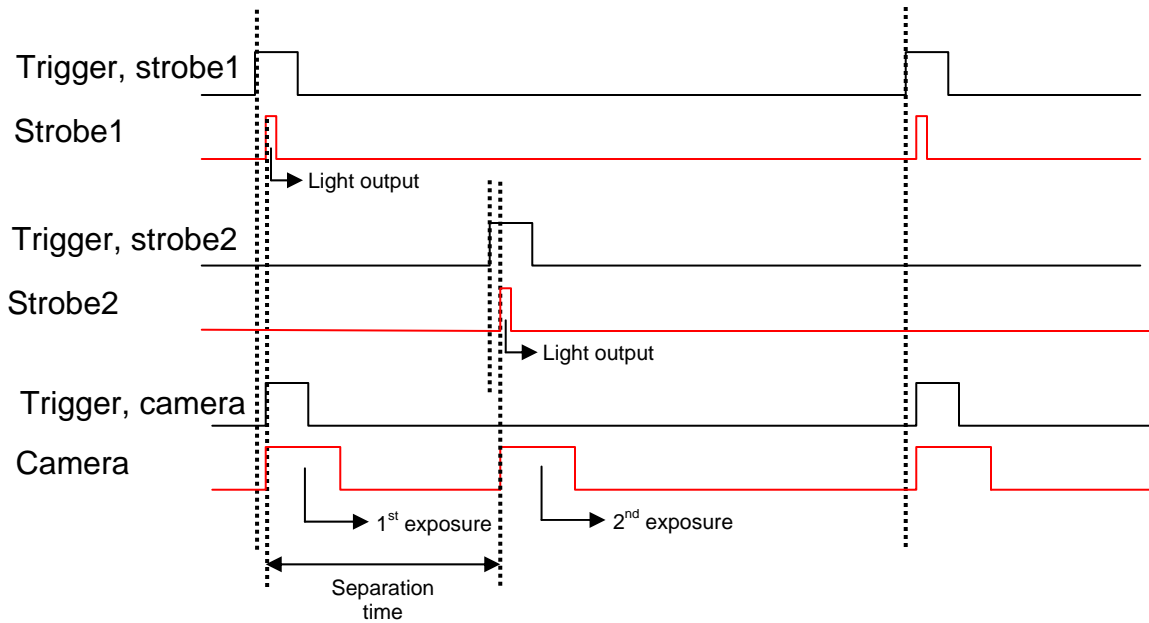
Flow rate (ml/min)	Low viscosity sample		High viscosity sample (30 locations in x direction)				
	Channel inlet	Inside channel	x=-2mm	...	x=1mm (Inside channel)	...	x=4mm
0.05			10 pairs of image deformation	10 pairs of image each location deformation	10 pairs of image deformation	10 pairs of image each location deformation	10 pairs of image deformation
0.1			10 pairs of image deformation	10 pairs of image each location deformation	10 pairs of image deformation	10 pairs of image each location deformation	10 pairs of image deformation
0.2	10 pairs of image velocity	10 pairs of image velocity	10 pairs of image deformation	10 pairs of image each location deformation	10 pairs of image deformation	10 pairs of image each location deformation	10 pairs of image deformation
0.3					10 pairs of image deformation		
0.4	10 pairs of image velocity	10 pairs of image velocity			10 pairs of image deformation		
0.5					10 pairs of image deformation		
0.6	10 pairs of image velocity	10 pairs of image velocity					
0.8	10 pairs of image velocity	10 pairs of image velocity					
1.0	10 pairs of image velocity	10 pairs of image velocity			10 pairs of image deformation		
2.0					10 pairs of image deformation		

### 2.3.2 System synchronization

The camera and two stroboscopes needed to be synchronized. A four channels pulse generator was used to generate external trigger signals for stroboscopes and camera. A proper timing sequence was needed according to the characteristic of stroboscopes and camera. The factors affecting the timing sequence, such as the delay time between external signals and illuminator light, the illuminator pulse duration and camera intrinsic timing, were considered to set up the timing sequence.

For the camera, an external signal was used to trigger the first exposure. The exposure time and the separation time between two exposures were set by the WinView software. After the separation time, the second exposure was started. There is no need to generate a trigger signal for the second exposure. Timing sequence for the experiment is illustrated in figure 10. There is a  $10\mu\text{s}$  delay time between trigger signal and strobe light. The light duration is  $8\text{-}10\mu\text{s}$ . There is also a  $200\text{ns}$  intrinsic time between the increasing edge of camera trigger signal and camera exposure, which is too small to show in the figure.

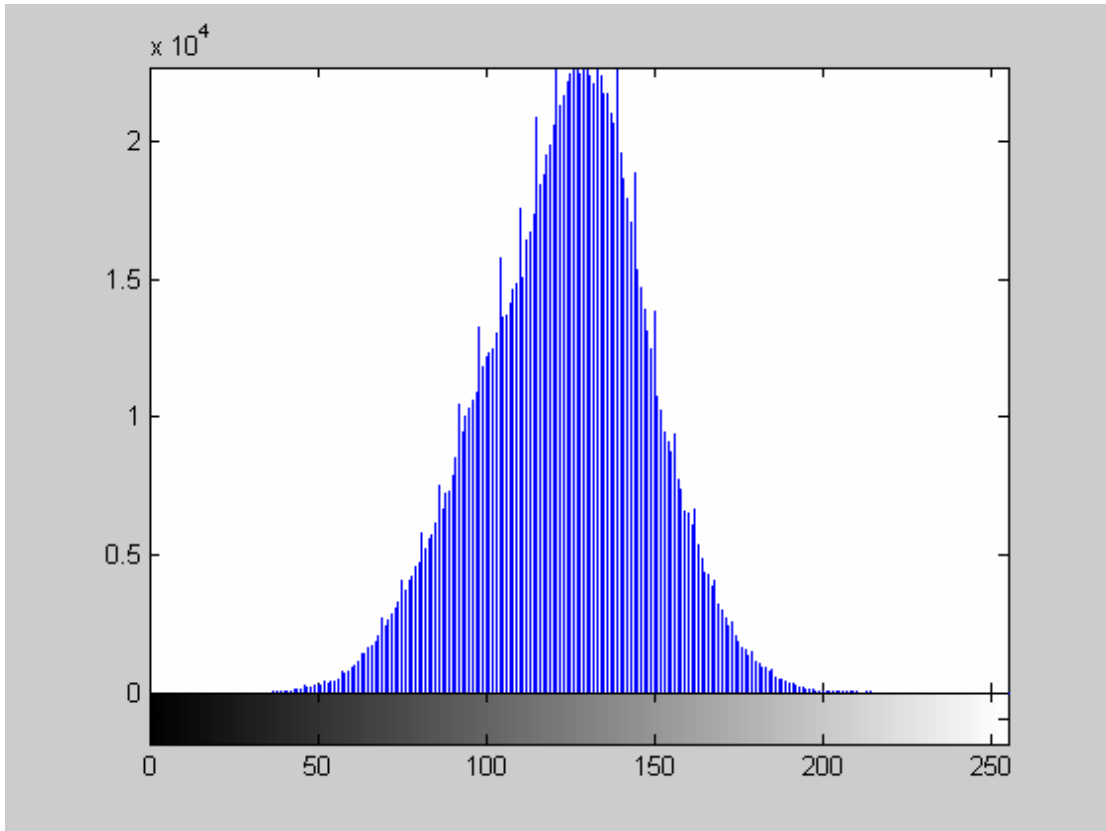
The exposure time and separation time needed to be properly set according to the experimental conditions. Due to the light output duration of stroboscopes, the separation time could not be shorter than  $10\mu\text{s}$ . The exposure time was set according to the image qualities on the computer screen. The location of the fiber-optic head and the intensity adjustment controller also contributed to the image qualities.



**Fig. 10** Timing sequence for the experiment

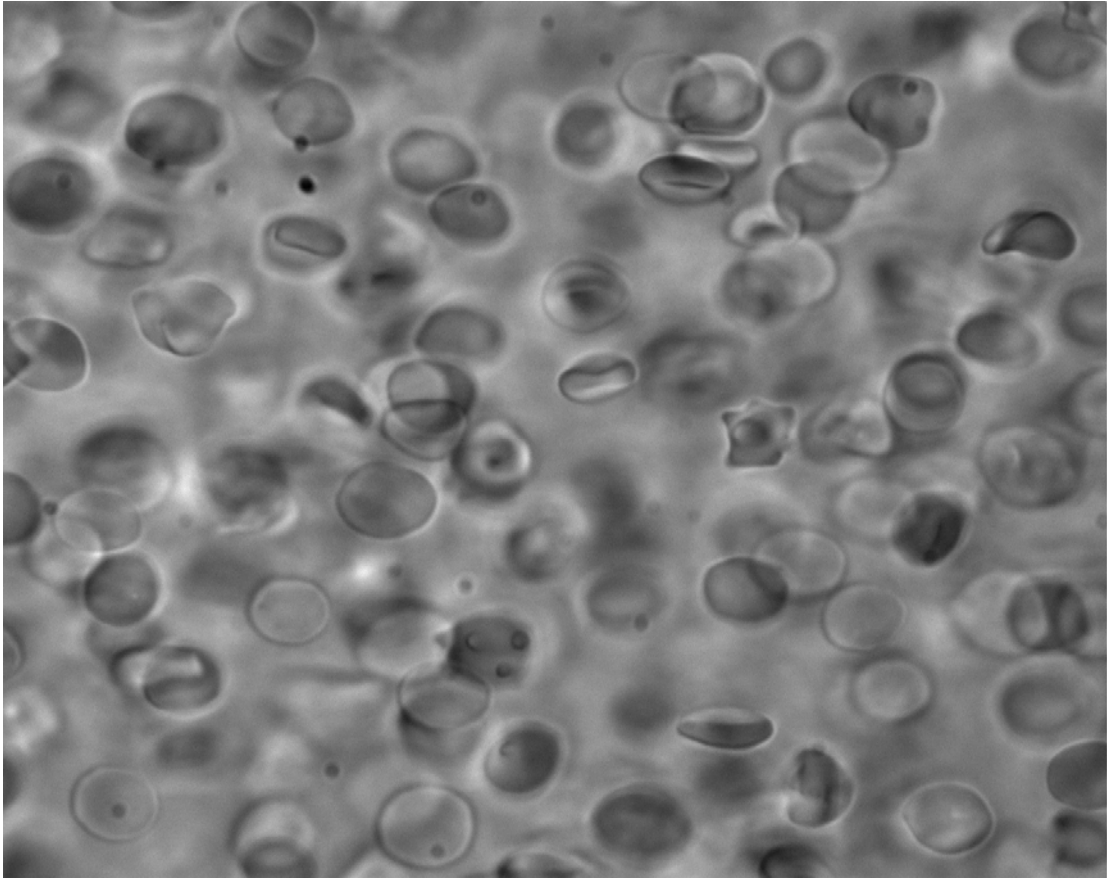
## 2.4 IMAGE PROCESSING

Matlab (MathWorks Inc., Natick, MA) Image Processing Tool Box was used to write image processing program (“separation.m” in Appendix). The histogram of a typical original image was shown in figure 11. In this histogram, the pixels concentrated in [40,210] gray level instead of covering the whole extent of gray level. The limit of gray level gradient made the image have a poor contrast between the interested object and background (fig.12). The image was equalized by setting all the non frequency gray level to either zero or 255 and widening other pixel gray level distributions proportionally to their originally ones. That allows the diversity be enlarged so that contrast was improved (fig.13, fig.14).

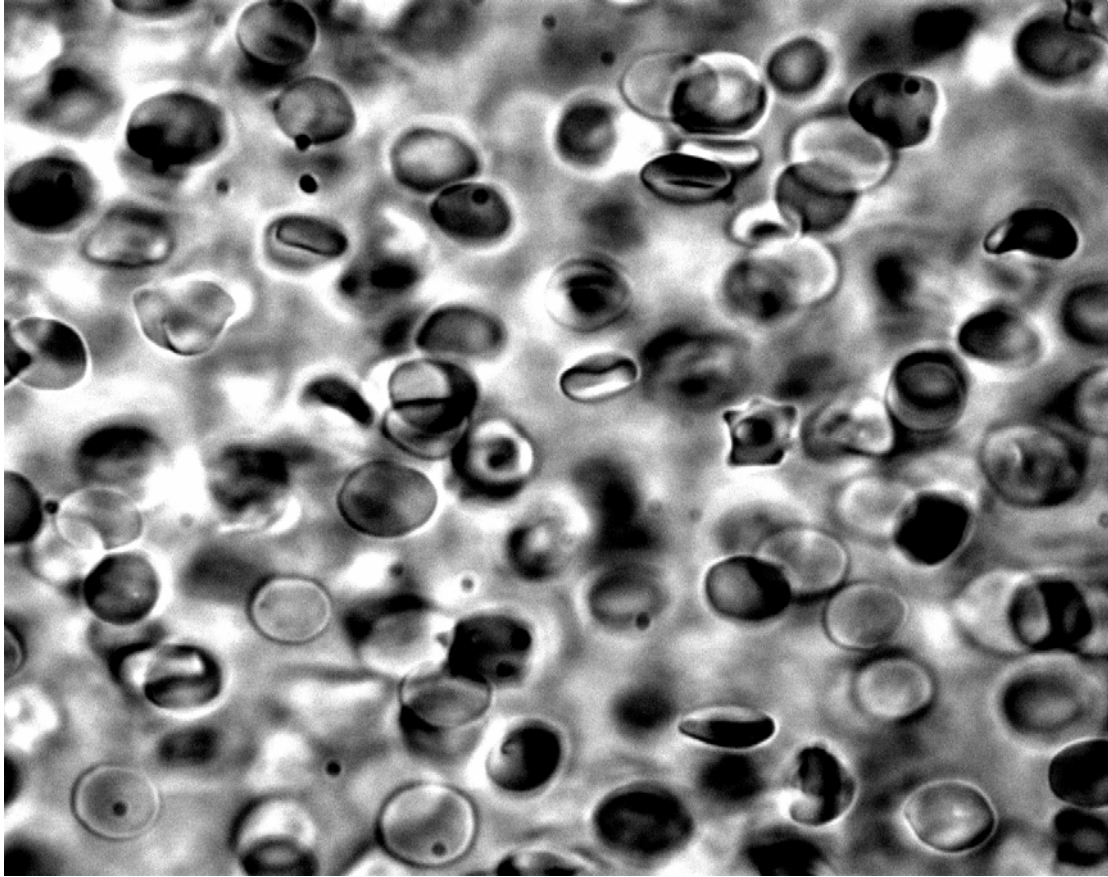


**Fig. 11** Histogram of original image

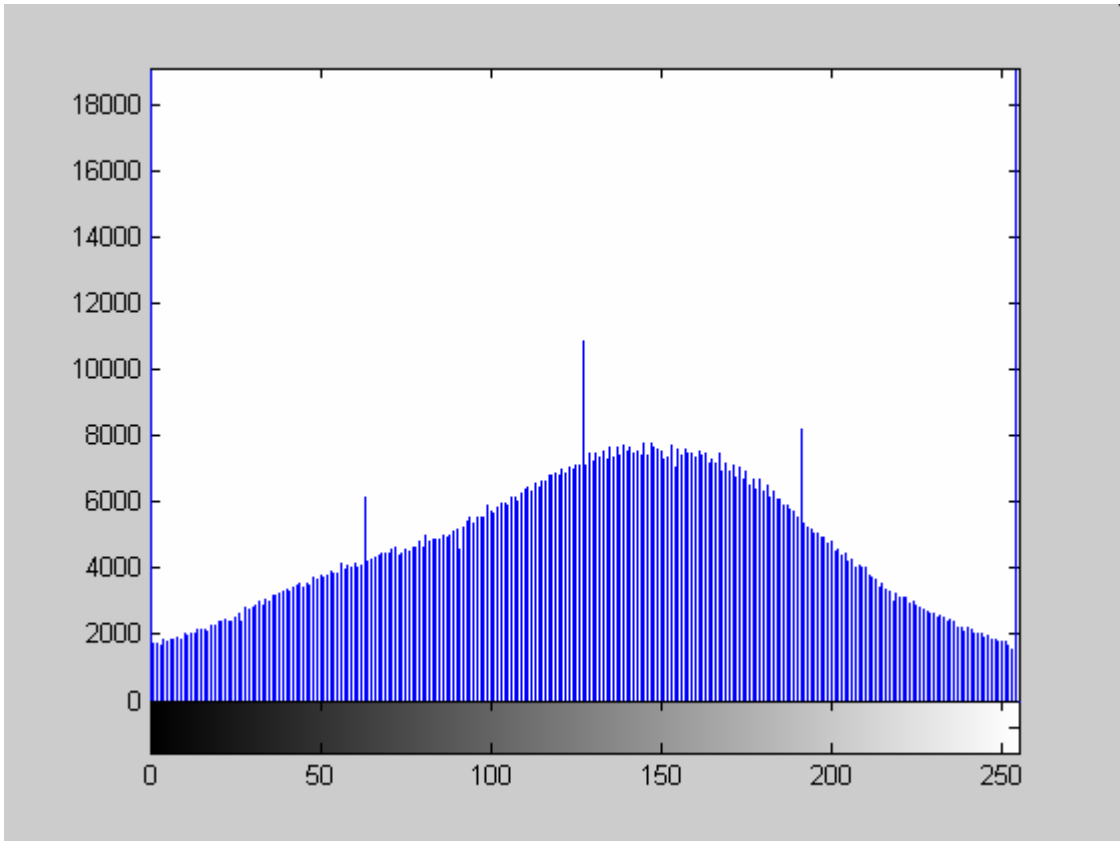




**Fig. 12** Original image



**Fig. 13** Enhanced image



**Fig. 14** Histogram of enhanced image

## **2.5 DATA ANALYSIS**

### **2.5.1 Velocity profile**

#### **2.5.1.1 Particle image velocimetry**

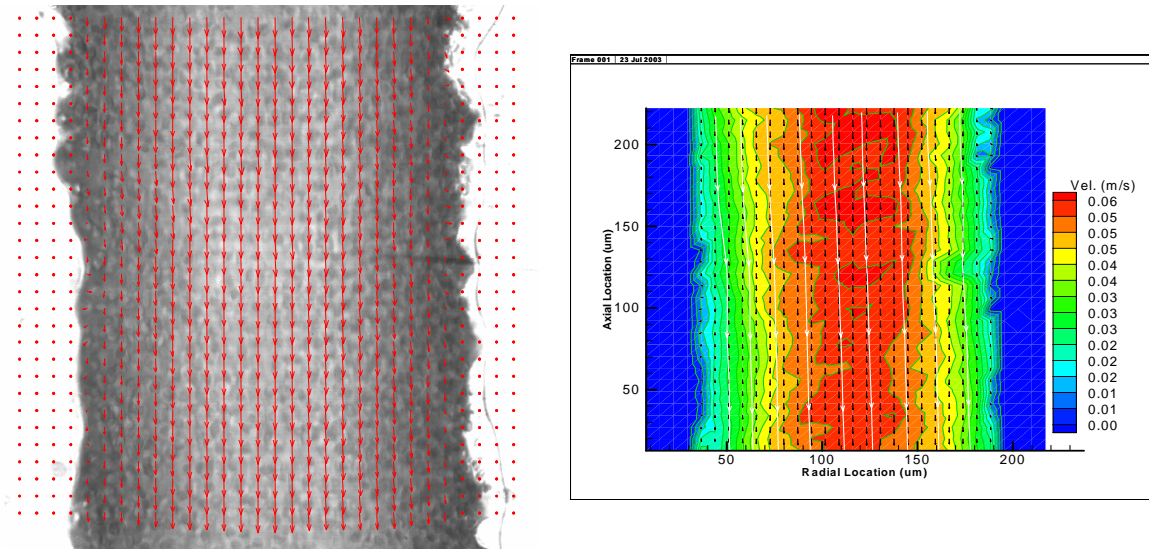
Particle image velocimetry (PIV) was used to measure the two-component velocity field of blood flow in the x-y plane. In PIV, image was separated to a matrix of subregions named interrogation

windows. The average displacement of tracer particles in each interrogation window was measured. Velocity was calculated using equation 7.

$$V = \frac{\Delta x}{M \cdot \Delta t} \tag{5}$$

Where,  $\Delta x$  is the average displacement of tracer particles,  $M$  is the optical system magnification and  $\Delta t$  is the separation time.

In this experiment, red blood cells were regarded as tracer particles, by assuming they were small enough to follow the flow accurately. Images taken with a 40× objective were used to measure velocity profile and were separated to a matrix of 64×64 pixel interrogation windows. Figure 15 is the typical velocity profile extracted from experiment. It shows that this experimental setting is good enough to measure velocity profiles on x-y plane.



**Fig. 15** a typical velocity profile on x-y plane

### 2.5.1.2 Cross-correlation algorithm

For Particle image velocimetry, it is impossible to track individual particles. The average displacement of tracer particles needed to be calculated statistically. In this experiment, double frame/single exposure images were taken and cross-correlation algorithm was used to calculate the average displacement of tracer particles in each interrogation window. The definition of cross-correlation function for digitally recorded images is:

$$R_{fg}(i, j) = f(i, j) \otimes g(i, j) = \sum_{x=0}^M \sum_{y=0}^N f(i, j)g(x-i, y-j) \quad (6)$$

Where,  $R_{fg}(i, j)$  is the intensity of the  $(i, j)^{\text{th}}$  pixel on resulting cross-correlation image,  $f(i, j)$  and  $g(i, j)$  are the intensity of the  $(i, j)^{\text{th}}$  pixel on the pair of original images.  $M$  and  $N$  are the x and y dimension of interrogation windows, respectively.

The function is normalized to remove the effect of brightness variation:

$$R_{fg}(i, j) = \frac{\sum_{x=0}^M \sum_{y=0}^N [f(x, y) - \bar{f}][g(x-i, y-j) - \bar{g}]}{\sigma_f \sigma_g} \quad (7)$$

Where,  $\bar{f}$  and  $\bar{g}$  are the average intensity value of the images.  $\sigma_f$  and  $\sigma_g$  are their standard deviations. The normalized  $R_{fg}(i, j)$  is varied between -1 and 1.

The cross-correlation function can be considered as the combination of correlation between particle pairs and correlation between different particles, which are called random correlations. The particle-pairs correlation is constant and will generate a peak which is much higher than the

peak generated by random correlations. According to the algorithm, the distance between this peak and the center of the cross-correlation image is the average displacement of tracer particles.

### **2.5.1.3 Velocity profile**

A software, PIVPROC (Glenn Research Center, NASA), was used to process the displacement data using cross-correlation algorithm. This software can generate a .VEC file whose format which can be read by TechPlot.

A  $15 \times 19$  data matrix was generated, in which each node is denoted as the average displacement of one  $64 \times 64$  interrogation window. The two-dimension location of each node was also recorded in the data file.

### **2.5.1.4 Cell deformation profile**

Matlab program (AppendixA) was used to measure cell deformation. The two cell length ends were picked up manually, according to the observed cell edge. The two dimension cell elongation data and cell location data were generated through Matlab program.

## **2.5.2 Post data processing**

Data was post processed using Matlab. All data were saved in specified “.txt” files for further using. For cell displacement data generated by PIVPROC, the mean and standard deviation displacement in each interrogation window was created by averaging data from ten images. For

cell displacement inside channels, the data from the same row were further averaged assuming there was no velocity change in x direction. Before averaging the data from the same row, the zero data and those data with angles more than  $10^\circ$  departure from x axis, which were regarded being generated by mistake, were excluded from results(AppendixB). After averaging data, the displacement data was converted to the velocity data by dividing the separation time between images. Shear rate data were generated from velocity data. For cell deformation data, the average cell deformation in one location was generated by averaging all the cell deformations in ten images.

### 3.0 RESULTS

#### 3.1 PRESSURE CONDITION

The input pressure of both the high viscosity sample and the low viscosity sample was measured and recorded (fig.16). The pressure increased linearly ( $R^2 > 0.99$ ) as flow rate increasing in both sample. The slopes were very close to each other (12.3 vs 12.1). These results showed that the experimental conditions were not changed in these two sets of experiments and there was no micro channel expansion due to too much pressure in both experiments.

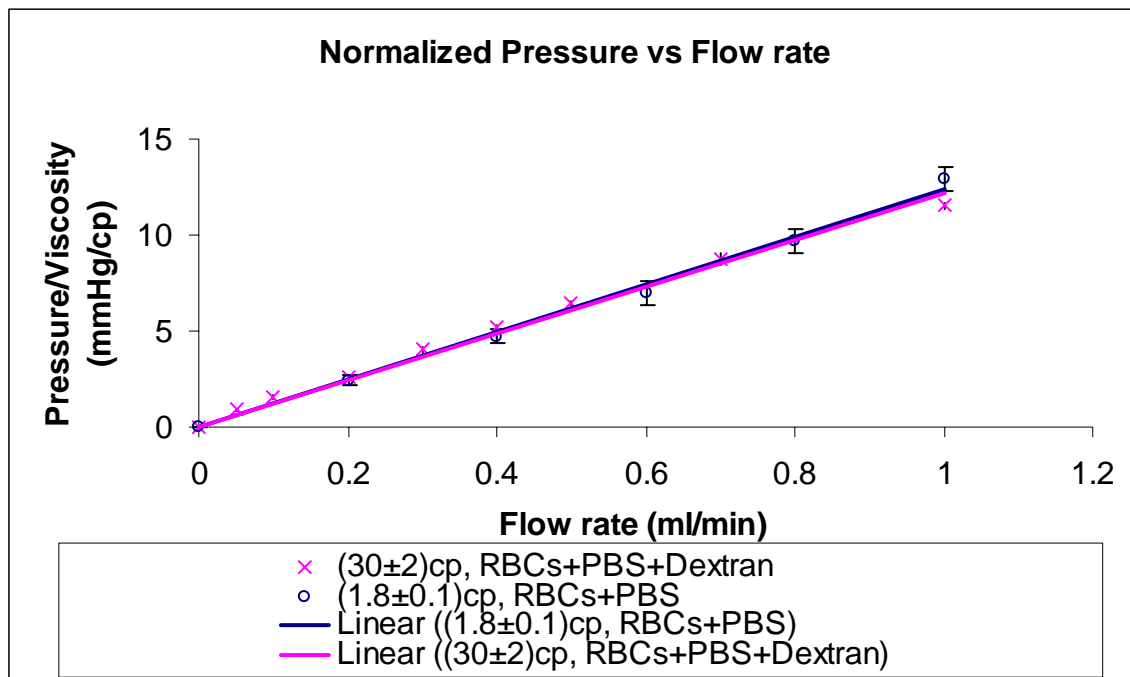


Fig. 16 Normalized pressure/flow rate in channel with 150µm width



## 3.2 FLOW STATUS

### 3.2.1 A few definitions

Before analyzing fluid flow conditions, we need to specify the equation and definition to describe the flow field. First of all, we need to make some assumptions for the flow conditions.

We assume the sample is an incompressible Newtonian fluid. Also, we assume that we look for a local model when stress depends only on the local gradient of the flow.

We define  $\underline{\underline{E}}$  as the strain rate tensor. Then

$$\underline{\underline{E}} = \frac{1}{2}(\nabla \underline{V} + \nabla \underline{V}^T) \quad (8)$$

Where,  $\underline{V}$  is the velocity vector [48]. For a 3-D flow

$$\underline{V} = [V_x \quad V_y \quad V_z] \quad (9)$$

$$\underline{\underline{E}} = \frac{1}{2} \left( \begin{bmatrix} \frac{\partial V_x}{\partial x} & \frac{\partial V_x}{\partial y} & \frac{\partial V_x}{\partial z} \\ \frac{\partial V_y}{\partial x} & \frac{\partial V_y}{\partial y} & \frac{\partial V_y}{\partial z} \\ \frac{\partial V_z}{\partial x} & \frac{\partial V_z}{\partial y} & \frac{\partial V_z}{\partial z} \end{bmatrix} + \begin{bmatrix} \frac{\partial V_x}{\partial x} & \frac{\partial V_y}{\partial x} & \frac{\partial V_z}{\partial x} \\ \frac{\partial V_x}{\partial y} & \frac{\partial V_y}{\partial y} & \frac{\partial V_z}{\partial y} \\ \frac{\partial V_x}{\partial z} & \frac{\partial V_y}{\partial z} & \frac{\partial V_z}{\partial z} \end{bmatrix} \right) \quad (10)$$

$$\underline{\underline{E}} = \frac{1}{2} \begin{bmatrix} 2\frac{\partial V_x}{\partial x} & \frac{\partial V_x}{\partial y} + \frac{\partial V_y}{\partial x} & \frac{\partial V_x}{\partial z} + \frac{\partial V_z}{\partial x} \\ \frac{\partial V_y}{\partial x} + \frac{\partial V_x}{\partial y} & 2\frac{\partial V_y}{\partial y} & \frac{\partial V_y}{\partial z} + \frac{\partial V_z}{\partial y} \\ \frac{\partial V_z}{\partial x} + \frac{\partial V_x}{\partial z} & \frac{\partial V_z}{\partial y} + \frac{\partial V_y}{\partial z} & 2\frac{\partial V_z}{\partial z} \end{bmatrix} \quad (11)$$

We define two simple flow models: shear flow and extensional flow. The strain rate is the off diagonal component for shear flow.

The strain rate expression caused by shear flow

$$\underline{\underline{E}}_{shear} = \frac{1}{2} \begin{bmatrix} 0 & \frac{\partial V_x}{\partial y} + \frac{\partial V_y}{\partial x} & \frac{\partial V_x}{\partial z} + \frac{\partial V_z}{\partial x} \\ \frac{\partial V_y}{\partial x} + \frac{\partial V_x}{\partial y} & 0 & \frac{\partial V_y}{\partial z} + \frac{\partial V_z}{\partial y} \\ \frac{\partial V_z}{\partial x} + \frac{\partial V_x}{\partial z} & \frac{\partial V_z}{\partial y} + \frac{\partial V_y}{\partial z} & 0 \end{bmatrix} \quad (12)$$

The strain rate expression caused by extensional flow

$$\underline{\underline{E}}_{ext} = \begin{bmatrix} \frac{\partial V_x}{\partial x} & 0 & 0 \\ 0 & \frac{\partial V_y}{\partial y} & 0 \\ 0 & 0 & \frac{\partial V_z}{\partial z} \end{bmatrix} \quad (13)$$

The magnitude of  $\underline{\underline{E}}$  is defined as

$$|\underline{\underline{E}}| = \sqrt{\frac{1}{2}(\underline{\underline{E}} : \underline{\underline{E}}^T)} \quad (14)$$

$$|\underline{\underline{E}}| = \sqrt{\frac{1}{2}(E_{11}^2 + E_{12}^2 + E_{13}^2 + E_{21}^2 + E_{22}^2 + E_{23}^2 + E_{31}^2 + E_{32}^2 + E_{33}^2)} \quad (15)$$

[49]

For shear flow,

$$|\underline{\underline{E}}|_{shear} = \frac{1}{2} \sqrt{\left(\frac{\partial V_x}{\partial y} + \frac{\partial V_y}{\partial x}\right)^2 + \left(\frac{\partial V_z}{\partial y} + \frac{\partial V_y}{\partial z}\right)^2 + \left(\frac{\partial V_x}{\partial z} + \frac{\partial V_z}{\partial x}\right)^2} \quad (16)$$

For extensional flow,

$$|\underline{\underline{E}}|_{ext} = \sqrt{\frac{1}{2}[(\frac{\partial V_x}{\partial x})^2 + (\frac{\partial V_y}{\partial y})^2 + (\frac{\partial V_z}{\partial z})^2]} \quad (17)$$

For a Newtonian fluid, stress and strain rate have the relationship of  $\underline{\underline{\sigma}} = 2\mu\underline{\underline{E}}$ . The magnitude of stress can be denoted as

$$|\underline{\underline{\sigma}}|_{shear} = 2\mu|\underline{\underline{E}}|_{shear} = \mu\sqrt{(\frac{\partial V_x}{\partial y} + \frac{\partial V_y}{\partial x})^2 + (\frac{\partial V_z}{\partial y} + \frac{\partial V_y}{\partial z})^2 + (\frac{\partial V_x}{\partial z} + \frac{\partial V_z}{\partial x})^2} \quad (18)$$

$$|\underline{\underline{\sigma}}|_{ext} = \mu|\underline{\underline{E}}|_{ext} = 2\mu\sqrt{\frac{1}{2}[(\frac{\partial V_x}{\partial x})^2 + (\frac{\partial V_y}{\partial y})^2 + (\frac{\partial V_z}{\partial z})^2]} \quad (19)$$

For a flow inside channel,  $V_y = V_z = 0$ .  $|\underline{\underline{\sigma}}|_{shear}$  is simplified to

$$|\underline{\underline{\sigma}}|_{shear} = \mu|\underline{\underline{E}}|_{shear} = \mu\sqrt{(\frac{\partial V_x}{\partial y})^2 + (\frac{\partial V_x}{\partial z})^2} \quad (20)$$

### 3.2.2 Inside channel

#### 3.2.2.1 Velocity distribution across y direction

Figure 17 shows the mean velocity along the y direction for low and high viscosity samples in channel with 150 $\mu$ m width. The curve fit well to a parabolic curve ( $R^2 > 0.98$ ). The figure also shows the 5<sup>th</sup> order polynomial regression of the data, which could be accurate to  $R^2 = 0.999$ . It shows that the bluntness only has slight effect near wall. We can get the shear rate component

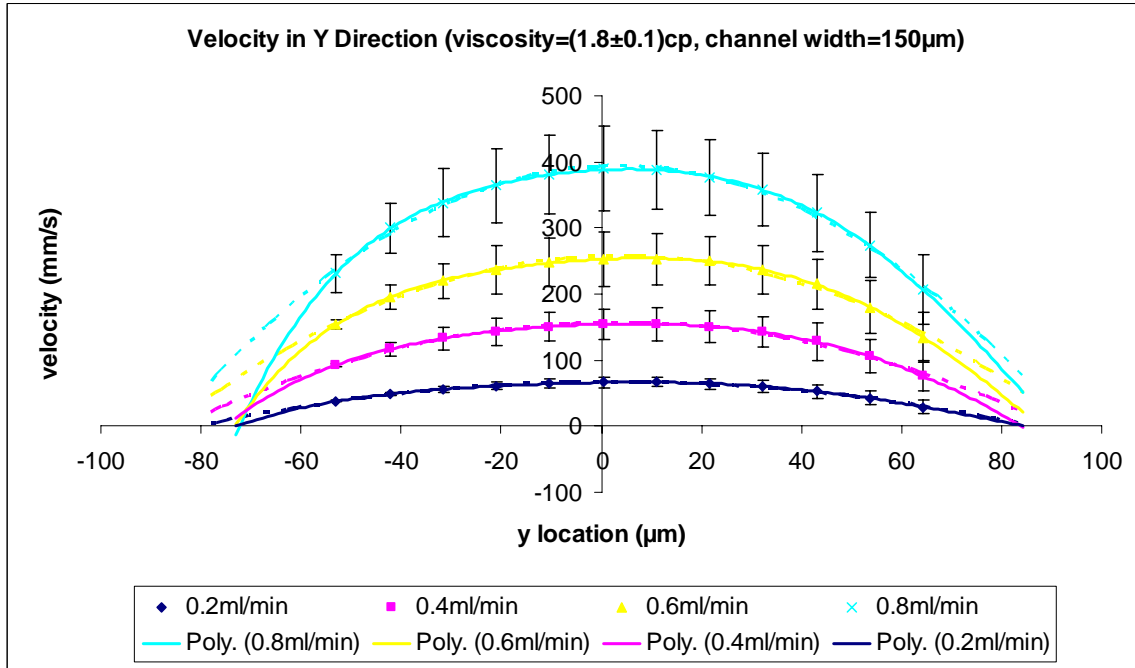
$\frac{\partial V_x}{\partial y}$  from velocity profile. To simplify the problem, we assume a parabolic velocity profile,

regardless the very small bluntness due to the cross section geometry. The velocity data were

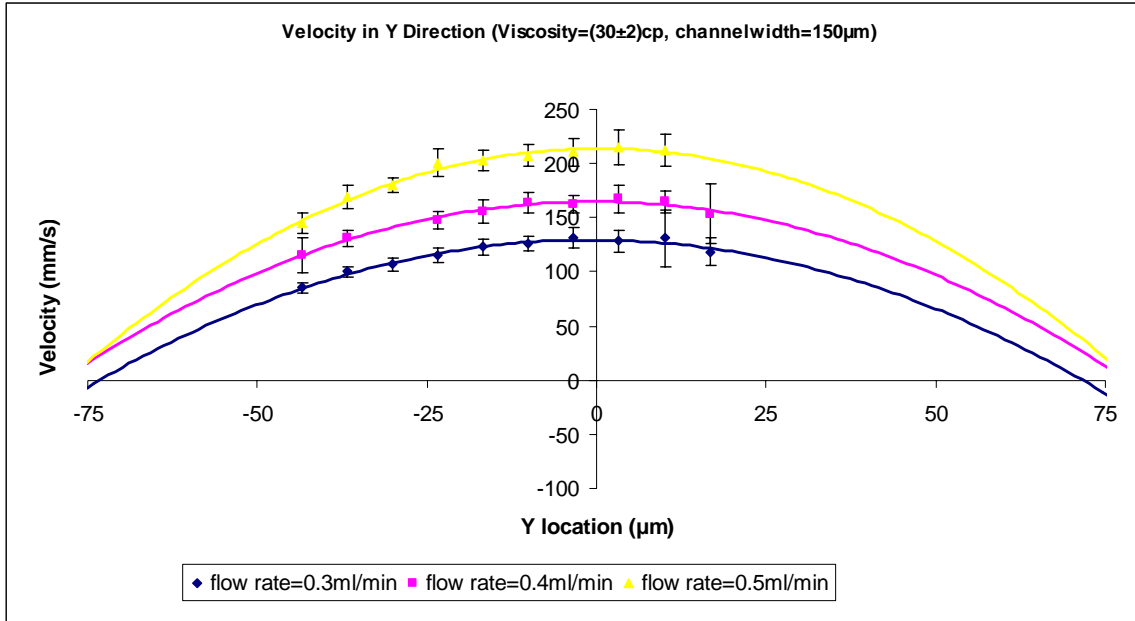
smoothed to the second order polynomial curve when they were used to calculate shear rate

$\frac{\partial V_x}{\partial y}$  profile. By this assumption, we can get a linear shear rate profile and it will be easier for the

analysis afterwards.



(a)

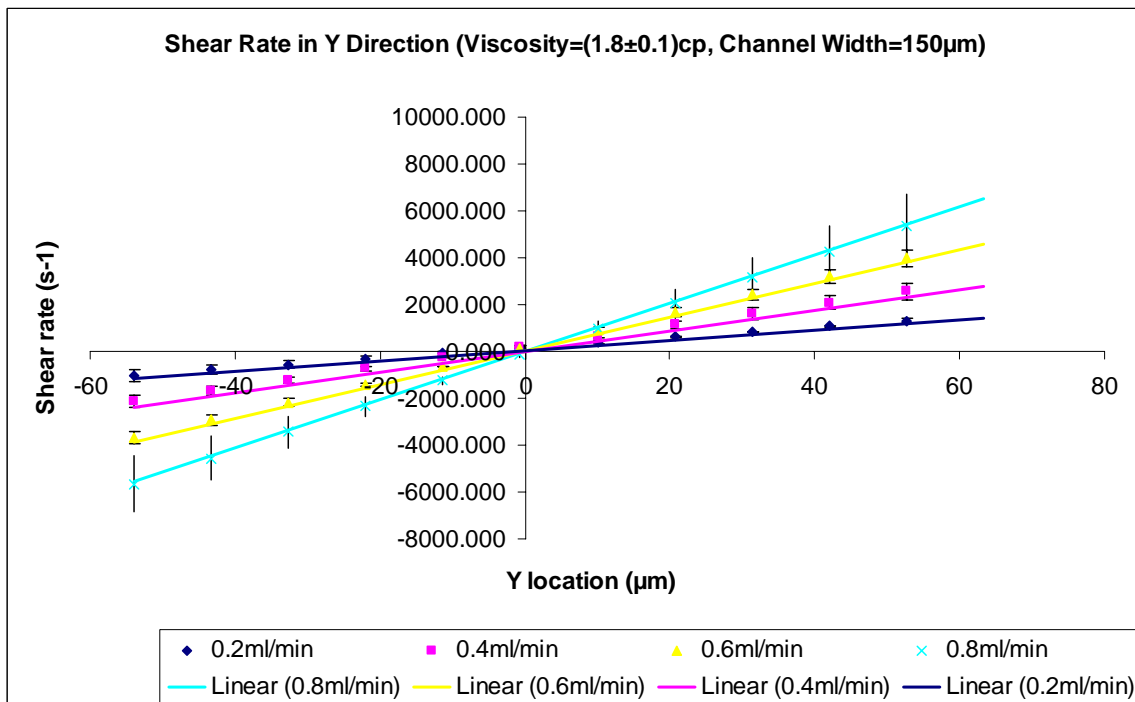


**(b)**

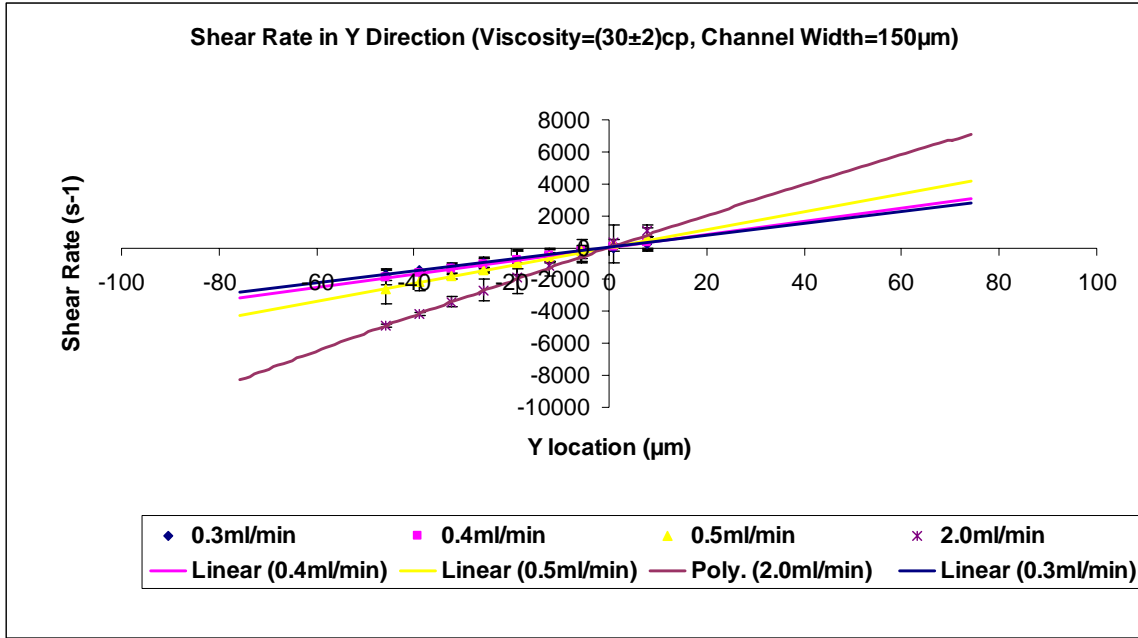
**Fig. 17** Mean velocity across y dimension, a: low viscosity sample, solid lines indicate 5<sup>th</sup> order polynomial regression, dash lines indicate quadratic regression b: high viscosity sample, in channel with 150μm width, solid lines indicate quadratic regression, channel walls are at y=-75μm and y=75μm

### 3.2.2.2 Shear stress across y direction

Figure 18 shows the shear rate component  $\frac{\partial V_x}{\partial y}$  increase as the flow rate increases for low and high viscosity samples in channel with 150 $\mu\text{m}$  width. The shear rate slope increased with increasing flow rate for both sample. The shear rate and shear stress are denoted a direction change instead of the arbitrary values so that it is easy to add a trend.



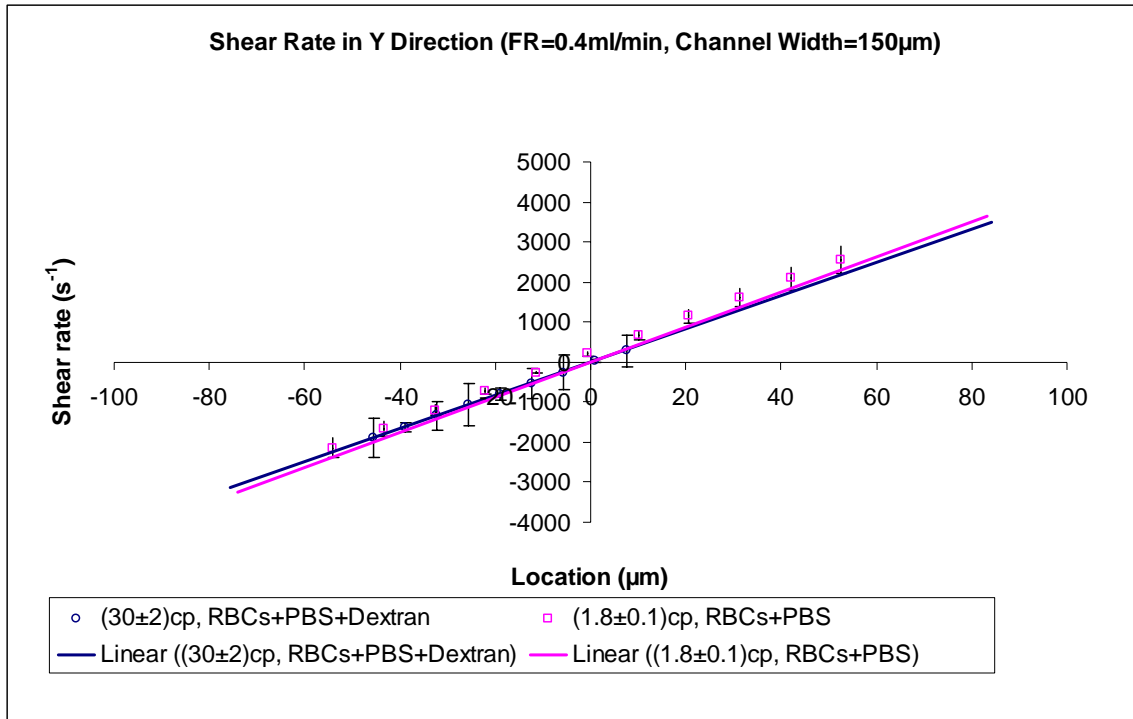
(a)



(b)

**Fig. 18** Shear rate as increasing flow rate, a: low viscosity sample, b: high viscosity sample, in a channel with 150μm width, channel walls are at y=-75μm and y=75μm, solid lines indicate linear regression

Figure 19 shows the comparison of shear rate distribution in the y direction between the high viscosity sample and the low viscosity sample, in channel with 150 $\mu\text{m}$  width. The shear rate is approximately the same.



**Fig. 19** Shear rate comparison between two samples, in a channel with 150 $\mu\text{m}$  width, channel walls are at  $y=-75\mu\text{m}$  and  $y=75\mu\text{m}$ , solid lines indicate linear regression



### 3.2.2.3 Wall shear stress

Figure 20 illustrates the wall shear stress in a micro channel with a width of  $150\mu\text{m}$ . When the flow rate increased to  $2.0\text{ml/min}$ , the wall shear stress could be increased to about  $240\text{Pa}$ .

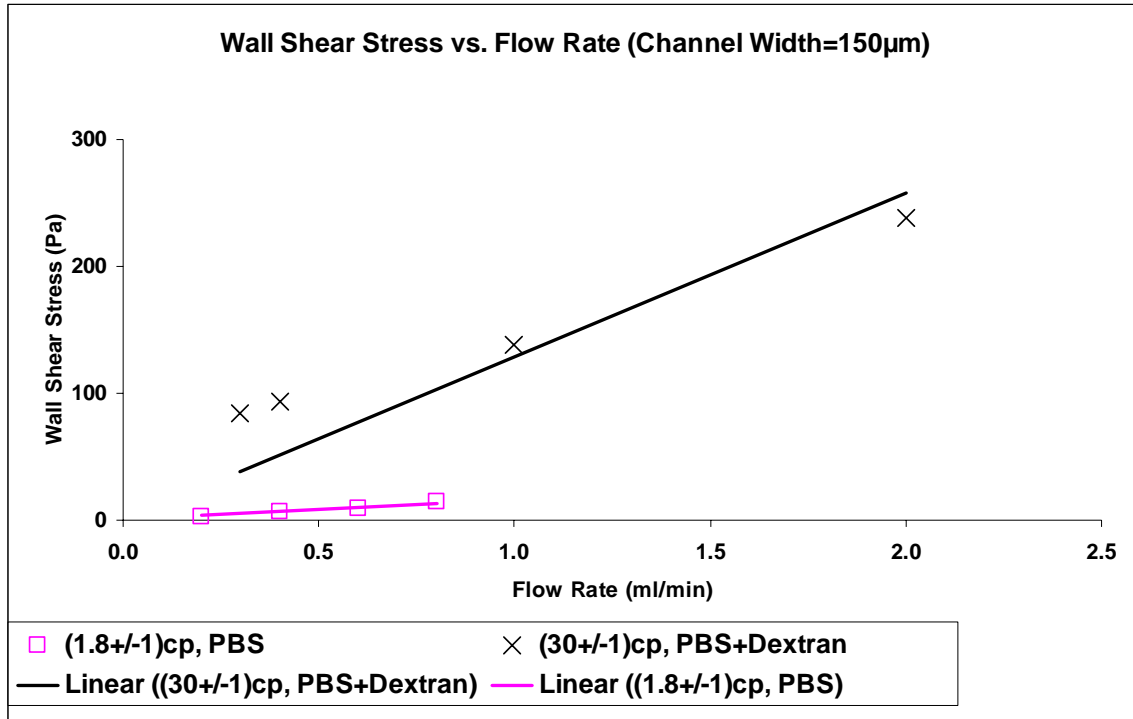
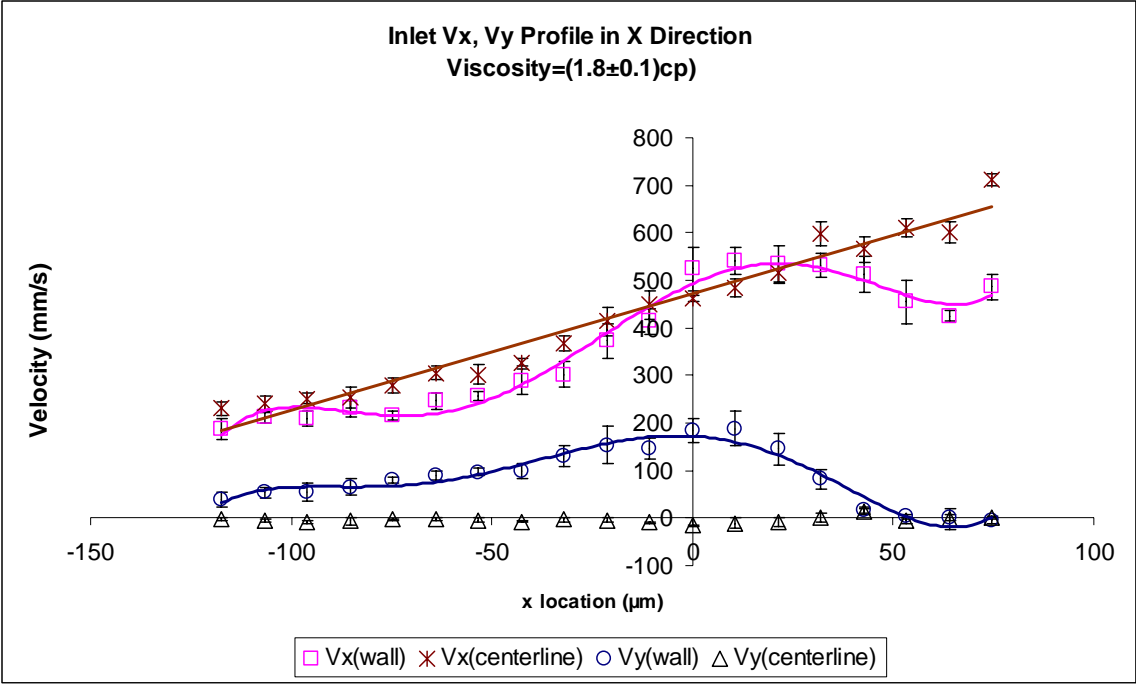


Fig. 20 Wall shear stress, in channel with  $150\mu\text{m}$  width, solid lines indicate linear regression

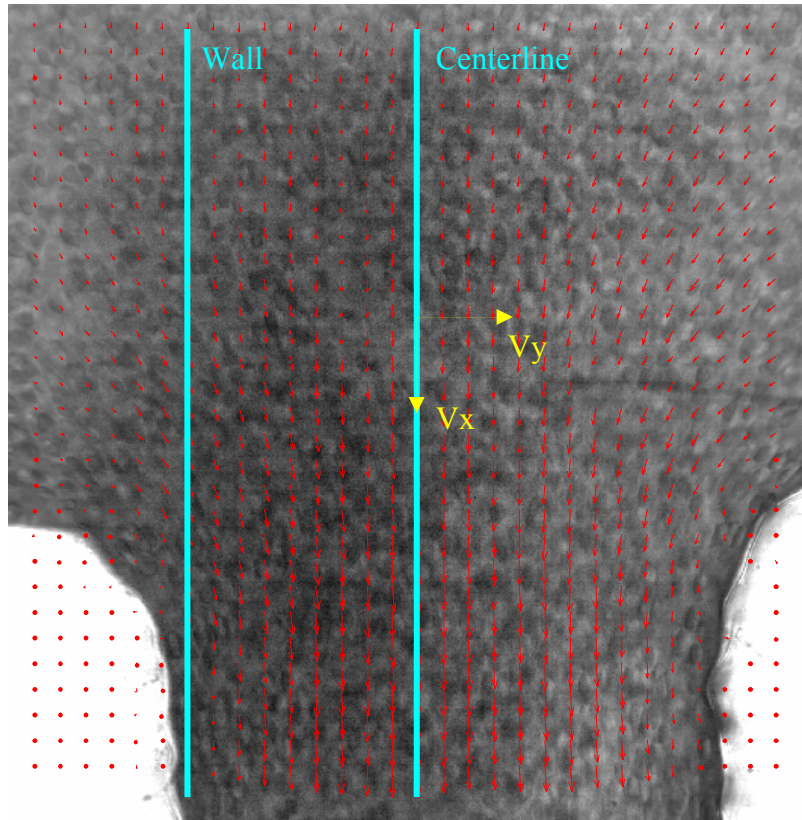
### 3.2.3 At Inlet

The two-dimensional velocity in the x direction was showed in figure 21. Along the centerline,  $V_x$  increased near linearly from  $-118\mu\text{m}$  to  $64\mu\text{m}$  ( $R^2=0.96$ ), while  $V_y$  remained around zero. Along the wall, Both  $V_x$  and  $V_y$  started from a non-zero value, increased outside channel, had the

maximal values at  $x=0\mu\text{m}$  and decreased when the cells entered micro channel.  $V_y$  was decreased all the way down to zero.



(a)

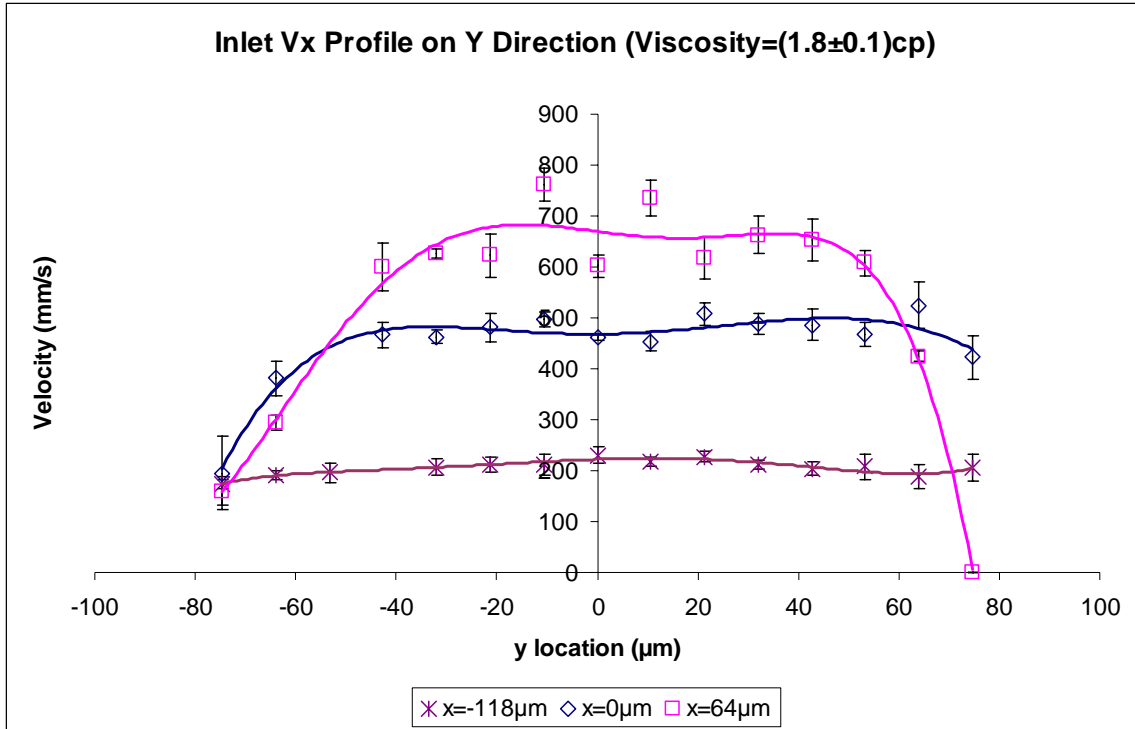


(b)

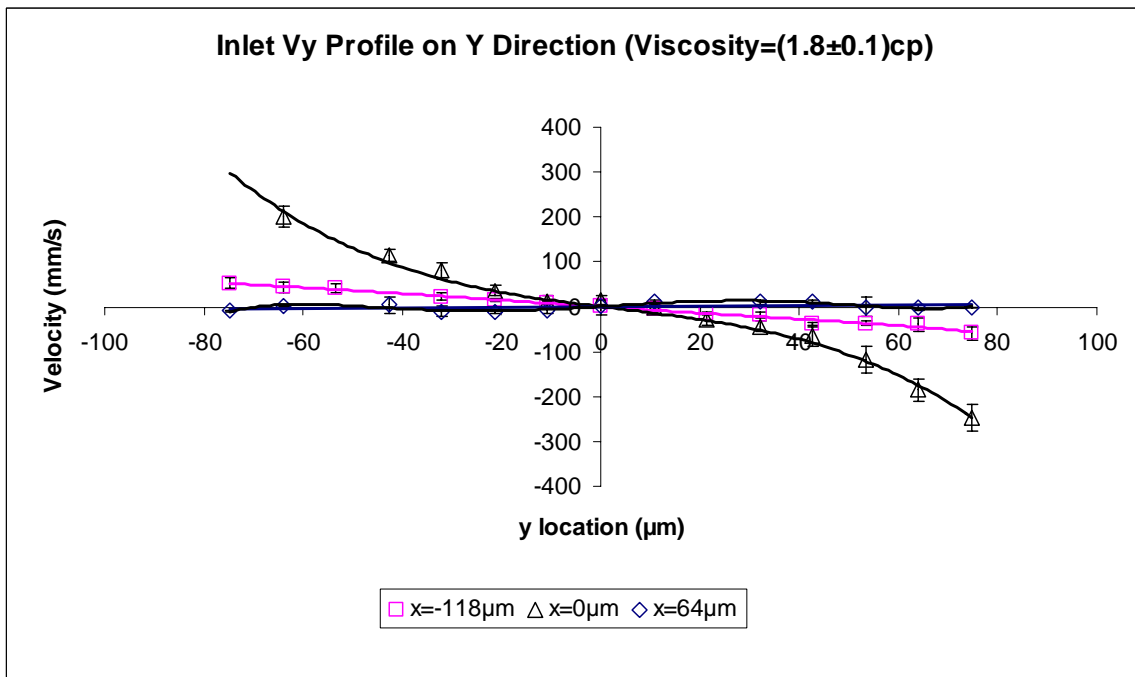
**Fig. 21** Inlet velocity distribution in x direction, a: distribution, b: the location which velocity distribution is taken from, in channel with  $150\mu\text{m}$  width, the solid lines on  $V_x(\text{wall})$  and  $V_y(\text{wall})$  indicate 5<sup>th</sup> order polynomial regression, the solid line on  $V_x(\text{centerline})$  indicate linear regression

From  $118\mu\text{m}$  outside the micro channel to  $64\mu\text{m}$  inside the channel, the velocity on x direction developed from a constant value crossing y direction to a non-fully developed Poiseuille flow. The centerline shear stress remained as zero (fig.22a).

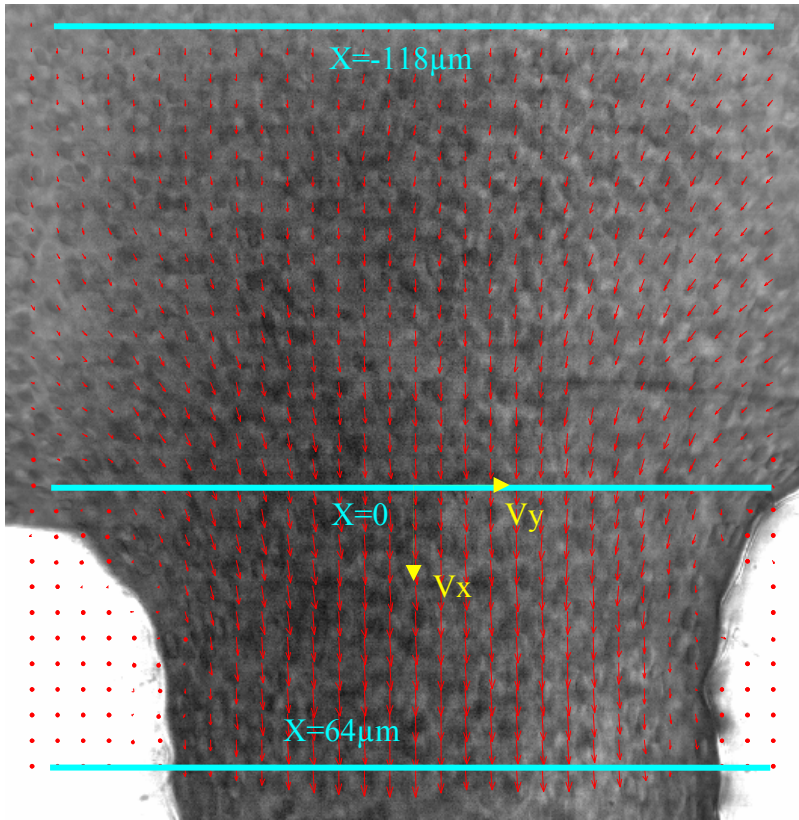
For  $V_y$ , there was a slight convergence at  $x=-118\mu\text{m}$ . The flow continued to aggregate as it moving towards inlet. After inlet, the  $V_y$  decreased to zero across channel width (fig.22b).



(a)



(b)



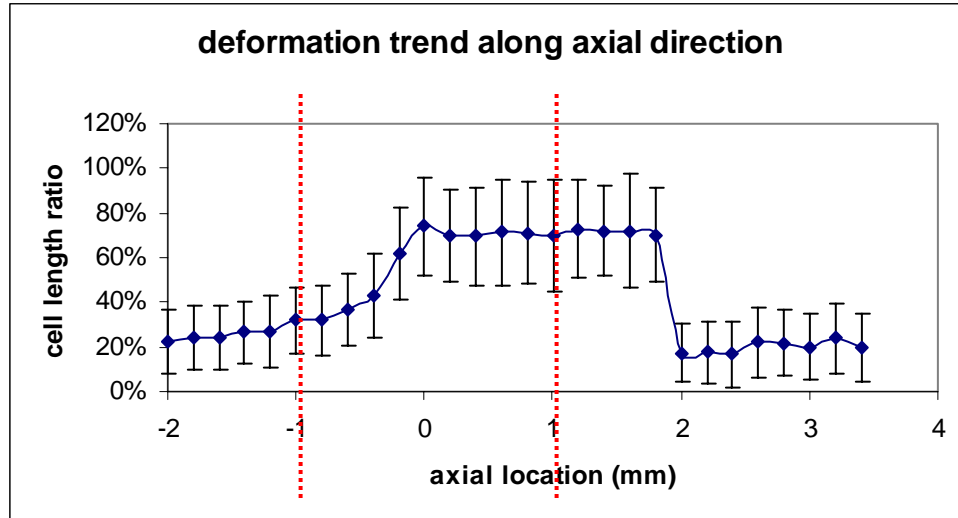
(c)

**Fig. 22** Inlet velocity distribution in  $y$  direction, a:  $V_x$  distribution, b:  $V_y$  distribution c: the location which velocity distribution is taken from, in channel with  $150 \mu\text{m}$  width, the solid lines indicate 5<sup>th</sup> order polynomial regression, channel walls are at  $y = -75 \mu\text{m}$  and  $y = 75 \mu\text{m}$

### 3.3 CELL DEFORMATION

#### 3.3.1 Cell deformation history

In the image processing, many cells were chosen in each of the ten images taken in each of the 30 locations and the mean cell deformation was calculated. Figure 23 shows the cell deformation along the x direction when it was in a 50 $\mu\text{m}$  wide channel. It showed that the cell elongated gradually, reaching a maximum at approximate 0.36mm in front of the inlet. In this area, the overall elongation rate as the change of distance, which is the slope of the linear regression from point 1 to point 9, is 0.71 $\mu\text{m}/\text{mm}$ . At channel inlet, the elongation rate changed dramatically to 8.39 $\mu\text{m}/\text{mm}$ . The cell length changed from 8.04 $\mu\text{m}$  at point 9 to 11.48 $\mu\text{m}$  at point 11. A peak mean value occurred at the 11<sup>th</sup> point, which is the 1<sup>st</sup> point after cell entering inlet. Inside channel, which is from point 11 to point 20, the overall elongation rate is -0.26 $\mu\text{m}/\text{mm}$ . At the outlet of the channel, from point 20 to point 22, cell length rapidly recovered. The mean cell length from point 22 to point 30 is 6.72 $\mu\text{m}$ , slightly smaller than 7.18 $\mu\text{m}$ , which is the mean value from point 1 to point 9.



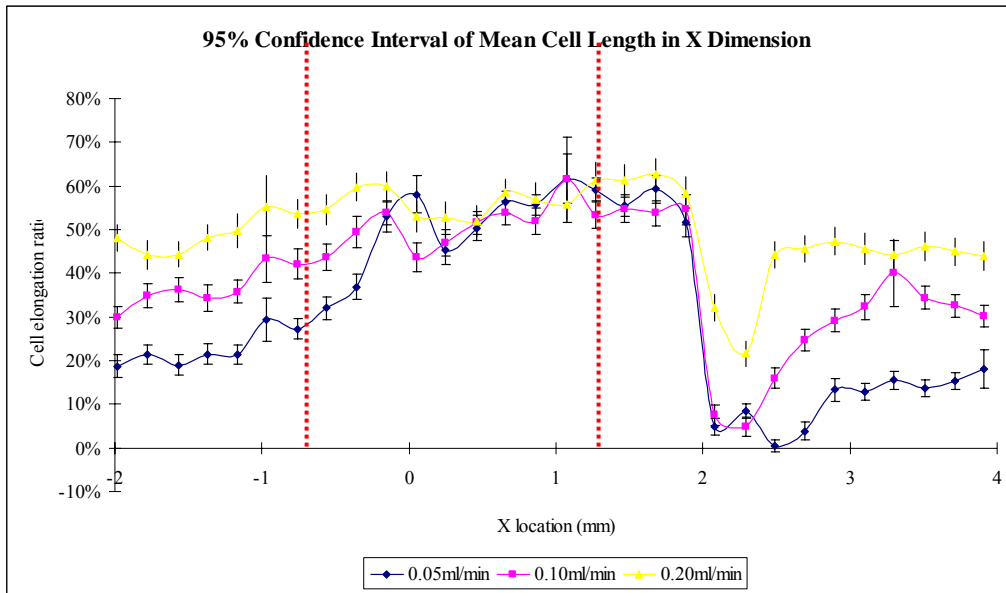
**Fig. 23** Cell deformation on x direction, flow rate=0.05ml/min, inlet: x=0, outlet: x=2mm

### 3.3.2 Cell deformation with changing of flow rate

Figure 24 indicates the cell deformation along x dimension for three different flow rates. Table 4 shows the deformation rate, which is the slope of 1<sup>st</sup> order regression curve when cells are before inlet, at inlet, inside channel, at outlet and out of outlet. Table 3 also shows the mean cell elongations before inlet, inside channel and out of outlet.

The cell deformation in individual flow rate is similar to the result shown in figure 23. When cells are outside the channel, the elongations are increased with the increase of flow rate. The cell length before inlet is a little bit larger than the one after outlet in each flow rate. However, when cells flowed inside channel, their lengths are approximately the same in three flow rate.

As we further increase the flow rate to 2.0ml/min, the cell deformation still remained in a value between 9 $\mu$ m to 10 $\mu$ m while the velocity is proportional to flow rate.



**Fig. 24** Cell deformation on x direction as flow rate changes, inlet: x=0, outlet: x=2mm

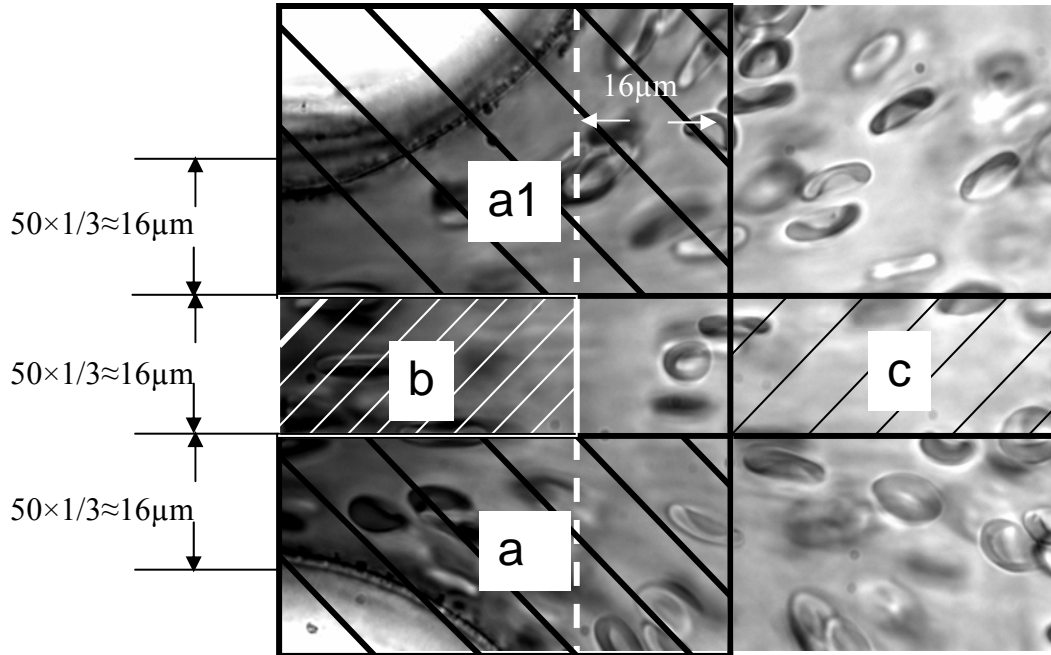


**Table 4** Cell deformation data

Flow rate ml/min		0.050		0.100		0.200	
Point number	distance from inlet (mm)	deformation rate ( $\mu\text{m}/\text{mm}$ )	mean length ( $\mu\text{m}$ )	deformation rate ( $\mu\text{m}/\text{mm}$ )	mean length ( $\mu\text{m}$ )	deformation rate ( $\mu\text{m}/\text{mm}$ )	mean length ( $\mu\text{m}$ )
1~9	-1.98~- 0.36	0.640	7.518	0.610	8.329	0.510	9.051
9~10	-0.36~- 0.15	4.600		1.250		0.020	
11~20	0.05~1.88	0.150	9.317	0.300	9.156	0.300	9.432
20~21	1.88~2.08	-14.040		-14.110		-7.830	
22~30	2.29~3.91	0.520	6.677	0.900	7.626	0.440	8.557

### 3.3.3 Cell deformation at inlet

Figure 25 shows cell deformation at inlet of a  $50\mu\text{m}$  channel. The image was separated to four areas, in which a1 and a2 were denoted as the area near walls, b was denoted as the area around centerline inside channel and c was denoted as the area around centerline outside channel. It shows that area b had the largest deformation.



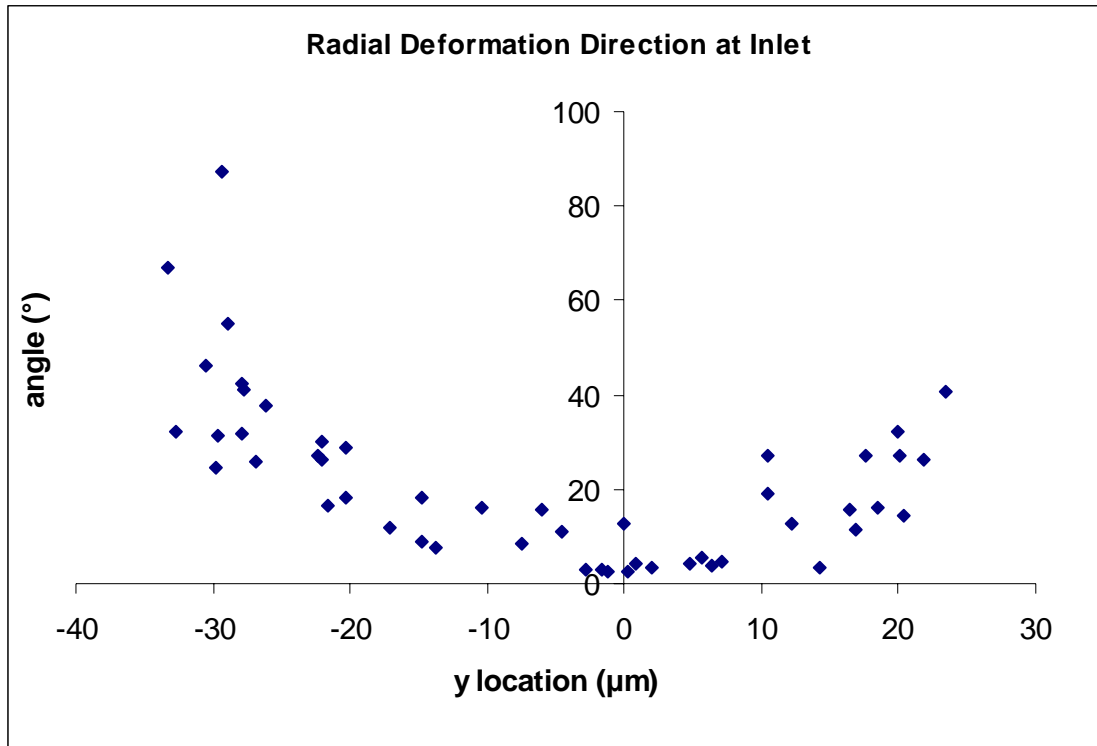
**Fig. 25** Cell deformation at inlet

**Table 5** Cell deformation in four areas

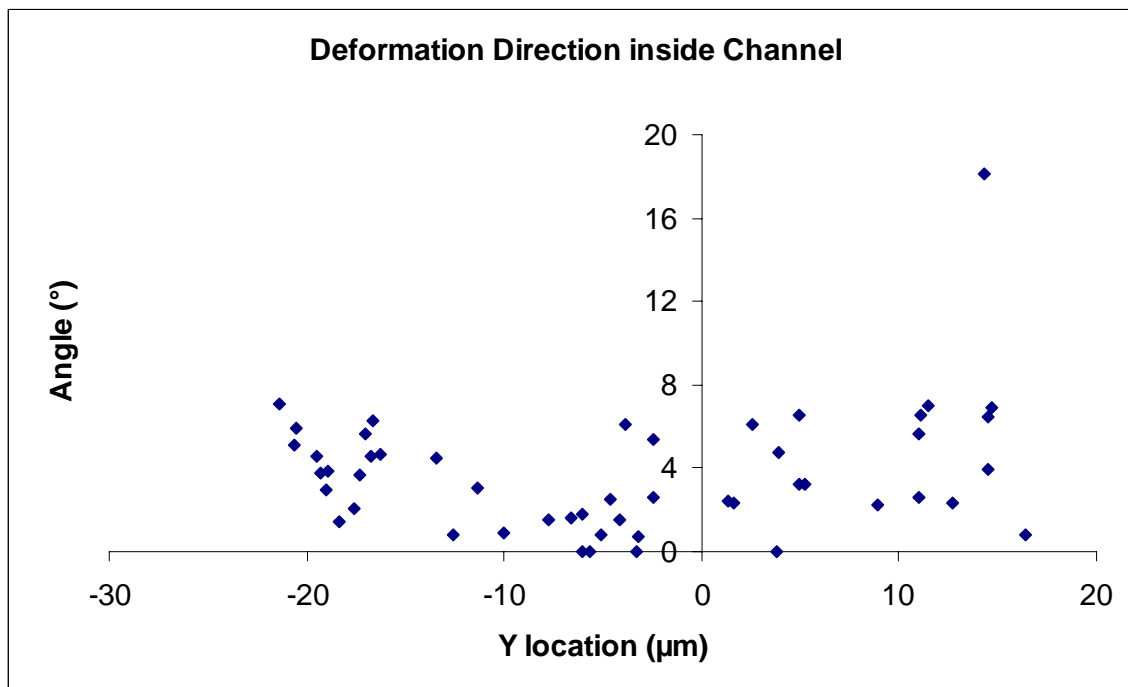
Area	X ends ( $\mu\text{m}$ )		Y ends ( $\mu\text{m}$ )		Cell numbers n	elongation	std
a1	-16	30	35	8	38	38.1%	23.6%
a2	-16	30	-8	8	28	36.9%	16.2%
b	-16	30	-8	-35	22	52.2%	28.0%
c	-60	-16	-8	8	22	17.4%	17.1%

### 3.3.4 Cell deformation orientation

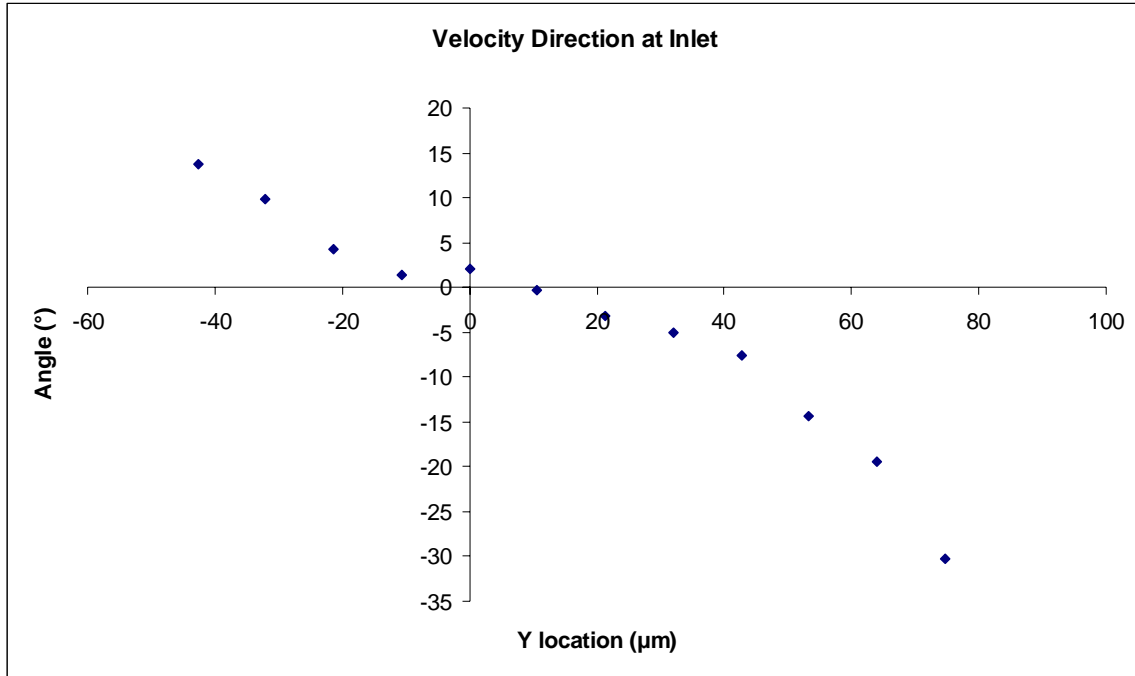
With comparing figure 26a with figure 26c and comparing figure 26b with figure 26d, we can see that cell deformed parallel to the flow direction, both at inlet and inside channel. Our results are coincident with the results of Fischer et al. [11] and [12]. From the velocity profile inside channel (fig.26d), we can see a cell migration towards centerline.



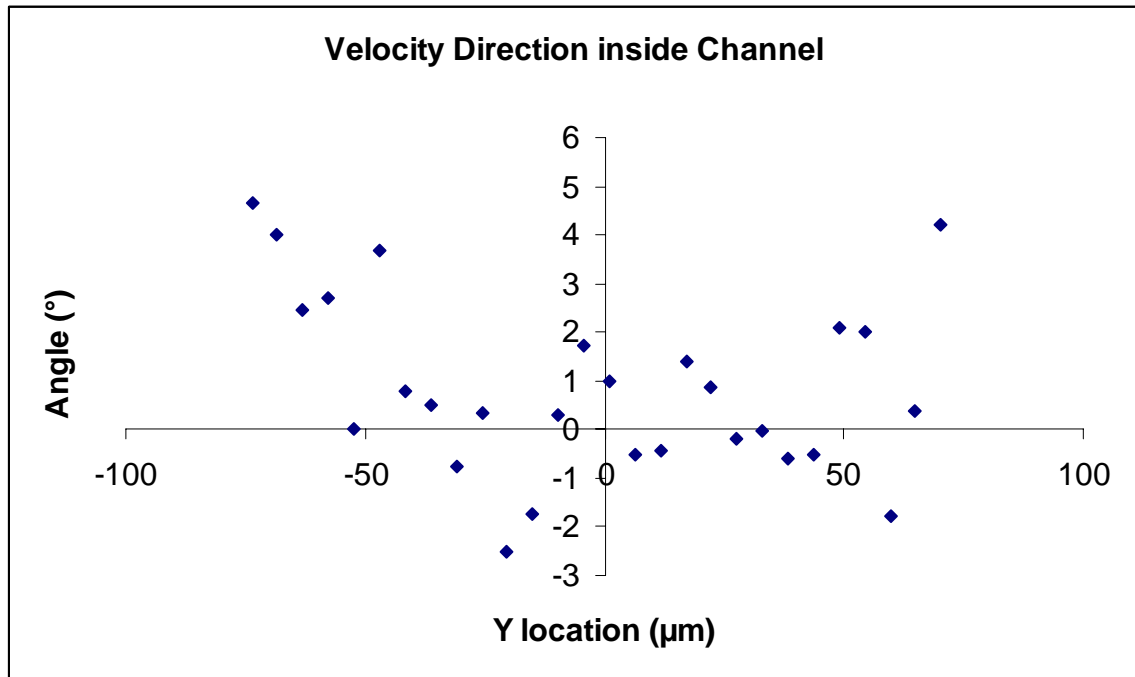
(a)



(b)



(c)



(d)

**Fig. 26** Deformation and velocity direction, a: deformation direction at inlet, b: deformation direction inside channel, c: velocity direction at inlet, d: deformation direction inside channel

## 4.0 DISCUSSION

### 4.1 TWO PHASE FLOW

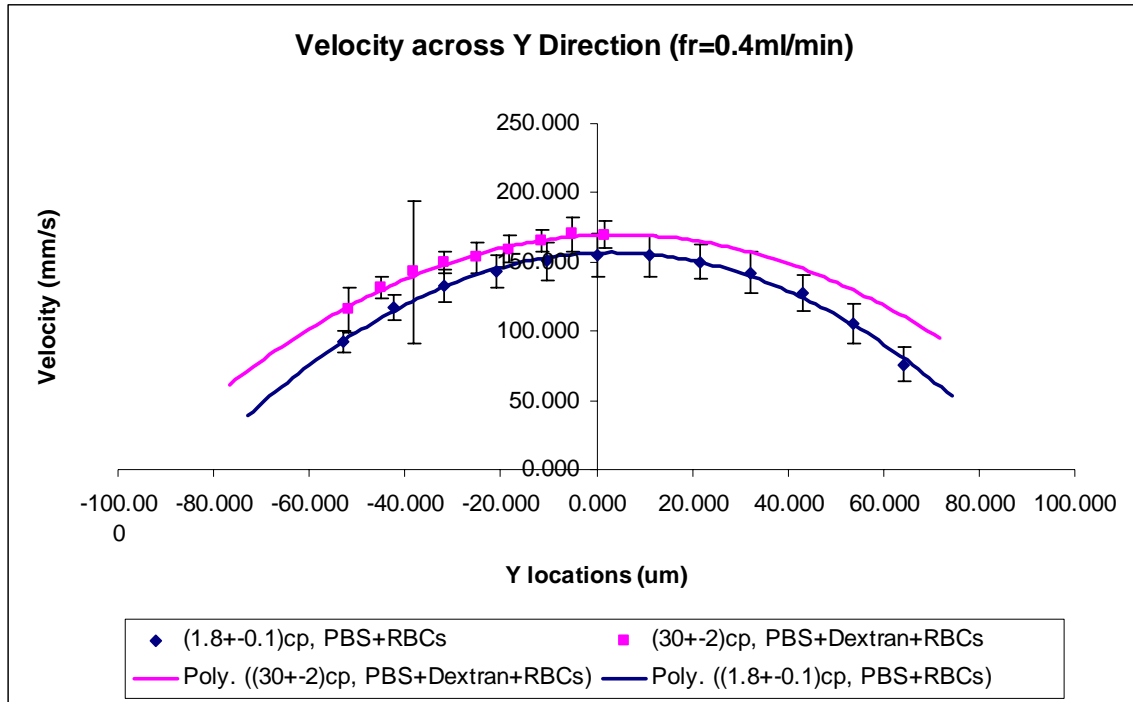
When blood flows through a duct whose hydraulic diameter is comparable to the diameter of red blood cells ( $<200\mu\text{m}$ ), the two-phase composition of blood cannot be ignored. In vitro and in vivo studies have reported unique phenomena due to two-phase flow effect, such as Fahraeus-Lindquist effect near the plasma free layer [50] [51] [52] and a blunted velocity profile [53]. Blood flow in small vessels is typified by a central core of red blood cells and a cell-free layer surrounding the core.

The results presented in the previous chapter (fig.27) shows that the velocity profile across  $y$  direction fits a parabolic curve, for both low viscosity sample ( $R^2>0.98$ ) and high viscosity sample ( $R^2>0.98$ ). The results are consistent with the mathematical model established by Sharan and Popel [54]. They concluded that the bluntness of the velocity profile in the core was inversely related to the diameter of the tube and was directly related to the hematocrit. They used a parameter  $B$  to represent bluntness, with an extreme value of  $B \rightarrow 1$  for a parabolic profile. For a tube with  $150\mu\text{m}$  diameter, the bluntness parameter is more than 0.95 for a blood sample with 20% hematocrit. For the high viscosity sample,  $B$  will be even higher due to the hematocrit being as low as 5%.

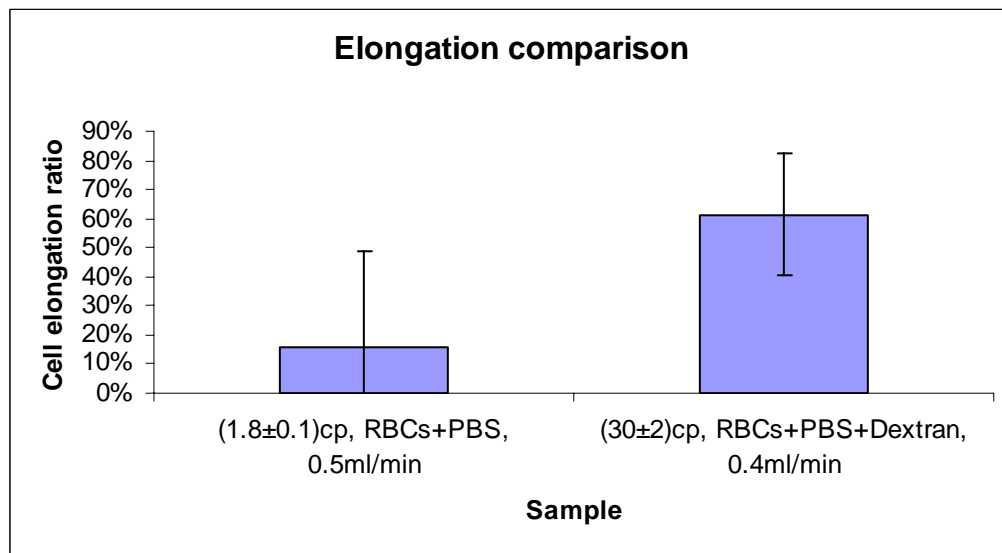
The bluntness due to the cross section geometry can be negligible, as shown in previously.

Between two samples, the velocity is slower in the low viscosity sample, with a hematocrit of 20%. A reason for this phenomenon is the hematocrit difference. The high hematocrit sample has more cells and involves more dissipation of energy due to inelastic cell collisions. Cell deformation and centerline migration may also be reasons for the increase of velocity and wall shear rate (fig.19). At the same flow rate, the shear stress on the cells in the high viscosity samples is much larger than the one on the low viscosity samples. The cell elongation is much higher in the high viscosity sample as shown in figure 28. The cell shows an elongation parallel to flow direction,, and based on the assumption of incompressibility, the dimension normal to flow direction becomes shorter. Both of the cell deformation and cell motion will reduce the cell resistance to the flow, thus to increase the velocity and flow rate.

Another reason for this phenomenon may be the cell free layer present in the flow. The cell free layer thickness is known to increase as the hematocrit decreases [54]. This enlargement causes the image plane for the high viscosity, low hematocrit sample to be higher than the plane for the low viscosity, high hematocrit sample. As in a duct with square cross section area, the velocity will be higher as the image plane moves towards centerline.



**Fig. 27** Effect of viscosity on velocity profile in micro channel



**Fig. 28** Effect of viscosity on cell elongation in micro channel

## 4.2 INLET FLOW

The contraction flow at the channel inlet is extremely important for cell deformation and damage. However, few previous experimental reports describe the micro fluid dynamics under these conditions. Our experiments using micro fabrication technique allows us to elucidate the details of this flow field.

From the definition of extensional flow model we can see that  $V_x$  is only a function of  $x$  and  $V_y$  is only the function of  $y$ . For the velocity changes on  $x$  direction  $\frac{dV}{dx}$ , the  $y$  component of velocity remains as a constant. The same situation happens on  $y$  direction for  $\frac{dV}{dy}$ , with the  $x$  component remaining the same.

The velocity gradients observed along the centerline in our channel, with a 40:3 contraction inlet, was nearly linear in the  $x$ -direction – consistent with the property of extensional flow. Figure 22(a) also shows that for the middle 1/3 of the channel width,  $V_x$  does not change in  $y$  direction. Furthermore, at the location of  $x=-118\mu\text{m}$ , upstream from the throat of the contraction, there was observed a linear gradient of  $V_y$  with constant  $V_x$ , illustrating a pure extensional status. For  $x=64\mu\text{m}$ , the velocity profile changes to a plug flow, with a near zero  $y$  velocity component. Consequently, the extensional effect diminishes as cells flow into channel. The flow proceeds to be fully developed when it moves further into the channel. It shows there is a maximal velocity change near the corner of channel inlet. The maximal stress is located here. The centerline also showed a stress increase at inlet.

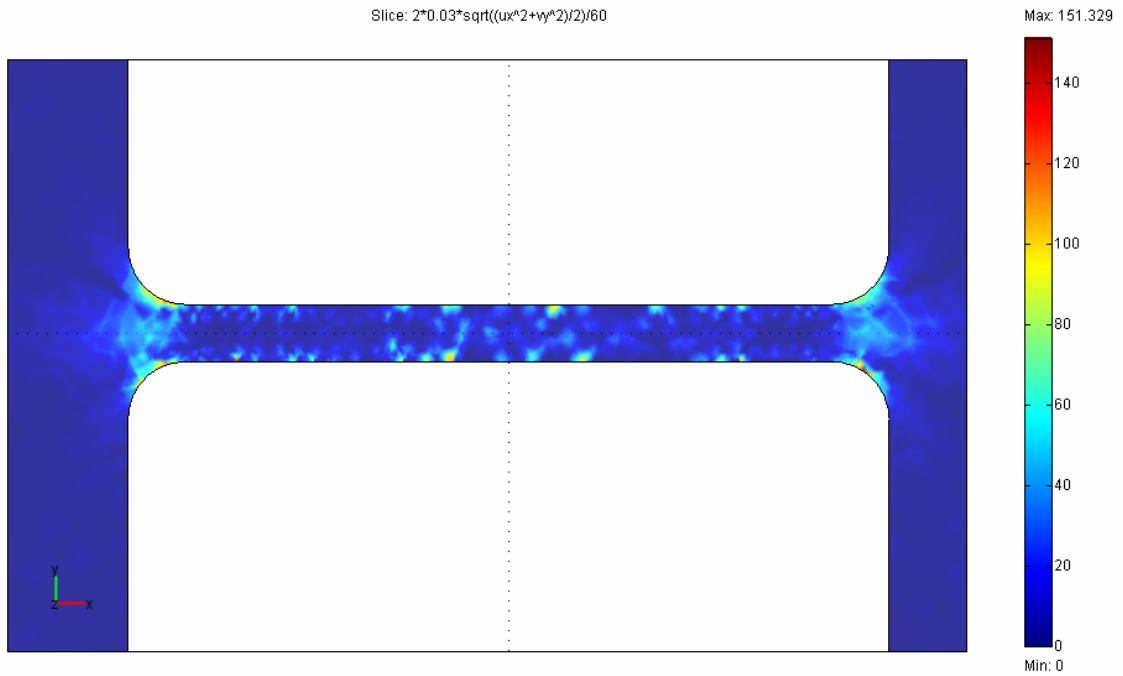


The flow pattern along wall in y direction and the flow pattern at inlet in x direction are more complex. We believe in y direction, there is a shear force due to the interaction between flow and the edge perpendicular to the channel wall, which forces the velocity direction to be altered, with a decrease of  $V_x$  and increase of  $V_y$ .

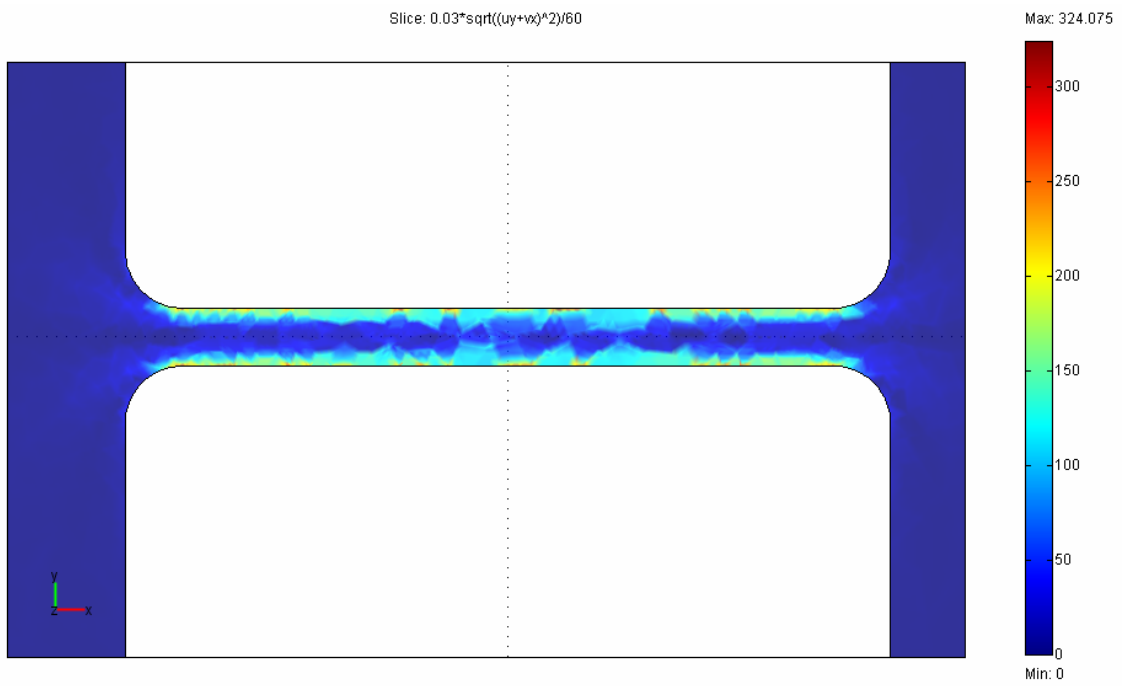
CFD results by solving Navier-Stokes equation also support this analysis. We use FEMLAB (COMSOL, Inc., Los Angeles, CA), a CFD software, to illustrate the flow conditions under the same experimental situation. For the purpose of comparison, figure 29a and figure 29b are calculated without including z direction component, because experimental data can not illustrate the z direction velocity component from images taken from xy plane. The results are consistent with experimental data, with a maximal value at the corner and strong effect on centerline of extensional stress (fig.29a). Shear stress has stronger effect on the wall when z component has not been involved.

CFD also allows us to calculate the stress value which is including z component. The extensional stress is almost the same in figure29a and figure29c. However, the shear stress has great effect from the top and bottom surface, especially on the centerline inside channel.

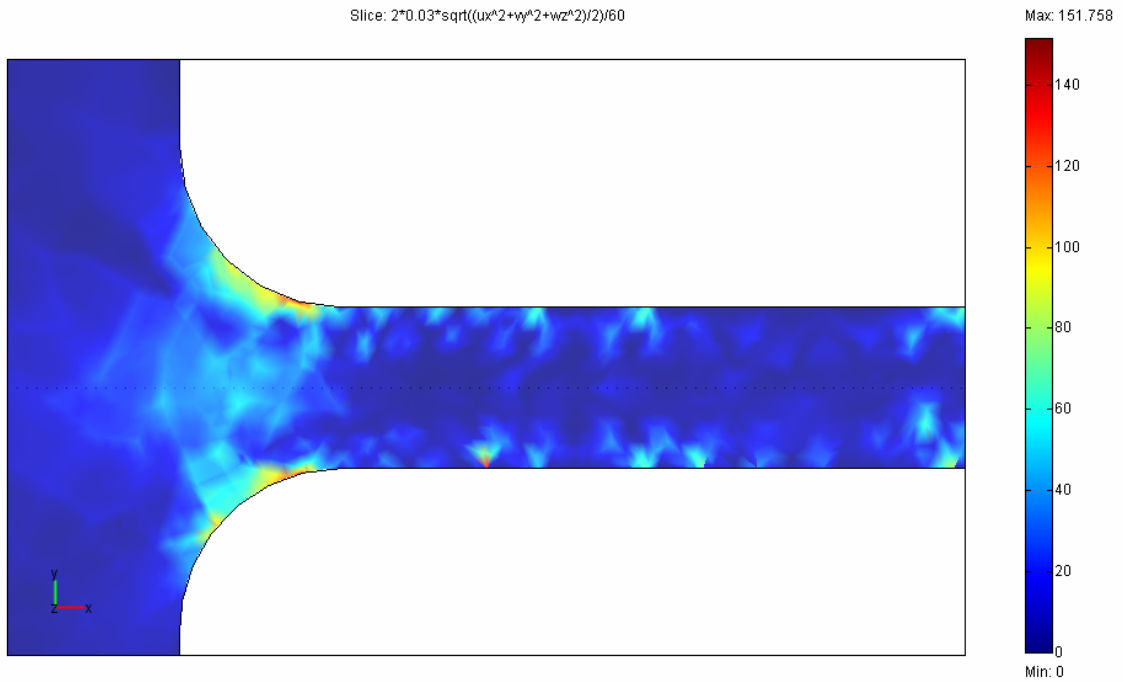
We can summarize that at the inlet, the flow is affected by the combine effect of extensional stress and shear stress. Figure29e shows the combined effect of shear stress and extensional stress.



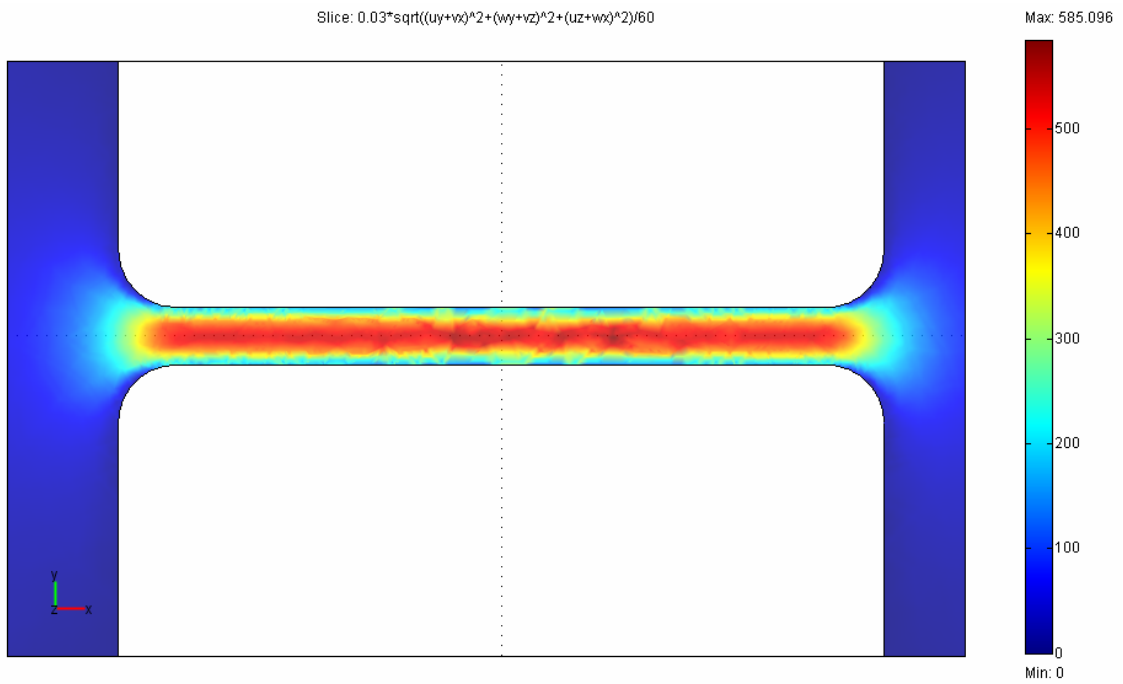
**(a)**



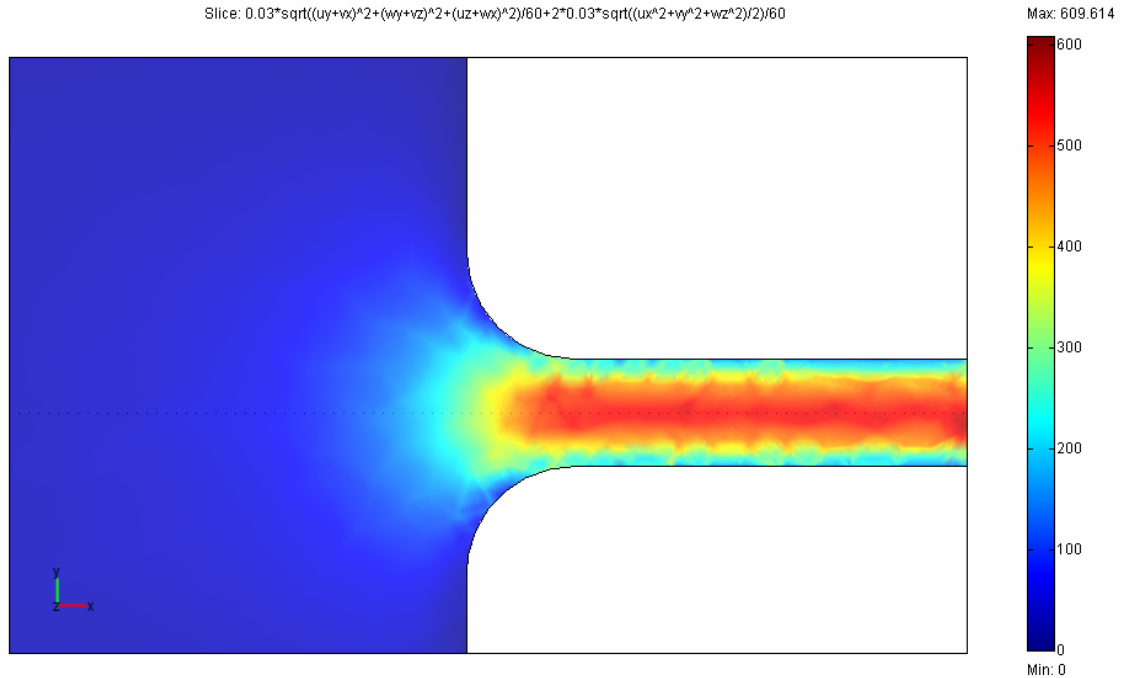
**(b)**



(c)



(d)



**(e)**

**Fig. 29** CFD results of inlet flow conditions, flow rate=0.5ml/min, viscosity=30cp, channel width=150 $\mu$ m, (a): extensional stress w/o z component, (b): shear stress w/o z component, (c): extensional stress w/ z component, (d): shear stress w/ z component, (e): extensional stress and shear stress w/ z component,

The cell deformation profiles observed these studies revealed that the largest deformation occurs at the inlet, surrounding the centerline for 1/3 of the channel width. We believe the maximum deformation at inlet is induced by the combine effect of extensional stress and shear stress.

### **4.3 CELL DEFORMATION**

The cell deformation history shows that the cells deform dramatically near inlet, bearing maximum elongation at inlet and recovering as soon as they flow out of the outlet.

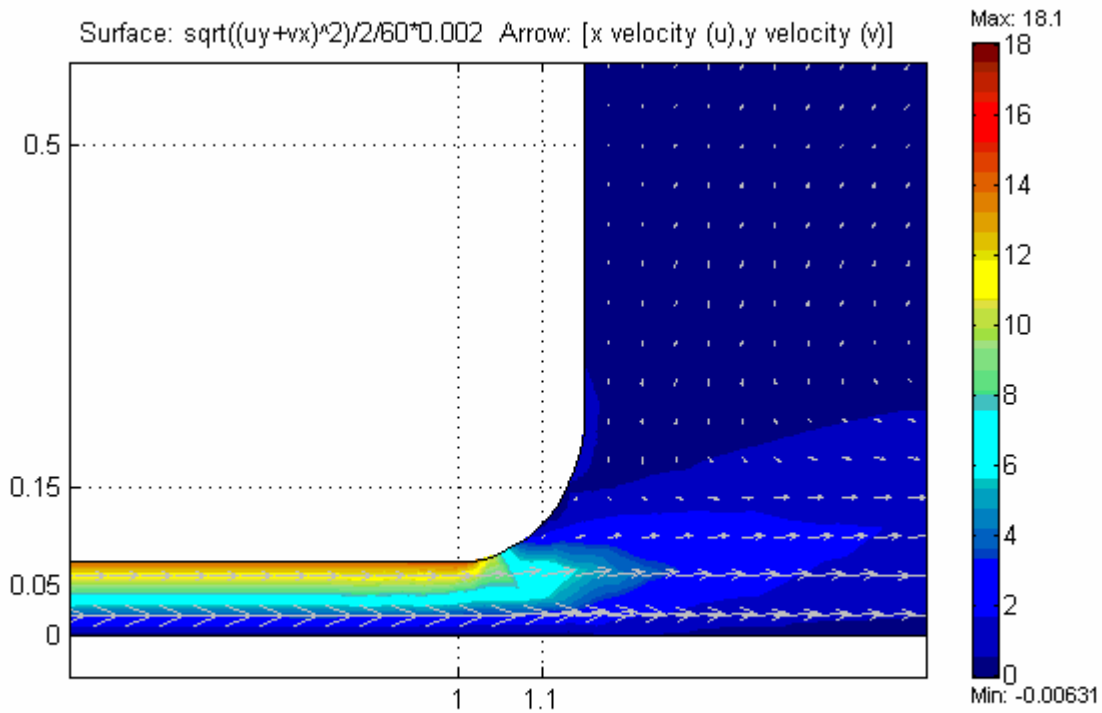
#### **4.3.1 Deformation at inlet**

We believe the maximum deformation at the inlet is induced by the combined effect extensional stress and shear stress. When blood becomes a duct flow, the elongational effect is substituted by shear stress. When pure shear stress acts on cells, cell elongation decrease only slightly.

#### **4.3.2 Deformation at outlet**

At the outlet, cells are found to recover as soon as they exit the channel. That result is quite different from the observation of Sutura et al., which showed a period of about 1 minute for recovery. The reason should be the different exposure time in the two experiments. We conclude that a cell can recover as soon as stress is unloaded after a short exposure time (on the order of micro seconds), but needs some extra time to recover after being exposed to a stress for a longer time (in minutes).

The CFD results show that the rapid decrease of cell deformation could because of the sudden vanish of shear stress, as shown in figure 30(a). There is also showed a rotation of flow at exit, which cause the cell stagnant at exit area and is smaller than the one afterwards.



**Fig. 30** shear stress and velocity at outlet, flow rate=0.5ml/min, viscosity=2cp, channel width=150 $\mu$ m

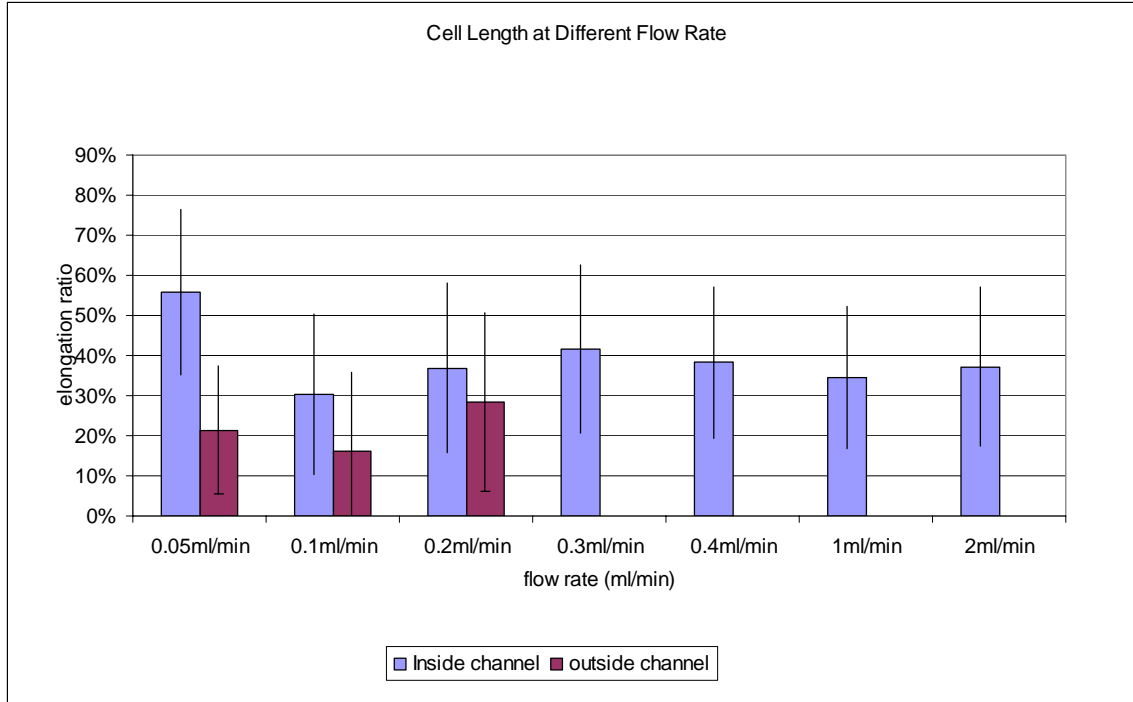
After cells exit, they enter a duct which has a diameter that is much wider than the micro channel. However the net shear  $dv_x/dy$  is virtually the same as the upstream duct. This shear stress is however small and does not influence the deformation on the cell. The deformation is the same as the one before inlet.

At outlet, cell recovers to a diameter which is shorter than the one after exit. The decreased diameter is the result of pure extensional stress.

The results of cell deformation over the x direction are consistent with the macro scale results of Umezu's experiment [34]. In his study, hemolysis was tested in different types of stenosis in a flow loop. The hemolysis in a stenosis with abrupt inlet and tapered outlet is 3 times greater than the one with a tapered inlet and abrupt outlet. Because abrupt connectors caused more hemolysis than tapered ones, we can conclude that the inlet geometry is more important in affecting hemolysis. We found the same phenomenon from our experiment, in which cell bore its maximum deformation at inlet.

#### **4.4 EFFECT OF FLOW RATE**

When flow rate increases, the cell deformation outside channel increased proportionally to the increasing velocity. However, the cells inside the channel demonstrated no further deformation above an asymptotic value, which in this case was  $9.91\mu\text{m}$  in length or 155% of the original diameter (fig.31).



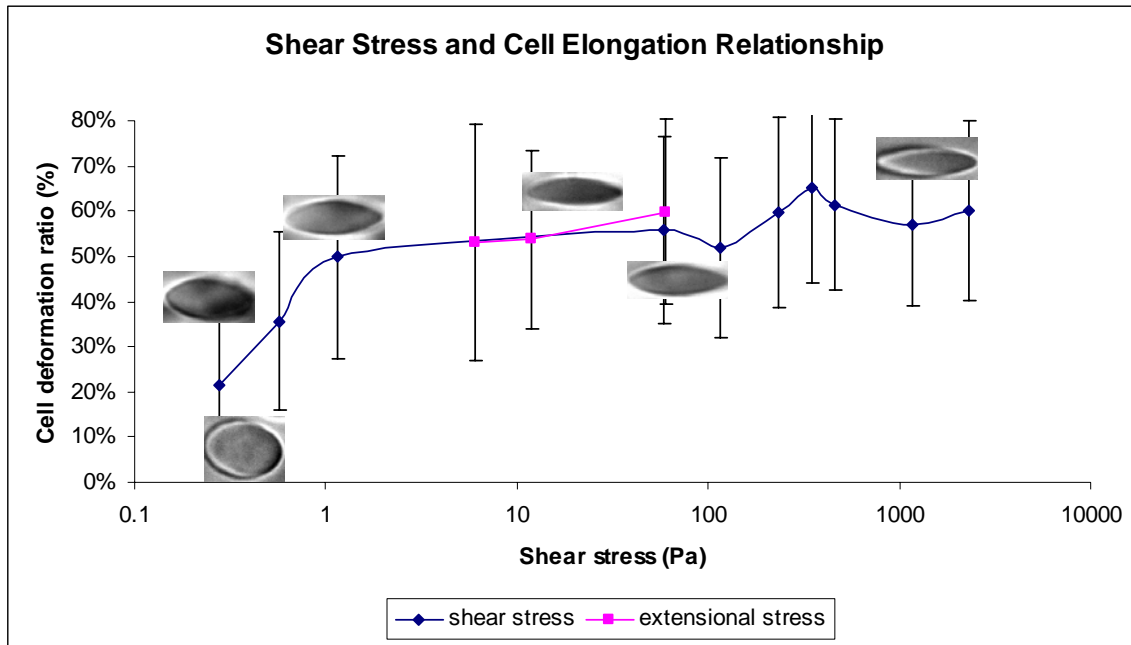
**Fig. 31** Cell deformation inside and outside the channel

Figure 32 shows a summarized relationship of wall shear stress of channel and cell deformation ratio in our experiment. The wall shear stress is calculated from theoretical equation (equation 2). Cell is sensitive to low shear stress from 0 to  $10^{-2}$  Pa. It will reach to a threshold when shear stress extends  $10^{-2}$  Pa, and stay at this threshold as shear stress increases from  $10^{-2}$  Pa to  $10^2$ - $10^3$  Pa.

One explanation for this phenomenon is the elasticity of the cell membrane. A blood cell is sensitive to shear stress and will readily to elongate when exposed to low shear stress. However, as the shear stress increasing, the cell membrane may reach a threshold and stop further elongation, due to the limitation of cell surface area and volume[55] [56] [57]. The measured



critical areal strain is 2-3%, beyond which the cell will be ruptured. A critical membrane tension of  $10^{-2}$  N/m is needed to cause cell rupture. However, a membrane tension of  $10^{-5}$ - $10^{-7}$ , which is much lower than the critical value, can cause the generation of pores on cell membrane, which may result in the sublethal blood damage[56] [58].



**Fig. 32** Relationship of stress and cell elongation, shear stress and extensional stress are calculated from CFD results

The membrane tension is calculated using the method established by Lokhandwalla et al. [58], assuming a steady flow conditions. In their paper, cell deformation was separated to two catalogs: inertial mode, where cell membrane elastic tension is less than the inertial forces generated by surrounding fluid, and viscous mode, where membrane elastic tension is greater than the inertial forces. In viscous mode, the tangential viscous stresses are exerted on the wall and be in equilibrium with membrane elastic tension,  $T_{elas} \approx T_{visc}$ . In inertial mode, viscous stress

is near zero ( $T_{\text{visc}} \approx 0$ ). The equations for calculating  $T_{\text{iner}}$  and  $T_{\text{visc}}$  in steady flow were give in the paper:

$$T_{\text{iner}} = \rho r_c^3 k^2 \quad (21)$$

$$T_{\text{visc}} = \mu k r_c \quad (22)$$

Where,  $\rho$  and  $\mu$  are the density and viscosity of flow, respectively;  $r_c$  is the radius of red blood cells and  $k$  is shear rate.

Our results also shows the cell is in the viscous mode described in their paper, where inertial tension from flow are smaller than the cell membrane elastic tension. The largest membrane tension we can achieve is on the order of  $10^{-3}$ - $10^{-2}$ , which is much lower than the critical tension to rupture cells but large enough to change the cell membrane feature.

At the inlet, the cell has a larger deformation than inside channel. However, the cell exposure time for the extensional flow is much shorter than the cell exposure time for shear flow. We conclude that the combine effects of extensional stress and shear stress can cause larger deformation in a shorter time.

## 5.0 CONCLUSION

An experimental investigation was undertaken to study the cellular dynamics that occurs at “hot-spots” in cardiovascular devices which feature non-uniform high shear stress conditions and are primarily responsible for hemolysis. The flow and cell deformation fields of blood cells were recorded within micro channels in vitro. We conclude that 1) when cells flow through a small gap or clearance, they successively bear a pure extensional stress, a combined effect of extensional stress and shear stress, a pure shear stress, and the unloading of extensional stress and shear stress. 2) cells deform to maximum in a transient time under the combined effect of extensional stress and shear stress when they enter the gap or clearance; 3) the largest possibility for blood damage occurs at the inlet of gaps or clearance; 4) the relationship of cell deformation and shear stress illustrates that cell is sensitive to low shear stress and stay in a threshold at high shear stress; 5) after bearing a high shear stress for a short exposure time, cells recover as soon as stress is relieved; 6) The sublethal damage is more likely to happen than the visible rupture of cells under the situation of “hot-spots”.

## **6.0 FUTURE WORK**

Our findings for the blood damage conditions at “hot-spots” show basic mechanism underlining device-induced blood damage. The methods are proved to be effective and are ready to be applied in further design and optimization. In the future, the investigation can be performed on the following tracks: 1) investigate cell damage in more complex flow conditions; 2) apply the experimental results in the design and optimization of “hot-spots” geometry; 3) Investigate the device effects on pathological cells; 4) investigate the basic mechanism of thrombosis at “hot-spots”.

## APPENDIX A

### CELL DEFORMATION AND LOCATION

```
%%This program is to get the cell deformation and location information
clear,close all;
name=input('the root name of the image?', 's');
time=input('separate time?');
fid=fopen([name '_deformation.txt'],'a');
fprintf(fid,'name of the file= %s \n',name);
fprintf(fid,'separation time= %4d \n',time);
fprintf(fid,'center_x, center_y, length, length_x, length_y (pixel)\n');
for i=1:2:19
    if i<=9                %read the set of two pictures
        im=imread([name '\ name '_00' int2str(i) '.tif']);
    else
        im=imread([name '\ name '_0' int2str(i) '.tif']);
    end
    imshow(im);
    g=ginput;
    L=length(g);
    for p=1:2:(L-1)
        center((p+1)/2,1)=(g(p,1)+g((p+1),1))./2;
        center((p+1)/2,2)=(g(p,2)+g((p+1),2))./2;
        leng((p+1)/2)=sqrt((g(p,1)-g((p+1),1)).^2+(g(p,2)-g((p+1),2)).^2);
        lxy((p+1)/2,1)=abs(g(p,1)-g((p+1),1));
        lxy((p+1)/2,2)=abs(g(p,2)-g((p+1),2));
        data1=center((p+1)/2,1);
        data2=center((p+1)/2,2);
        data3=leng((p+1)/2);
        data4=lxy((p+1)/2,1);
        data5=lxy((p+1)/2,2);
        fprintf(fid, '%10.3f, %10.3f, %10.3f, %10.3f, %10.3f\n', data1,data2,data3,data4,data5);
    end
end
end
```

```
fopen([name '_deformation.txt'],'r');
```

## APPENDIX B

### MEAN AND STANDARD DEVIATION

```
%This function is to get the mean and standard deviation of x values at
%fixed y location.
%lox=x location; loy=y location;vx=velocity of x direction; vy=velocity of
%y direction;
function [mn,sd]=sdvec(name);
file=importdata([name '.vec']); %load .vec file
data=file.data; %load data part of the file
lox=data(:,1);
loy=data(:,2);
vx=data(:,3);
vy=data(:,4);
j=1;
for i=132:64:900
    ii=find(loy==i);
    fx=vx(ii); %find vx at the location of particular y value.
    fy=vy(ii);
    iii=find(fx); %find fx which is not equal to zero
    nonzerofx=fx(iii);
    nonzerofy=fy(iii);
    iv=find((atan(nonzerofy./nonzerofx).*180./3.14)<10);
    ffx=nonzerofx(iv);
    mn(j,1:2)=[i,mean(ffx)]; %mean and sd are both j*2 matrices
    sd(j,1:2)=[i,std(ffx)];
    j=j+1;
end

%%Main program
clear,close all;
name=input('the root name of the files?', 's');
```

```

n=input('the last file number?', 's');
time=input('separate time?');           %input separation time, unit 'us'
fid=fopen([name '_mean and sd.txt'], 'a');
fprintf(fid, 'file name: %s\n', name);
fprintf(fid, 'separate time: %4d us\n', time);
fprintf(fid, 'loc_Y, Mean_X_D, STD_X_D, \n');
for i=1:2:n
    if i<=9
        NM=[name '_00' int2str(i)];
    else
        NM=[name '_0' int2str(i)];
    end
    [mn, sd]=sdvec(NM);    %mn means 'mean'.
    loy=mn(:, 1);
    meanvx=mn(:, 2);
    sdvx=sd(:, 2);
    s=length(loy);
    for j=1:s
        fprintf(fid, '%10.3f, %10.3f, %10.3f\n', loy(j, 1), meanvx(j, 1), sdvx(j, 1));
    end
end
fid=fopen([name '_mean and sd.txt'], 'r');

```



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